

2110413 Computer Security

Lecture 9 Quantum Key Distribution

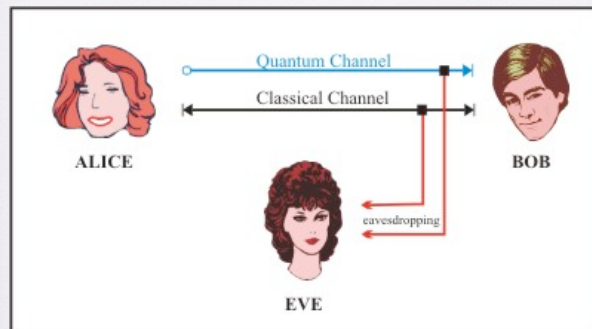
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Outline

- Motivation
- About Quantum
- Algorithm
- Why does it secure?

Detailed Walkthrough



Message

H E L P
00111 00100 01011 01111



ALICE

0



BOB

Message

H E L P
00111 00100 01011 01111



ALICE



BOB



Message

H E L P
00111 00100 01011 01111



ALICE



BOB



EVE

Message

H E L P
00111 00100 01011 01111



ALICE



BOB



EVE

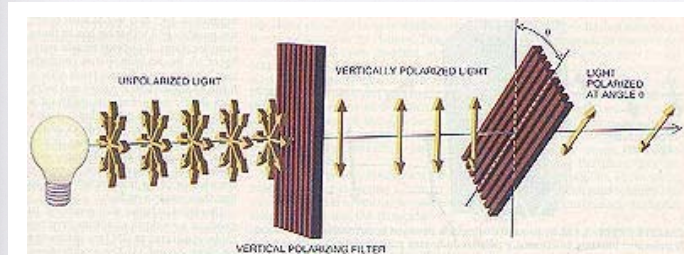
Private communication

Alice and Bob share a one-time pad
(secret random key).

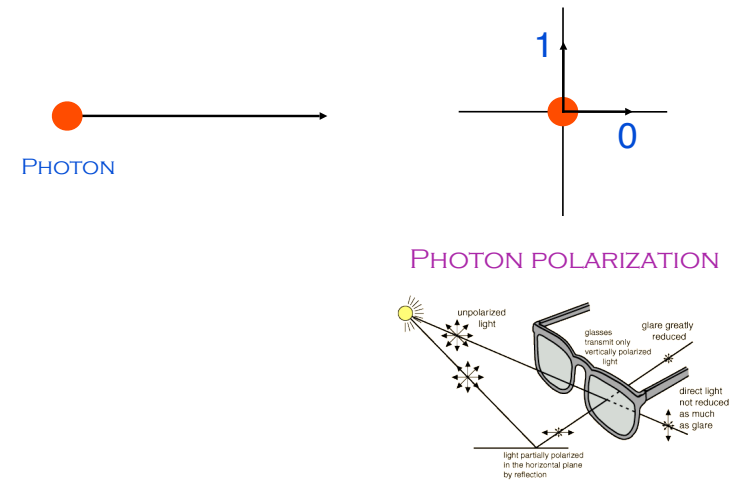
	00111001000101101111	Message
⊕	<u>01110010011010010011</u>	Key (random string)
	01001011011111111100	Coded message
⊕	<u>01110010011010010011</u>	Key (random string)
	00111001000101101111	Message

But where do Alice and Bob get the key?

Quantum



Qubits: Two-state quantum systems



How does it work?

 ALICE	Bit sequence, $s[i]$	0	0	1	1	0
	Encoding bases, $b[i]$	R	D	R	D	D
	Transmitted photons	→	↗	↑	↖	↗
 EVE	Eve's measurement bases, $eb[i]$	R	R	D	D	D
	Eve's measurement results, $es[i]$	0	1	0	1	0
	New, transmitted photons	→	↑	↗	↖	↗
 BOB	Bob's measurement bases, $b'[i]$	R	D	D	R	D
	Bob's measurement results, $s'[i]$	0	1	0	0	0
	eavesdropping detected and communication aborted					
FINAL KEY would have been:		0		0		

"TWO-BIT" DEVICE



RULES

1. AN INTERLOCK MECHANISM PERMITS ONLY ONE BOX AT A TIME TO BE OPENED.
2. WHEN A BOX IS OPENED, THE INTERLOCK ALSO CAUSES A RANDOM BIT TO BE PLACED IN THE OTHER BOX.

INFORMATION CAPACITY = 1 BIT

IF YOU TRY TO SEND 2 BITS ENCODED IN WHICH BOX AND WHAT'S IN THAT BOX, YOU END UP SENDING ONLY HALF A BIT.

Secret key distribution



ALICE



BOB

0 r

X

Secret key distribution



ALICE



BOB

0

X

0 s

X Y

Secret key distribution



ALICE



BOB

0 r

X

Secret key distribution



ALICE



BOB

0

X

s t

X Y

Secret key distribution



ALICE

1 0 1 0 0 1 0 0 0 1
X X Y X Y Y X Y Y



BOB

r r r 0 r 1 r 0 0 r
Y Y X X X Y X X Y X

ALICE AND BOB ANNOUNCE THEIR BOX SEQUENCES PUBLICLY
AND KEEP THE BITS ONLY WHEN THE BOXES AGREE. THIS
PROCESS, CALLED SIFTING, YIELDS A SHARED SECRET KEY, IN
THIS CASE
0100
THE KEY GENERATION RATE IS 50% (1/2 BIT PER TRY).



ALICE

1 0 1 0 0 1 0 0 0 1
X X Y X Y Y X Y Y



BOB

r r r 0 r s r s 0 r
Y Y X X X Y X X Y X

r r r 0 0 r 0
Y Y X X Y X

HEH, HEH,
HEH.

ERROR CORRECTION AND
PRIVACY AMPLIFICATION ALLOW
ALICE AND BOB TO EXTRACT A
SECRET KEY PROVIDED THE
ERROR RATE DOES NOT EXCEED
17.1%.



EVE

FLAW: IF EVE CAN DEACTIVATE THE
INTERLOCK, SHE CAN OPEN BOTH
BOXES AND DETERMINE THE SIFTED
KEY WITHOUT INTRODUCING
ERRORS.

Secret key distribution



ALICE

QUANTUM MECHANICS TO THE RESCUE!
FOR QUANTUM SYSTEMS, THE TWO RULES ARE
CONSEQUENCES OF THE LAWS OF QUANTUM
MECHANICS: THERE IS NO HIDDEN INTERLOCK
MECHANISM TO BE DE-ACTIVATED.



BOB



EVE

RATS!
FOILED AGAIN. I HATE
THOSE QUANTUM
MECHANICIANS.

Alice sends photons with one of the four polarizations, chosen at random.



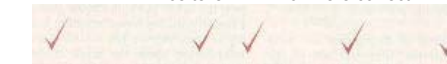
For each photon, Bob chooses at random the type of measurement: + or X



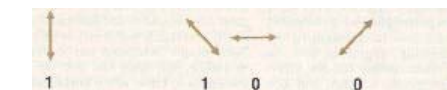
Bob records the result of his measurements, but keeps it a secret.



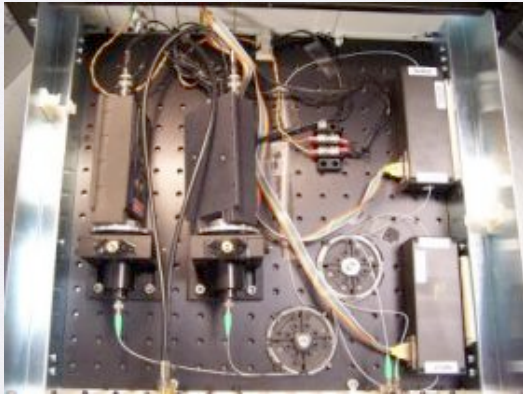
Bob tells Alice the measurement types used (but not results) in freespace.
Alice tells him which were correct.



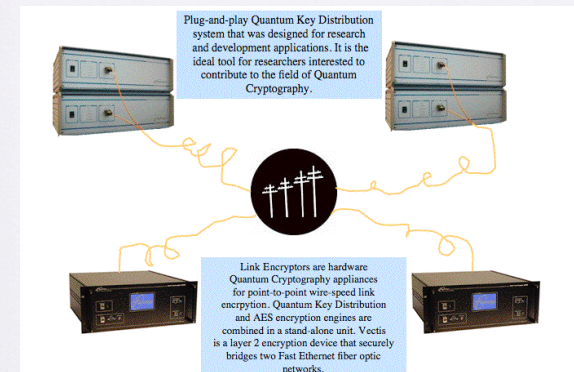
Alice and Bob keep correct cases and translate to 0's and 1's



Real Device



for Sale!



Why is quantum key distribution secure?

An unopened box has no bit value waiting to be discovered. Alice and Bob create the key by opening their boxes. Before that, there is no key for Eve to steal.

"There is no there there."
Gertrude Stein damning her native Oakland and inadvertently describing quantum systems.

Essential ingredient: Entanglement between qubits