# A Tutorial on Machine Vision <br> Prabhas Chongstitvatana <br> Department of Computer Engineering <br> Chulalongkorn University <br> prabhas@chula.ac.th 

- Motivation

What is Machine Vision
Its applications

- Fundamentals
- Specific to Robocup


## Fundamentals

## Camera model

$1 / u+1 / v=1 / f$
$u$ the distance from the lens to the object v the distance from the lens to the image $f$ the focal length
$\mathrm{M}=$ image size/ object size
$\mathrm{f}=\mathrm{uM} /(\mathrm{M}+1)$

## Example

a 10 cm object, with a camera sensor $8.8 \times 6.6 \mathrm{~mm}$., from the distance 0.5 m . find f
$\mathrm{M}=8.8 / 100=0.088, \mathrm{f}=500 \times 0.088 / 1.088=40.44 \mathrm{~mm}$.
select $\mathrm{f}=35 \mathrm{~mm}$.

- image sensor CCD
- video standard NTSC (USA, JAPAN), CCIR (Thailand, Europe)


## CCIR

- picture rate 50 Hz (20ms)
- odd/even line (interlace scanning) picture frame rate 25 Hz .
- each frame 625 lines line frequency $625 \times 25=15625 \mathrm{~Hz}$ ( 64 us )
- 11.5 us for blanking and synchronizing
- 4:3 horizontal-to-vertical aspect ratio


## Image Acquisition

sensor sampling frequency
bandwidth of the video signal
A/D sampling frequency (frame grabber)

## Sampling

- Spatial frequency components
high spatial frequency correspond to quick changes in the image intensity
- Nyquist frequency


## Effective resolving power of the image acquisition system

A sensor with 756 sites (along a line) can capture only the signal of spatial frequency 378 Hz
CCIR line frequency is 15625 Hz , the nominal bandwidth 5 MHz , max spatial frequency of video signal is 5 x $10^{\wedge} 6 / 15625=320 \mathrm{~Hz}$
a frame grabber with sampling rate 512 pixels (in horizontal), can capture only 256 Hz signal.

## Aspect ratio

4:3 horizontal-to-vertical
video signal 100:100 --> image 100:75 (frame store)
CCIR 625 lines, only 576 lines are used for visual information
framestore with vertical resolution 512 pixels so
effective aspect ratio $4:(3 \times 512 / 576)=3: 2$
the effective pixel distance
vertical 1
horizontal 3/2
diagonal sqrt(13/4)

## Digital Image Processing

## - point

contrast streching
thresholding
noise suppression by image addition
background subtraction

- neighbourhood
convolution
noise suppression by averaging
low pass filter
using median
Gaussian smoothing


## Gaussing function

$\mathrm{G}(\mathrm{x}, \mathrm{y})=1 / 2 \mathrm{pi} \mathrm{g}^{\wedge} 2\left(\exp \left[-\left(\mathrm{x}^{\wedge} 2+\mathrm{y}^{\wedge} 2\right) / 2 \mathrm{~g}^{\wedge} 2\right]\right.$
where g defines the effective spreading
$\mathrm{g}=1.5$
$\mathrm{G}(\mathrm{x}, \mathrm{y})=3,28,135,411,800,1000,800,411,135,28,3$
decide max amplitude 1000
thinning, erosion, dilation
(mathematical morphology)
erosion
for all pixel
if pixel is an object AND all its neighbours are objects
copy it
dilation

```
for all pixel
    if pixel is an object
        copy it and its eight neighbour
```

geometric

- spatial warping
a spatial transformation
an interpolation scheme
$(\mathrm{i}, \mathrm{j})=(\mathrm{Wx}(\mathrm{x}, \mathrm{y}), \mathrm{Wy}(\mathrm{x}, \mathrm{y}))$
$W x(x, y)=\operatorname{sum} p$ sum $q \mathbf{a} \_p q x^{\wedge} p y^{\wedge} q$
(for $\mathrm{n}=2$, nine terms)
$W y(x, y)=\operatorname{sum} p \operatorname{sum} q b \_p q x^{\wedge} p y^{\wedge} q$
(for $\mathrm{n}=2$, nine terms)
find $a \_p q, b \_p q$

1 Know transformation exactly for a number of points (nine)
2 know $\mathrm{x}, \mathrm{y}$ and their corresponding i,j
3 to solve the equation of nine unknowns, needs at least nine observations

## Grey-scale Interpolation

- nearest-neighbour
- first order interpolation (bi-linear) (4-neighbour)

34
12
Fit a hyperbolic paraboloid surface defined by the bilinear equation:
$f(p, q)=a p+b q+c p q+d$
determine $\mathrm{a}, \mathrm{b}, \mathrm{c}, \mathrm{d}$
$\mathrm{d}=\mathrm{f} 1$
$\mathrm{b}=\mathrm{f} 2-\mathrm{f} 1$
$\mathrm{a}=\mathrm{f} 3-\mathrm{f} 1$
$\mathrm{c}=\mathrm{f} 4+\mathrm{f} 1-\mathrm{f} 3-\mathrm{f} 2$
example
60,129[12] 61,129 [15]
60,128 [10] 61,128 [14]
What is the grey-value at $(60.4,128.1)$ ?
$f(0.4,0.1)=(14-10) \times 0.4+(12-10) \times 0.1+(15+10-14-12) \times 0.4 \times 0.1+10$
$=11.76$

## Segmentation

## thresholding

$\mathrm{T}=\mathrm{T}(\mathrm{x}, \mathrm{y}, \mathrm{N}(\mathrm{x}, \mathrm{y}), \mathrm{g}(\mathrm{x}, \mathrm{y}))$
if $\mathrm{g}(\mathrm{x}, \mathrm{y})>\mathrm{T} \quad(\mathrm{x}, \mathrm{y})$ is labelled an object
$\mathrm{g}(\mathrm{x}, \mathrm{y})$ grey-level
$\mathrm{N}(\mathrm{x}, \mathrm{y})$ neighbour
$\mathrm{x}, \mathrm{y}$ point co-ordinate

Global, Local, Dynamic

## Global threshold

- find threshold by histogram
- bi-modal, multi-modal
- smooth histogram (3x1) averaging operator
- use grey pixels which lie on the boundary

Which pixels are on the boundary?
Use Marr-Hildreth operator to find edges
$\mathrm{T}=$ mean of edge pixels

## Edge detection

- gradient, difference-based
- template matching


## Gradient

the first difference
x-direction: $f(x+1, y)-f(x, y)$
$y$-direction: $f(x, y+1)-f(x, y)$

## 34

12

## Roberts operator

$g(x, y)=\operatorname{sqrt}\left[\{f 1-f 4\}^{\wedge} 2+\{f 3-f 2\}^{\wedge} 2\right] \quad$ RMS of directional differences
$g(x, y)=|\mathrm{f} 1-\mathrm{f} 4|+|\mathrm{f} 3-\mathrm{f} 2| \quad$ Absolute
$\mathrm{g}(\mathrm{x}, \mathrm{y})=\operatorname{Max}(|\mathrm{f} 1-\mathrm{f} 4|,|\mathrm{f} 3-\mathrm{f} 2|) \quad$ Rosenfeld and Kak
Combining differencing and local average (to reduce noise) : Sobel, Prewitt

## Robert

| 1 | 0 |
| :--- | :--- |
| 0 | -1 |


| 0 | 1 |
| :--- | :--- |
| -1 | 0 |

Sobel

| -1 | -2 | -1 |
| :--- | :--- | :--- |
| 0 | 0 | 0 |
| 1 | 2 | 1 |


| -1 | 0 | 1 |
| :--- | :--- | :--- |
| -2 | 0 | 2 |
| -1 | 0 | 1 |

## Laplacian

has zero response to gradual change and respond to both sides of edge, once with positive and once with negative sign. An edge is at zero-crossing.
$\nabla^{2}=\frac{\partial^{2}}{\partial x^{2}}+\frac{\partial^{2}}{\partial y^{2}}$
approx by
$\mathrm{L}(\mathrm{x}, \mathrm{y})=\mathrm{f}(\mathrm{x}, \mathrm{y})-1 / 4\{\mathrm{f}(\mathrm{x}, \mathrm{y}+1)+\mathrm{f}(\mathrm{x}, \mathrm{y}-1)+\mathrm{f}(\mathrm{x}+1, \mathrm{y})+\mathrm{f}(\mathrm{x}-1, \mathrm{y})\}$

- Marr-Hildreth 1980
smooth the image (Gaussian) and isolate zero-crossing (Laplacian)
$\mathrm{I}(\mathrm{x}, \mathrm{y})$ image
$\mathrm{G}(\mathrm{x}, \mathrm{y})$ Gaussing
Laplacian of Gaussian
Let D2 be, $\nabla^{2} \quad$ Py2 be $\frac{\partial^{2}}{\partial y^{2}}$
$\mathrm{D} 2\{\mathrm{I}(\mathrm{x}, \mathrm{y}) * \mathrm{G}(\mathrm{x}, \mathrm{y})\}=\mathrm{D} 2 \mathrm{G}(\mathrm{x}, \mathrm{y}) * \mathrm{I}(\mathrm{x}, \mathrm{y})$
2-D convolution can be separable into four 1-D convolution
$\mathrm{D} 2\{\mathrm{I}(\mathrm{x}, \mathrm{y}) * \mathrm{G}(\mathrm{x}, \mathrm{y})\}=\mathrm{G}(\mathrm{x}) *\{\mathrm{I}(\mathrm{x}, \mathrm{y}) * \operatorname{Py} 2 \mathrm{G}(\mathrm{y})\}+\mathrm{G}(\mathrm{y}) *\{\mathrm{I}(\mathrm{x}, \mathrm{y}) * \operatorname{Py} 2 \mathrm{G}(\mathrm{x})\}$
- Template matching


## Region growing

- grouping areas with a common feature into region
- What is the criteria for merging two regions?
- At what point does merging cease?

Global thresholding, grey-level
Horowitz and Pavlidis 1976
Quad-tree
Boundary detection: Hough Transform
contour following

## Specific to Robocup

- Real-time constraint: Windowing, prediction
- Local threshold
- Colour segmentation
- Shape recognition

3-D machine vision
Visual servoing
Object recognition

## Conclusion

Have fun and learn along the way

## References

1. R. Jain, R. Kasturi, B. Schunck, Machine Vision, McGraw Hill, 1995. (the standard text book in machine vision)
2. S. Umbaugh, Computer Vision and Image Processing: A practical approach using CVIP tools, Prentice Hall, 1998. (the software is developed by Computer vision and image processing laboratory at Southern Illinois University at Edwardsville (SIUE))
3. M. Petrou, P. Bosdogianni, Image processing: the fundamentals, John Wiley \& Son, 1999. (mathematical foundation of image processing)
4. R. Gonzalez, R. Woods, Digital Image Processing, Addison Wesley, 1992. (the classic of digital image processing)
5. There are plenty of image processing code at www.intel.com
