

MULTI-EVIDENCE LEARNING FOR MEDICAL DIAGNOSIS

Miss Tongjai Yampaka

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สาขาวิชาวิศวกรรมคอมพิวเตอร์ ภาควิชาวิศวกรรมคอมพิวเตอร์
คณะวิศวกรรมศาสตร์ จุฬาลงกรณ์มหาวิทยาลัย
ปีการศึกษา 2563
ลิขสิทธิ์ของจุฬาลงกรณ์มหาวิทยาลัย



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ในช่วงไม่กี่ปีที่ผ่านมาได้มีการสร้างโมเดลการเรียนรู้จากชุดข้อมูลหลายแหล่งโดยพิจารณาจากความหลากหลายของชุดข้อมูลที่นำมาประกอบเป็นหลักฐาน งานวิจัยที่พยายามใช้ชุดข้อมูลที่หลากหลายเพื่อช่วยปรับปรุงให้โมเดลมีความแม่นยำมากขึ้น การวินิจฉัยทางการแพทย์ก็ใช้ชุดข้อมูลจากหลายหลักฐานมาช่วยในการสร้างโมเดลเพื่อช่วยในการวินิจฉัยโรค ตัวอย่างเช่นการตรวจคัดกรองมะเร็งเต้านม โดยปกติการแปลผลของนักรังสีวิทยาจะใช้ภาพถ่ายรังสีเต้านมสองมุมมอง (Cranio-Caudal และ Medio-Lateral-Oblique) หรือภาพถ่ายเต้านมด้วยคลื่นความถี่สูงสองโหมด (B-mode และ Doppler mode) ใช้ในการวินิจฉัยว่าผู้ป่วยมีโอกาสเป็นมะเร็งเต้านมหรือไม่ งานวิจัยนี้มุ่งเน้นการสร้างโมเดลการเรียนรู้จากหลายหลักฐานสำหรับวินิจฉัยทางการแพทย์โดยใช้การวินิจฉัยมะเร็งเต้านมเป็นกรณีศึกษา โดยใช้ภาพถ่ายรังสีเต้านม (Mammography image) และภาพถ่ายเต้านมด้วยคลื่นความถี่สูง (Ultrasonography image) วิธีที่เราเสนอประกอบด้วยสี่ขั้นตอนดังนี้ 1) สกัดคุณสมบัติจากภาพโดยใช้โครงข่ายประสาทเทียมแบบสังวัตนาการ (Convolutional Neural Networks) 2) เลือกคุณสมบัติที่เหมาะสมโดยพิจารณาจาก สารสนเทศร่วม (Mutual information) ที่ขึ้นต่อกันระหว่างคุณสมบัติกับคลาสเป้าหมาย 3) รวมชุดหลักฐานโดยใช้การวิเคราะห์สหสัมพันธ์คาโนนิคัล และ 4) สร้างโมเดลเพื่อจำแนกประเภทโดยใช้ซัพพอร์ตเวกเตอร์แมชชีน (Support Vector Machine) เป็นตัวจำแนกเชิงเส้น เป้าหมายเพื่อวินิจฉัยว่าเป็นก้อนเนื้อมะเร็งหรือไม่ใช่มะเร็ง ผลการทดลองระบุว่าการเรียนรู้หลายหลักฐานโดยใช้สารสนเทศร่วมกับการวิเคราะห์สหสัมพันธ์คาโนนิคัล มีแนวโน้มที่จะเพิ่มประสิทธิภาพการจำแนกประเภท นอกจากนี้ไม่เพียงแต่มีความแม่นยำสูงเท่านั้น แต่ข้อมูลหลักฐานที่นำมารวมกันยังมีความสัมพันธ์สูงสุดอีกด้วย

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In recent years, a great many approaches for learning from multiple sources by considering the diversity of different views have been proposed. The most interesting field is medical diagnosis. For example, breast cancer screening normally employs two views of mammography (Cranio-Caudal and Medio-Lateral-Oblique) or two modes of ultrasound (B-mode and Doppler mode) breast images. This study proposes a multi-evidence learning model that combines the multiple evidences of breast images to improve diagnosis. Two views mammography and two modes of ultrasound were used. Our proposed model consists of four stages. First, feature extraction using Convolutional Neuron Networks was operated to extract the image features on each view separately. Second, feature selection by exploring the mutual information between the feature and the class label was used to select the informative features. Third, canonical correlation analysis was explored to merge two feature sets into one final layer. Finally, the classification of malignant or benign was performed using a support vector machine. The experiment results indicated that the proposed method increases the classification performance. In addition, not only high accuracy but also the maximal correlation has been achieved with combined views.

Field of Study: Computer Engineering

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Chapter I

Introduction

1.1 General background

1.1.1 Multi-evidence data and multi-evidence learning

Computer and information technology in the last decade have rapidly developed almost every discipline in science and engineering. Data mining and machine learning methods conduct the related research to transform many fields from small data to increasingly big data. Meanwhile, data can be collected and extracted from multiple information sources to represent various models. In general, this approach is defined as multi-view data, in which each view represents the same object but may have different views. In the common machine learning setting, the data is obtained in a single vector space, however, multi-view data may be represented in several different vector spaces or even a mixture of vector spaces [1]. In the same instance with multi-evidence data, each view could represent the same or different objects. For example, in medical diagnosis, data can be represented in images or text. Therefore, multi-evidence learning has become a valuable step to help in decision making.

1.1.2 Benefits of multi-evidence learning

In the following, the three benefits from multi-evidence learning and the relevant examples are illustrated.

Benefit one: Consensus principle of two hypotheses, the connection between the consensus of two hypotheses gave the inequality and their error rates. The agreement on multiple evidence aims to maximize the agreement on multiple distinct evidence. Suppose two available data X^1 and X^2 The learning data were formed in $\{x_i^1, y_i\}$ and $\{x_i^2, y_i\}$ therefore two data set as $\{x_i^1, x_i^2, y_i\}$, where y_i is the label associated with the example. The inequality shown as:

$$P(f^1 \neq f^2) \geq \max\{P_{err}(f^1), P_{err}(f^2)\}$$

From the inequality, the probability of a disagreement of two independent hypotheses should be upper bounds the error rate of either hypothesis. Thus, the minimized of disagreement rate shows that the error rate of each hypothesis will be minimized [2]. In recent years, these consensus methods have developed to utilize this consensus principle, nevertheless, the contributors are not considering about relationship between the datasets. For example, Xia et al., (2010) [3] proposed the arbitrary point and its k nearest neighbors to force similar outputs in the low-dimensional embedding space. Following this local consensus optimization, all the patches from different views are unified by global coordinate alignment. This can be seen as a global consensus optimization.

Benefit two: The complementary principle in multi-evidence learning, when each data source may contain some knowledge that other sources do not have. Therefore, multiple pieces of evidence can be employed to complete and describe the data. In obviously, the complementary information can be improved the learning performance in machine learning problems. In recent years, the traditional solution for the multiple datasets problem is to concatenate vectors into a new single vector and then straightforwardly apply a single vector to learning algorithms. However, these concatenation causes are not considering the relationship between the two datasets. To avoid this problem, several methods have been designed by constructing a latent subspace shared by multiple datasets to integrate complementary information from different views. Thus, it is possible to find the corresponding latent space connected with the point on the others. For instance, the cartoon character retrieval from [4] was proposed in semi-supervised multi-view distance metric learning (SSM-DML). This approach showed that since various low-level features can be extracted to represent the image, each feature space will give one measurement of similarity of the data, so it is difficult to decide which measurement is the most suitable. The complementary information underlying a shared latent subspace can be taken of metric learning to precisely construct the dissimilarity between different examples.

Consequently, as addressing the problem of multiple dataset learning, both the consensus and complementary principles should be kept in mind to take full advantage of multiple evidence learning.

1.1.3 Challenges of multi-evidence learning

Traditionally, machine learning or data mining have been conducted from single data. Although the multiple dataset learning has become increasingly crucial when the need to extend the general theories to the full power of knowledge, as same as the multi-evidence learning is a very challenging task.

The 1st challenge: The consensus principle and complementary principle could be improved the diagnosis accuracy. For example, inefficient information from the grayscale image can complete by the multi-evidence learning mechanism of the visual perception system. Because of the color image of the real world can perceive by seamlessly integrating images about the surrounding scene from two perspectives. This example demonstrates learning from multi-view data is more complete than single-view data. As a result, the medical diagnosis from multiple evidence or medical images could be obtained by collecting the complementary information. Figure 1 illustrates a complementary from grayscale and color mode of breast ultrasound image.

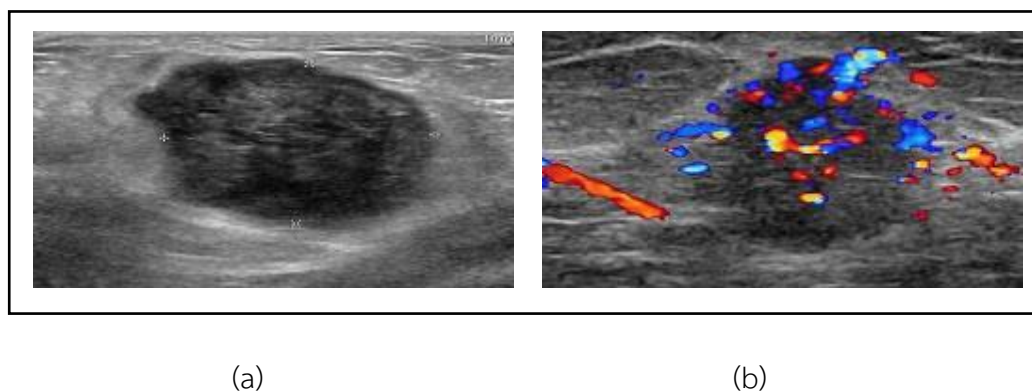


Figure 1 (a) B-mode and (b) color Doppler mode of breast ultrasound image

As shown in the above, breast ultrasound is examined by two modes including B-mode (grayscale) and color Doppler mode (color). B-mode displays the acoustic impedance of a two-dimensional cross-section of tissue, while color Doppler

mode displays blood flow, the motion of tissue over time, the location of blood, the presence of specific molecules, the stiffness of tissue, or the anatomy of a three-dimensional region. The complementary information from multiple data, especially when the weaknesses of one data are complemented by the strengths of others, the complete pattern could be obtained.

Other example, learning from multiple data can reduce the noise or can avoid the missing information. Figure 2 illustrates a missing example in breast mammogram image.

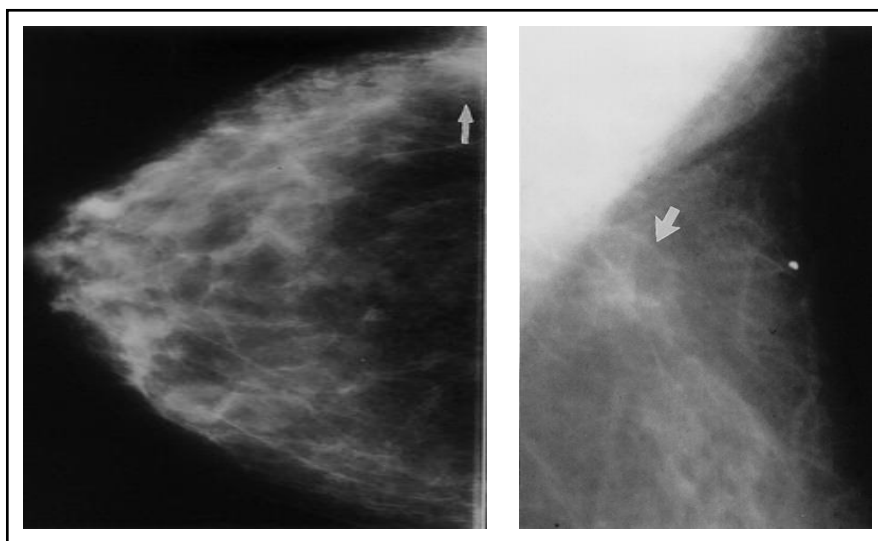


Figure 2 missing example in breast mammogram image

As shown in the above, breast mammography is examined by two views including a side view (MLO) and top view (CC) of the breast. The missing lesion is appearing in the CC view, but it can be seen in the MLO view. Therefore, the missing information can be avoided when using multiple datasets.

For the convenience of joint analysis, modeling multi-evidence is required. The challenge is “How to model multiple data in a proper way is a basic issue in multi-evidence learning?”

The 2nd challenge, the relationships among datasets are important in many applications. Then such a strategy can potentially identify the relationships between multiple datasets and evaluate their learning capabilities. The particularly useful in this problem when collecting the correlated data but collecting the

correlated data from multiple sources may be resource-demanding and thus expensive. Sometimes, the dataset from multiple sources is uncorrelated but it useful for complementary information. Therefore, how to create their relationship to facilitate multi-evidence learning is still a challenging problem.

The 3rd challenge, dimension reduction of a huge dataset is considered. In practical applications, both the number of objects and the number of features is growing at a rapid rate. The dimension reduction methods seem an essential step for further analysis. Then, how to implement the dimension reduction becomes a challenging issue.

In this Thesis, the above challenge will be performed respectively. Meanwhile, we focus on complementary information based on the subspace learning method to apply with multi-evidence learning in medical diagnosis.

1.2 Combination of multi-evidence data

1.2.1 Subspace Learning

Subspace learning of multiple dataset learning aims to obtain a latent subspace which generated and shared by multiple evidence data. This latent subspace dimension is lower than any input data to reduce the large dimension for convenient classification or clustering tasks. In reviewing the literature on multiple dataset learning, we find that it is tightly connected with other topics in machine learning. For example, the multi-view metric learning proposed by Quadrianto and Lampert (2011) [5] and Zhai et al. (2012) [6] constructs the embedding projections from multiple datasets to shared subspace. Chen et al. (2010) [7] applied Markov network to construct the connections between the two datasets through latent subspaces. Salzmann et al. (2010)[8] and Jia et al. (2010) [9] found a latent subspace in the information by correctly factorized into shared and private parts across different datasets. Domain adaptation problem which the source domain and the target domain seen as different views can be solved by cross-language text classification [10, 11]. In addition, multi-view majority voting and multi-view co-classification [12] have been designed and successfully applied latent subspace for this problem.

Correlation between views is an important consideration in subspace-based approaches for multiple dataset learning. Traditionally, subspace learning using canonical correlation analysis (CCA) has been widely applied in multiple dataset learning. Hotelling (1936) [13] introduced canonical correlation analysis (CCA) to explore the linear relation between two variable sets by mutually maximizing the correlations. Several measures of association in the literature are constructed as functions of the correlation coefficients. The maximal correlation was widely selected for the next tasks.

1.2.2 Extended subspace learning

Supervised-CCA: In many studies, the original CCA is extended in many algorithms. The most extended is supervised CCA, in which one view is derived from the data and another view is derived from the class labels. Sharma et al. (2012)[14] proposed a Generalized Multi-view Analysis (GMA) which exploits supervised and unsupervised feature extraction techniques. This algorithm can potentially replace CCA whenever classification or retrieval label information. Zhai et al. (2012) [15] proposed a new semi-supervised method called Multi-view Metric Learning with Global consistency and Local smoothness (MVML-GL). This method established the relationship between data and pairs of labeled instances and shared latent space for unlabeled and test data. LEE et al. (2015) [16] presented a new method called supervised Multi-view Canonical Correlation Analysis (sMVCCA). sMVCCA utilizes a closed-form solution for determining the optimal separable and low dimensional representation via simultaneous correlation between all pairs of modalities and between each modality with the label information. This study demonstrated that the ability of sMVCCA to perform statistically significantly better in classification AUC compared to other data fusion methodologies.

MI-CCA: In reviewing the literature on extended CCA demonstrate that the supervised CCA is useful for multiple datasets learning not only reducing the data dimension but also improving the performance. However, the class labels may have appeared only on one dataset. Therefore, the CCA including the mutual information is introduced in a supervised CCA approach when the class labels have



appeared both datasets. Liu and Yuen (2011) [17] introduced two new confidence measures, namely, inter-view confidence and intra-view confidence using mutual information between the latent distribution and the class labels. Inspired by their success, this study proposes the mutual information including canonical correlation analysis (MI-CCA) which handles the multiple evidence of the medical diagnosis. This is distinct from previous work. First, the dataset has own class labels. Second, the mutual information is separately measured to explore the appropriate feature sets followed by CCA tasks.

1.2.3 Overview of multi-evidence learning strategies

Overview: The contribution of this study aims to fuse multiple evidence image for breast cancer diagnosis including (a) feature extraction from breast image including breast ultrasound and mammography using CNN, (b) extension of CCA via Mutual Information MI-CCA for data fusion, and (c) building a classifier model to distinguish breast tumor from benign and malignant.

Feature extraction using Convolution Neuron Network (CNN) : The features were automatically extracted by using Convolutional Neural Networks (CNN) which is powerful models that achieve impressive results for image classification to avoid the cost hand-crafted feature extraction [18]. The success from many studies [19-22] was applied to large-scale image and video recognition. Inspired by their success, this approach was used to extract the features from breast images. Bengio and LeCun suggested that complicated functions could be represented by high-level abstractions when used deep architectures, but the effective depth layers also affect to the learning time.

Extended CCA using mutual information (MI-CCA): CCA performs to maximize cross-correlation between datasets. Nevertheless, these representations do not consider the class labels of individual data. Therefore, supervised dimension reduction methods supervised-PCA and supervised-CCA are introduced [16, 23]. These studies reported that the supervised method is able to fuse data from any number of modalities to a joint subspace that can improve the model performance.



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1.3 Contributions of this dissertation

1.3.1 Breast ultrasound image

Ultrasound (US) has been used in screening as a supplementary tool especially in women with dense breast tissue [24]. The most abnormal breast lesions are easy to find by using the conventional ultrasound, while some lesions are still hidden. Therefore, multiple ultrasound modes have been performed to extract different information from breast lesions. For example, B-mode (Brightness) displays the acoustic impedance of a two-dimensional cross-section of tissue, while color Doppler mode displays blood flow, the motion of tissue over time, the location of blood, the presence of specific molecules, the stiffness of tissue, or the anatomy of a three-dimensional region.

In previous studies, a single ultrasound mode has been individually improved. For instance, non-mass lesions were defined in four types[25]. It could be improved positive predictive values but the differentiation of NMLs by B-mode remained ambiguous and need further exploration. After intensive researches, elastography mode was well-established in cases of breast masses[26, 27]. Guo et al. [28] used of contrast agents CEUS to depict the microcirculation of breast masses and provide qualitative and quantitative analysis for classifying breast lesions. These studies showed that elastography mode could be helpful, but they note that it remained imprecise in interpretation. Color Doppler mode, which used to supplement in the conventional ultrasound, showed high sensitivity, low angle dependency, and no aliasing [29]. Nevertheless, the compilation with recent clinical research [30] reported that the Doppler image alone was not significantly distinguished from a solid mass.

Although previous studies demonstrated that single ultrasound mode could improve the overall accuracy, these investigations have some limitation. Consequently, multiple ultrasound modes have been widely combined with improving diagnosis performance. When B-mode was always examined together with color Doppler mode, the fusion of B-mode and color Doppler mode was performed [31, 32]. These studies reported that combining the B-mode and color Doppler mode showed high accuracy and specificity. Laurence R. et al. [31] evaluated the



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performance fusion of B-mode, color Doppler, and SWE measurements. The result could significantly ($p < 0.001$) improved characterization of testicular masses and, therefore, could avoid inappropriate total orchiectomy.

Although previous studies demonstrated that the combination of ultrasound modes could improve the overall accuracy, these investigations were interpreted by the radiologist. According to Jeongmin Lee et al, [32] investigated the effect of automatic breast lesion detection. When inexperienced radiologists described and categorized breast lesions, especially in comparison with experienced radiologists, the automatic breast lesion detection can be more beneficial and educational for less experienced radiologists than for experienced radiologists not only describing lesions but also determining if the lesion is malignant.

Therefore, this study aims to combine the B-mode and color Doppler mode for modeling the breast cancer classification with improving diagnosis performance.

Data Acquisition and Data Description: The experiment dataset has been provided by the Department of Radiology of Thammasat University and Queen Sirikit Center of Breast Cancer of Thailand. These lesion images consisted of 53 benign lesions and 202 malignant lesions (including 255 B-mode images and 255 color Doppler mode images). The patients' information has been removed from the images. All lesions were confirmed by biopsy; thus, it is absolutely clear whether the lesion was malignant or benign. In addition, the lesion was classified by three leading experts as malignant or benign. The consensus decision has been obtained by the majority voting rule (two out of three). The image was obtained by a Philips iU22 ultrasound machine in resolution ranges from 200x200 to 300 x400 pixels based on the criteria of the provider. Figure 1.1 shows the different characteristics between B-mode and color Doppler mode.

1.3.2 Breast mammography image

Mammography has been widely used for early screening that comprises of Medio Lateral oblique view (MLO) and Cranio Caudal view (CC). Two views are always examined and classified in benign or malignant lesions by the radiologist. Well-trained radiologists have been found that some common pitfalls appeared in CC

view, whereas some pitfalls appeared in MLO view [33]. Single view and two-view mammographic examinations interpreted by experienced radiologists were compared in many studies [34-36]. These studies reported that two-view screening could improve the cancer detection rate. Then, they suggested that other methods may be reduced missing such as explored correlation of image or integrated of double reading. The study in breast positioning explained that CC-view and MLO-view are different point of each view.

According to previous reports, multi-views in mammography tend to avoid missed interpretation. Vijayarajan and Jaganathan (2014) [37] proposed transform 2D to 3D feature of MLO and CC view, then, the features were combined 3D boundary features of two views. Several recent studies[38, 39] worked with feature extraction using Convolutional Neuron Networks (CNNs) to share relevant features between MLO and CC view and improve model performance.

Data Acquisition and Data Description: Breast mammographic digitized images published from the Digital Database for Screening Mammography (DDSM) has been widely used as a benchmark for numerous studies on the mammographic area. These datasets consist of 600 CC-view and 600 MLO-view and compose of 200 normal, 200 benign, and 200 malignant for each view. Each image has a resolution of 256x514 pixels gray level tones.

1.3.3 The contributions of dissertation

1.3.3.1 When The consensus principle and complementary principle could be improved the diagnosis accuracy, this study proposes the data fusion approach to employ comprehensively and accurately describe the data by using the data that may contain some knowledge that other evidence does not have.

1.3.3.2 Also, we propose the supervised feature selection explored the mutual information between related feature and class label. The output features of the last convolutional layer were reduced before the fusion process.

1.3.3.3 Information fusion using canonical correlation analysis is performed to combine multi-evidence features (multiple ultrasound modes or multiple mammography views). Each feature provides an independent, but it could be



complemented observation of the instances and thus we implement CCA on their combination to seek a joint mapping, which is useful for detecting breast lesions and distinguishing breast cancer.

Chapter II

Primarily theories

2.1 Primarily theories

2.1.1 Feature Extraction

This section is dedicated to the description of NN in general and its special type called CNN that use for feature extraction.

2.1.1.1 Neural Networks

NNs is the invention of Perceptron inspired by Biology of central nervous systems of mammals. Perceptron used the biological neuron that also described an algorithm for direct learning from data. It resembles the brain in two respects. First, the knowledge is acquired by the network from its environment through a learning process. Second, the strength connection of neuron, known as synaptic weights, are used to store the acquired knowledge. When NNs are used for classification problems, it interprets the outputs as probabilities of the inputs belonging to each class. For example, the inputs (x_1, x_2) are the coordinates, and the output (y_0, y_1) is constant, which sums to 1. The decision boundary is chosen. This means that when $y_0 > y_1$ the algorithm will classify the data point as 0 and vice versa. The schematic representation can be seen in figure 3.

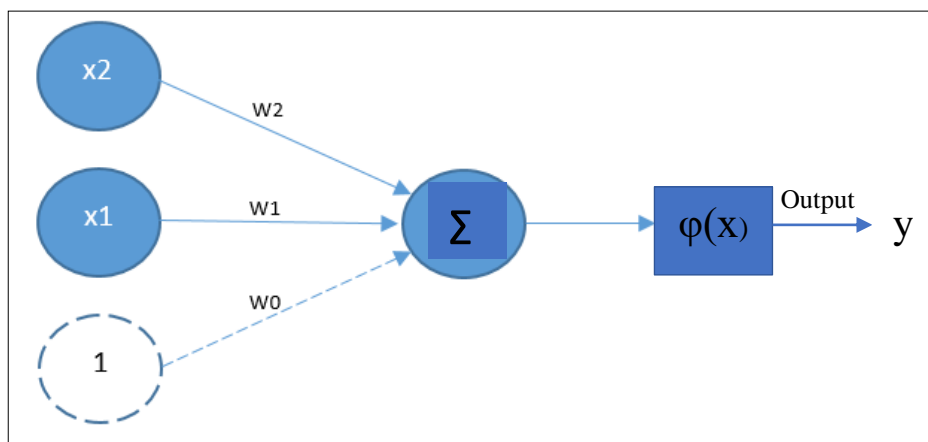


Figure 3 Schematic representation of a simple perceptron.

Input variables x_i , corresponding weights w_i , the weighted sum of the inputs, an activation function φ , the output y and the bias b . Bias is an additional input to each neuron often represented as an input $x = 1$ and a weight w_0 ($w_0 = b$). The output y from the single perceptron is:

$$y = \varphi \left(\sum_{k=1}^m w_k x_k + b \right)$$

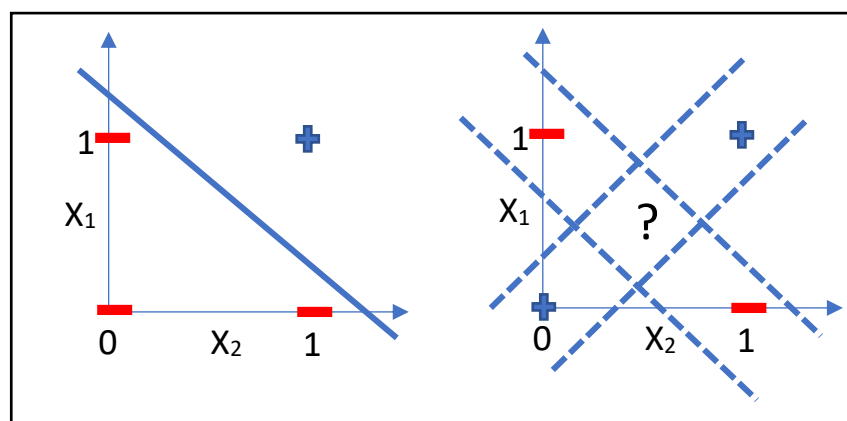
Including the bias in the summation we get:

$$y = \varphi \left(\sum_{k=0}^m w_k x_k \right)$$

φ is called an activation function. A sigmoid function is often used for regular NNs, as the logistic function or $\tan(x)$. When working with CNNs, the Rectified Linear Unit (ReLU) is mostly used to extract the features. It is defined as:

$$\varphi(x) = \begin{cases} 0 & \text{if } x \leq 0, \\ x & \text{if } x > 0. \end{cases}$$

The decision boundary is a hyperplane that is linearly (cf. linear SVM). With a single perceptron, it may solve the AND and OR problem.



(a) (b)
Figure 4 (a) AND problem (b) XOR problem

Figure 4 shows a simple perceptron that is very promising to separate linearly problems. However, among other studies contained mathematical proof that perceptron is unable to solve simple XOR problem [40]. Therefore, NNs was shown that any complex problems could have been solved by usage of multiple perceptron units. The invention of the back-propagation learning algorithm was introduced to gather neurons into groups called layers which can be stacked into hierarchical structures to form a network called Multilayer Perceptron (MLP).

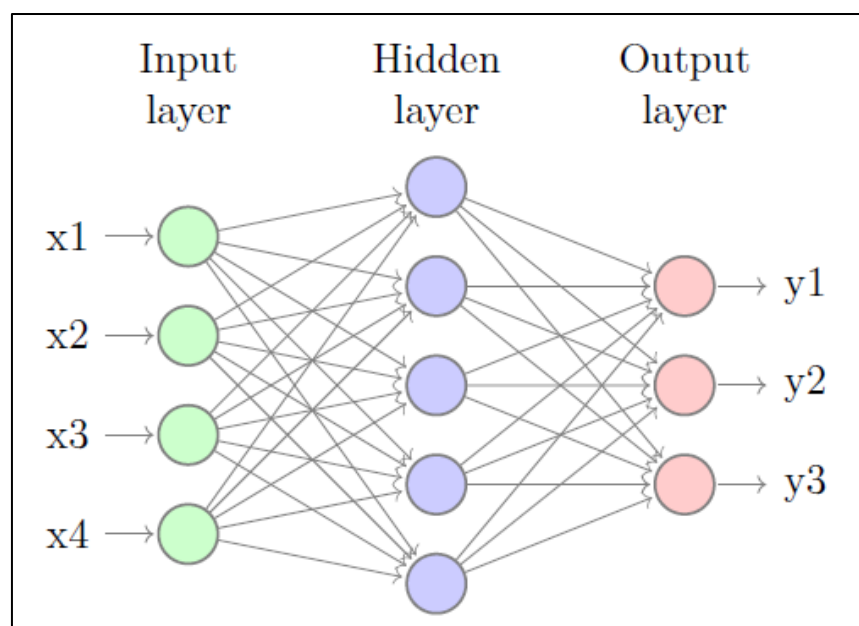


Figure 5 Schematic representation of a Multilayer Perceptron.

Figure 5 has classified the output y_i for the input x_i . The function for calculating these outputs is:

$$y_i = \varphi_0 \left(\sum_{i=0}^5 w_{ij} \varphi_n \left(\sum_{k=0}^4 \tilde{w}_{jk} x_k \right) \right)$$

In the final classification, softmax function is commonly used to get y_i from the probability that belongs to class i . Deep Neural Networks or deep learning are also performed to increase the depth of the network. When adding hidden layers, the decision boundary is not limited to a hyperplane.

2.1.1.2 Convolutional Neural Networks

Convolutional Neural Network (CNN) is a neural network that composes of deep neural layers. Due to further application in image analysis, the use of CNNs is widely used as medical images.

Structure: Convolutional Neural Network consists of the hidden layers that have different configurations. A filter of spatial neurons takes input images and presents the probability of each class as output. A schematic representation of a Convolutional Neural Network can be seen in figure 6, and below explain the different layers.

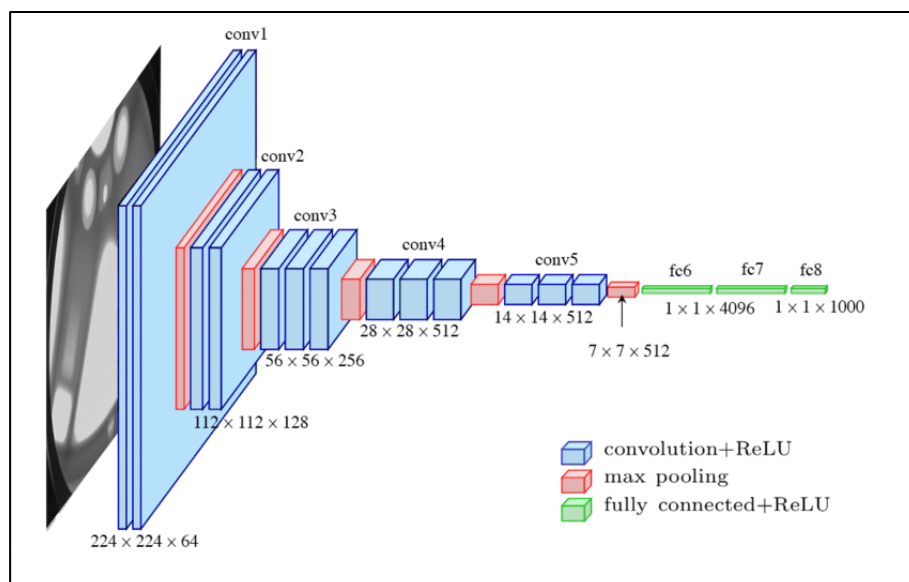


Figure 6 Schematic representation of a Convolutional Neural Network.

Convolutional layer: Convolution is a major part of the function of these networks, a function x with a kernel w in two dimensions is defined as:

$$S(i, j) = \sum_m \sum_n I(m, n) F(i - m, j - n),$$

The filter (F) up-down and left-right and sum over all products.



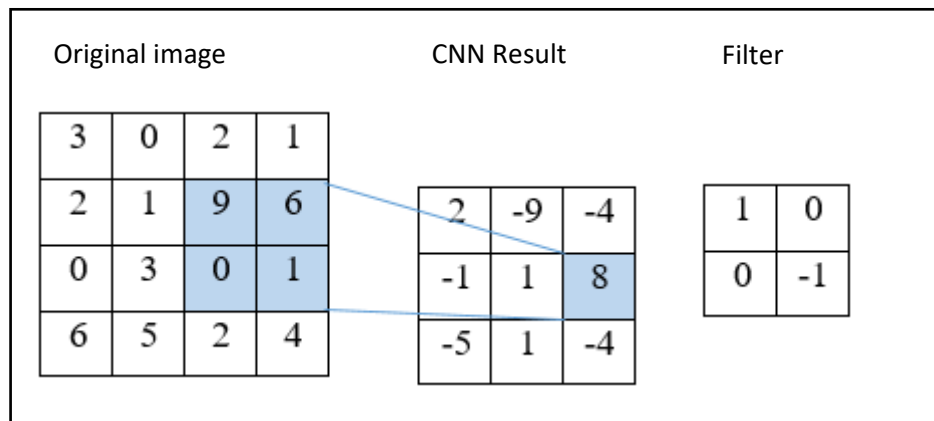


Figure 7 An example showing how convolution of an image works.

An example can be seen in the top picture in figure 7. The marked pixels will calculate of the convolution at this point:

$$\text{Input pixel} = \begin{bmatrix} 9 & 6 \\ 0 & 1 \end{bmatrix}, \text{Filter} = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$$

The results is:

$$(1)(9) + (0)(6) + (0)(0) + (1)(-1) = 8$$

Pooling layer: Pooling layers cause a down-sampling of the filter outputs. Max-pooling, which the largest value within this filter is saved to the next layer, is mostly used in CNN network. Thus, the largest information of image will save and move to do the next calculation.

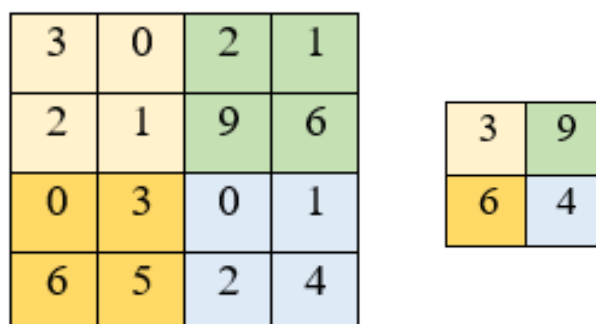


Figure 8 the principle of max-pooling.

Fully-connected Layer: Neurons in a fully connected layer have full connections to all activations in the previous layer. A matrix multiplication followed by a bias offset is computed with their activation.

The most common architecture stacks compose of a few CONV-RELU layers, follow them with POOL layers, and repeat this pattern until the image has been merged spatially to a small size. The class scores are calculated from the last fully-connected layer. Furthermore, other layer such as Normalization layer or Dropout layer have been introduced to improve the model performance.

2.1.2 Feature Selection

Feature Selection is the process of selecting what inputs should be presented to a classification algorithm. Generally, the feature selection was performed by domain experts, while modern classification approaches attempt to collect all possible features and then use a statistical feature selection process to determine which features are relevant for the classification problem. The feature set contains irrelevant (weak information about the classification problem) and/or redundant (already present in more informative features). Both irrelevant and redundant are increase the collection cost of the feature set. In addition, shrinking the feature set also improve classification performance. These heuristic notions of relevancy and redundancy were formalized by Kohavi & John [41] into three classes: strongly relevant, weakly relevant, and irrelevant. The strongly relevant features contain useful information, while the weakly relevant features contain weak information, then, the irrelevant features contain no useful information about the problem. Therefore, the ideal feature selection algorithm would return the set of strongly relevant features excluding the irrelevant features. In chapter 2.1.1, the feature extraction was performed and returned the set of strongly relevant features, subset of the weakly relevant features, and including the irrelevant features.



Feature selection algorithms are three main kinds: filters, wrappers, and embedded methods. This chapter will focus on filters algorithms. Filters algorithm is the evaluation function or criterion which scores the utility of a feature or a feature set, and the search algorithm which generates new candidate features or feature sets for evaluation.

2.1.2.1 Filters algorithm

Filter approaches use a measure of relevancy or separation between the candidate feature or feature set and the class label by scoring a feature or feature set. These measures range from simple correlation measures such as Pearson's Correlation Coefficient [42], through complex correlation measures such as the mutual information (discussed in Section 2.1.3). All these measures achieve to return the strong relationship between the candidate feature set and the class label. This relationship might be a measure of probabilistic independence. This thesis calls mutual information scoring (MI score) based on information theoretic measures. The scoring criteria is along with a search method to select candidate feature sets [43]. The complexity of the scoring usually enforces the complexity of the search method. Many common filters use greedy forward or backward searches [44, 45] to adding or removing each feature based on high score or low score. Branch & Bound methods [46] was improved in optimal search strategies and exclude groups of features from consideration if they can never improve in performance. However, such complex search algorithms are unnecessary in certain situations, notably in the case of univariate feature selection where the best features based on univariate statistical tests can be investigated discrete target variable.

Due to the use of abstract measures of correlation between variables and target classes, they return useful feature set which should perform well with classification algorithms.

2.1.3 Mutual Information

2.1.3.1 Information Theory

The relationship between two variables can measure the amount of shared information between two variables. Information Theory has been performed to measure the amount of shared information. The uncertainty quantity of information can be reduced in one variable when another variable is known. Claude Shannon defines three crucial measures which form the basis of much of the rest of the work we present in this thesis [47].

They are the Entropy, $H(X)$, for a random variable X , the Conditional Entropy of X given another random variable Y , $H(X;Y)$, and the Mutual Information between two variables, $I(X; Y)$.

The Entropy of a random variable X , measures the uncertainty about the state of a sample x from X . The entropy of X is defined in terms of the probability distribution $p(x)$ over the states of X as follows:

$$H(X) = - \sum_{x \in X} p(x) \log p(x)$$

The logarithm base defines the units of entropy, with \log_2 using bits. High values of entropy mean the state of x is very uncertain (and thus highly random), and low values mean the state of x is more certain (and thus less random), then, the uncertain state of x is the hardest to predict. The entropy of X given Y measures the uncertainty of the state of a sample of x when Y is known. This has two equivalent definitions, in terms of the joint probability distribution $p(x; y)$,

$$\begin{aligned} H(X; Y) &= \sum_{y \in Y} p(y) H(x; Y = y) \\ &= - \sum_{y \in Y} \sum_{x \in X} p(x, y) \log p(x, y) \end{aligned}$$

The conditional entropy investigates the interaction between two variables. When knowing the entropy of X , it can derive any useful information. This conditional entropy is called the Mutual Information, $I(X; Y)$. It measures the



reduction in uncertainty in the state of X when the state of Y is known and increase in the relevant information. This leads to several equivalent definitions for the mutual information,

$$\begin{aligned} I(X; Y) &= H(X) - H(X; Y) \\ &= H(Y) - H(Y; X) \\ &= H(X) + H(Y) - H(XY) \end{aligned}$$

The mutual information can also be expressed as the relative entropy between the joint distribution $p(x; y)$ and the product of both marginal distributions $p(x)p(y)$, defined as follows:

$$I(X; Y) = \sum_{y \in Y} \sum_{x \in X} p(x, y) \log \left(\frac{p(x, y)}{p(x)p(y)} \right)$$

With this formulation can investigate the mutual information reaches its maximal and minimal values. The maximal value is the minimum of the two entropies $H(X)$ and $H(Y)$, and occurs when knowledge of one variable allows perfect prediction of the state of the other. The minimal value is 0, which occurs when X and Y are independent. When knowing of one variable (and the condition of variable), It allows the perfect prediction. This study will use of the conditional mutual information in feature selection task.

2.1.3.2 Estimating the mutual information

Mutual information calculation can estimate using entropy estimation and estimate probability distributions. Paninski [48] shows the detail of this topic. This section provides a brief summary of the relevant issues and notations. The mutual information as the expected logarithm of a ratio of probabilities:

$$I(X; Y) = E_{xy} \left\{ \log \frac{p(x, y)}{p(x)p(y)} \right\}$$

Then \hat{p} denote a probability distribution which has been estimated from a dataset sampled from the true distribution p . The sample estimate using \hat{p} converges to the expected value N observations (x_i, y_i) :

$$I(X; Y) \approx \hat{I}(X; Y) = \frac{1}{N} \sum_{i=1}^N \log \frac{\hat{p}(x, y)}{\hat{p}(x)\hat{p}(y)}$$

The estimated distributions $\hat{p}(x, y)$, $\hat{p}(x)$, and $\hat{p}(y)$ were estimated. The maximum likelihood estimate of the probability of an event $p(X = x)$ is given by the frequency of occurrence of the event $X = x$ divided by the total number of events. The estimators estimate the probability distributions \hat{p} , and direct entropy estimators calculate the entropy from data without constructing probability distributions. For more information on alternative entropy estimation procedures, we refer the reader to Paninski [48, 49]. For the remainder of this thesis, we use notation $MI(X; Y)$ to compute the mutual information.

2.1.3 Subspace Learning-based Approaches

Subspace learning-based approaches aim to obtain a latent subspace shared by multiple views by assuming that the input views are generated from this subspace. Besides the well-known canonical correlation analysis (CCA), other more effective methods to construct the subspaces have recently become available.

2.1.3.1 Singular Value Decomposition

The relevant to our work is based on the Truncated Singular Value Decomposition [50] (TSVD). It is related to Principal Component Analysis [51] (PCA) that is established approach to dimensionality reduction. Given a sample dataset with l samples and n dimensions is a set:

$$S_1 = \{x_1^1, x_2^1, \dots, x_n^1\}, S_2 = \{x_1^2, x_2^2, \dots, x_n^2\}, S_l = \{x_1^l, x_2^l, \dots, x_n^l\}$$

where $x_i \in R^n$ are generated independently and identically distributed (i.i.d.) according to an underlying distribution. Given an $n \times l$ sample matrix, the goal is to find a best approximation with rank at most k under additional constraints:

$$\min_{U \in R^{n \times k}, S \in R^{k \times k}, V \in R^{l \times k}} \|X - U \cdot S \cdot V^T\|_F$$

Subject to

$$U^T U = I_k$$

$$V^T V = I_k$$

$$S = \text{diag}(\sigma), \sigma \in R^k, \sigma_i \geq 0$$

The PCA is based on a low rank decomposition of the empirical covariance matrix and computed based on the sample matrix. The main idea is to find a subspace that accounts for as much as variability in the data as possible. The first principal component is defined as the one-dimensional subspace that maximizes the variance of the data when projected onto it. Formally, it solves the following problem:

$$\max_{u \in R^n} \text{Var}(u^T \cdot X),$$

Subject to

$$\|u\| = 1$$

The other principal vectors can be solved the eigenvalue problem:

$$\min_{U \in R^{n \times k}} \|Cov(X) - U \cdot \Lambda \cdot V^T\|_F$$

One of the main applications of PCA is as a dimensionality reduction technique. The data is projected to the space spanned by the normalized eigenvectors (also called principal vectors). In general applications, an eigenvalue decomposition is used and discarded the principal vectors with small eigenvalues (similar to SVDs).

2.1.3.2 Canonical Correlation Analysis

Canonical Correlation Analysis (CCA) [52] is a general procedure for finding the relationships between two sets of random variables based on analyzing the cross-covariance matrix. CCA aims to identify linear relationships between two random vectors. Given two random vectors X^1 and X^2 are in pair of function $f^{(1)}$ and $f^{(2)}$ such that there is linear dependence between $f^{(1)}(X^1)$ and $f^{(2)}(X^2)$, that is, $f^{(1)}(X^1)$ should share some information for $f^{(2)}(X^2)$. This enables applications such as cross-modal information retrieval, classification, clustering, etc.

For example, if $f^{(1)}$ encodes a visual image and $f^{(2)}$ encodes a textual description of the scene, text input based on search over a collection of images was performed using cross-modal shared information [53]. Bi-lingual document analysis is another application, see[54, 55].

The idea is to find two vectors $w_1 \in R^p$ and $w_2 \in R^q$ so that the random variables $w_1^T \cdot X^1$ and $w_2^T \cdot X^2$ are maximally correlated (w_1^T and w_2^T map the random vectors to random variables, by computing weighted sums of vector components). By using the sample matrix notation X^1 and X^2 this problem can be formulated as the following optimization problem:

$$\rho = \underset{w_1 \in R^p, w_2 \in R^q}{\text{maximize}} \frac{w_1^T \text{Cov}(X^1, X^2) w_2}{\sqrt{(w_1^T \text{Cov}(X^1) w_1)(w_2^T \text{Cov}(X^2) w_2)}}$$

where $\text{Cov}(X^1)$ and $\text{Cov}(X^2)$ are estimated of variances of X^1 and X^2 , and $\text{Cov}(X^1, X^2)$ is covariance between X^1 and X^2 . The optimization problem can be solved to a generalized eigenvalue problem [55]:

$$\begin{bmatrix} 0 & \text{Cov}(X^1, X^2) \\ \text{Cov}(X^2, X^1) & 0 \end{bmatrix} \cdot \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} = \lambda \cdot \begin{bmatrix} \text{Cov}(X^1, X^1) & 0 \\ 0 & \text{Cov}(X^2, X^2) \end{bmatrix} \cdot \begin{bmatrix} w_1 \\ w_2 \end{bmatrix}$$

Or

$$[C_{22}^{-1} C_{21} C_{11}^{-1} C_{12} - \lambda I] w_i = 0$$

where C_{11} , C_{22} , and C_{12} are covariance matrix of the features X^1 and X^1 , X^2 and X^2 , then X^1 and X^2 , and I is the identity matrix.

A single canonical variable is usually inadequate in representing the original random vector and typically one looks for k projection pairs $(w_1^1, w_1^2), \dots, (w_k^1, w_k^2)$, so that w_i^1 and w_i^2 are highly correlated. This problem can be formulated as a symmetric eigenvalue problem.

Chapter III

Methodology

3.1 Overview proposed methodology

The contribution of this study aims to fuse multiple evidence for breast cancer diagnosis. The proposed method is including (a) feature extraction from breast images using CNN, (b) feature selection using mutual information that is extension of CCA (c) CCA for data fusion, and (d) building a classifier model to distinguish breast tumor from benign and malignant. Figure 9 shows the overview of method.

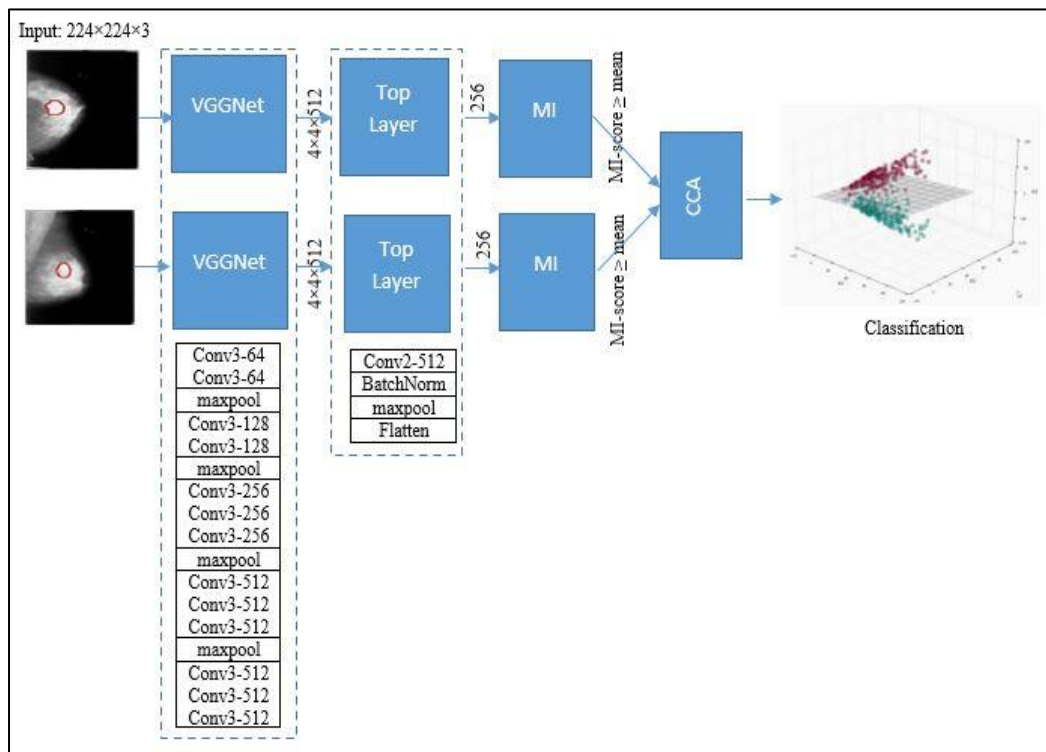


Figure 9 MI-CCA architecture model

The runner-up in ILSVRC 2014 [56] showed the depth of the network that was a critical component for good performance. However, training a deep CNN often requires computational resources. To address these challenges, transfer learning [57] is introduced to pre-trained followed by a specific task. The architecture of VGGNet was used to extract the features for breast ultrasound and mammography images followed by top-layer. There are three steps for extracting the image feature. First,

the input of each modes is fed to VGGNet backbone without fully training. Second, the output features from VGGNet layer are trained using CNN top-layer. Finally, the backpropagation process is performed only with CNN top-layer. Proposed model architecture consists of two parts that show in Figure 13.

3.2 Feature extraction

3.2.1 Software Tools

There are many software tools for machine learning. Almost every commonly used programming language has either some software library or at least some available Application Programming Interface (API). Keras written in python and high-level neural network API was used for this study. It is very simple with rapid model development and good documentation containing many code examples to get started very quickly.

3.2.2 Hardware and Software Configuration

Training of CNN demands a lot of resources and converts into many multiplications of matrices. Central Processing Units (CPUs) are not sufficient for computations. On the other hand, modern GPUs are designed to perform these operations. An efficient GPU in Keras is relying on either Theano or Tensorflow backend.

3.2.3 Dataset Preparation

The CNN model imposed the constraint that each image has to be of the same size and aspect ratio. Then, dataset preparation was done in three stages.

Image generator using keras library: The field of machine learning encounters a situation where the model tries to load a dataset but there is not enough memory. This is already one of the challenges in the field of vision where large datasets of images and video files are processed. To address this problem, keras supports data generators for loading and processing images. The ImageDataGenerator class is an easy way to load and augment images in batches for image classification tasks.

Split data into training and testing dataset: Images are randomly split between train and test dataset. It is very important that both datasets should be having an equal split among the categories because the imbalance category would be biased to the major category. This was caused by the fact that medical image was hard to collect equally classes. It was solved by kernel-based methods during random selection.

3.2.4 Model building blocks

For the implementation of CNN using Keras, the sequential model is appropriate for modeling of the feed-forward network. Definition of the network is composed of multiple Keras layers. All models were created by composition of following layers.

Convolutional: Convolutional layer used in the architecture was of following structure

```
Conv2D(filters=n, kernel_size=(z, z), strides=(s, s),
padding='valid', input_shape=shape)
```

where n is number of filters that the layer will have, Z is size of kernel, S is number of pixels in stride and $input_shape$ defines size of input matrix.

Activation: The activation function was added to the output of the layer.

```
Activation(activation_function)
```

where $activation_function$ is either “softmax” or “relu”. Both specifications are equivalent because Keras automatically uses linear activation function for each layer.

Pooling: Pooling layer can be specified as

```
MaxPooling2D(pool_size=(z, z), strides=(s, s))
```

where $pool_size$ specifies size of pooling kernel and $strides$ specifies number of pixels in x and y direction that are traversed in between application of individual pools.



Flatten: Feature extraction layers are multidimensional. Specifically, both Convolutional and Pooling layers are two dimensional. Classification layers that are created by fully connected layers are one dimensional. Then, flatten is necessary to create mapping between them.

```
Flatten()
```

3.2.5 Model Compilation and fitting

Model Compilation: Before trained the model, it needs to have cost function, optimization procedure and metrics defined. This is done by compiling the model.

```
model.compile(
    loss= 'categorical_crossentropy',
    optimizer=Adam(lr=0.001) ,
    metrics=['accuracy'])
```

parameter *loss* specifies cost function, optimizer optimization procedure and metrics specifies metrics by which the model is measured.

Model fit: Process of model training is in Keras called model fitting.

```
model.fit([train_data1, train_data2], train_labels,
         batch_size=batch_size, epochs=epoch_num,
         shuffle=True, verbose=0,
         validation_data=([valid_data1, valid_data2],
         valid_labels))
```

3.3 Feature selection using mutual information

The MI between random variables X and Y can be estimated the under-probability distribution form posterior knowledge of the pointwise mutual information $I(X; Y)$. If X given Y are the evens, then the true frequencies of all combinations of $(X; Y)$ pairs can estimate by counting the number of times each pair occurs in the data.

The mutual information scores were computed using the equation, shown as:

$$I(X; Y) = \sum_{y \in Y} \sum_{x \in X} p(x, y) \log \left(\frac{p(x, y)}{p(x)p(y)} \right) \quad (1)$$

where $p(x, y)$ is the joint probability density function of X and Y , and $p(x)p(y)$ are the marginal probability density functions of X and Y respectively. If X and Y are independent, then knowing X does not give any information about Y , their mutual information is zero. Followed by this concept the parametric distributions over feature and target class, it is convenient to revise from the equation (1), shown as:

$$I(f(\cdot); Y) = \sum_{f(\cdot) \in X} \sum_{y \in Y} p(f(\cdot); Y) \log \left(\frac{p(f(\cdot); Y)}{p(f(\cdot))p(Y)} \right) \quad (2)$$

where the set of $f(\cdot)$ is final output from CNNs networks, and Y is the possible target class. The mutual information scores:

$$I_1(f(x_1); Y), I_2(f(x_2); Y), \dots, I_i(f(x_i); Y)$$

An information theoretic filter algorithm is one that uses a measure drawn from Information Theory (such as the mutual information we described in Chapter 2) as the evaluation criterion. Evaluation criteria are designed to measure how useful a feature or feature subset is when used to construct a classifier. We will use MI_{score} to denote an evaluation criterion which measures the performance of a feature or set of features. The most evaluation criteria in information theoretic feature selection is selecting the feature with the highest mutual information to the class label Y . shown as:

$$MI_{score_i} = I_i(f(x_i); Y) \quad (3)$$

We refer to this feature scoring criterion as “score”, standing for mutual information which considers a score for each feature independently of others. This criterion is very simple, and thus it can replace conditions in the search algorithm. This is a univariate measure, and each feature's score is independent of the other selected features. If we wish to select k features using MI_{score} will pick the top k features, ranked according to their mutual information with the class. We could also

select features until we had reached a predefined threshold of mutual information or another condition.

The proposed method was computed from equation (2). Then, the features from CNNs networks $\hat{f}(\cdot)$ which correspond over mean score would be selected to the fusion task, shown as:

$$\hat{f}(X_1) = MI_{score_i^1} \geq mean$$

$$\hat{f}(X_2) = MI_{score_i^2} \geq mean$$

where superscript¹ is the first dataset and superscript² is the second dataset, respectively.

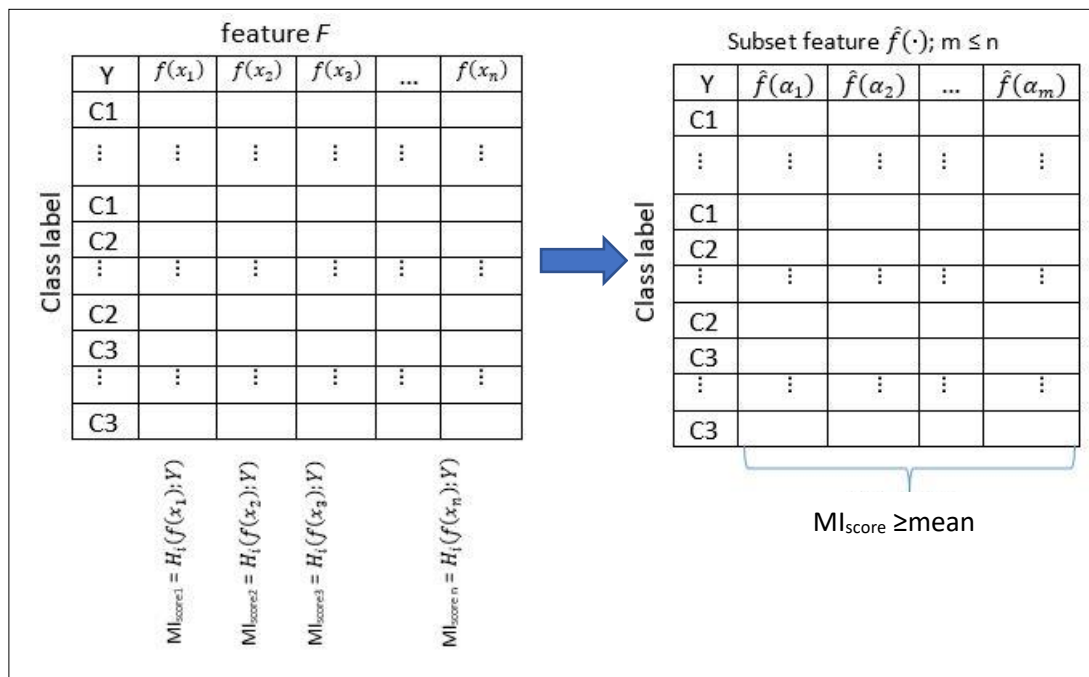


Figure 10 Mutual Information evaluation and selection

This operation can be performed using `sklearn.feature_selection` library. The library was used for estimating the mutual information for a continuous target variable. The function relies on nonparametric methods based on entropy estimation as described in [58] and [59]. Both methods are based on the idea originally proposed in [60].

3.4 Feature fusion using canonical correlation analysis

The features from CNNs networks $\hat{f}(\cdot)$ which correspond over 0.95 score were selected and defined as $\hat{f}(\alpha_1), \hat{f}(\alpha_2), \dots, \hat{f}(\alpha_i); i \in 1, 2, \dots, n$. Given pair of data samples $\alpha_1^i, i \in \{1, 2, \dots, n\}$ of the first dataset, such that $\alpha_2^i, i \in \{1, 2, \dots, n\}$, to the second dataset respectively. Features matrix such that $A_1 = [\alpha_1^1, \alpha_1^2, \dots, \alpha_1^n]$ and $A_2 = [\alpha_2^1, \alpha_2^2, \dots, \alpha_2^n]$, respectively. CCA accounts to fusion more than two datasets based on cross correlation. Although the correlation of more than two datasets could not be easy to examine, the subspace which maximizes the correlations of each pair in sequential has been instead approximated [61]. Given n data samples comprise of features $A_1^1, A_1^2, \dots, A_1^M, M, i \in \{1, 2, \dots, n\}$ from M dataset and n feature, this implementation of pairwise CCA attempts a set of linear transformations $w_1 \in R^{n_1 \times 1}, w_2 \in R^{n_2 \times 1}, \dots, w_M \in R^{n_M \times 1}$ such that the sum of the correlations across all pairs of modalities is maximized, show as:

$$\rho = \underset{w_1, w_2}{\text{maximize}} \frac{w_1^T C_{12} w_2}{\sqrt{(w_1^T C_{11} w_1)(w_2^T C_{22} w_2)}} \quad (4)$$

where C_{11} , C_{22} , and C_{12} are covariance matrix of the features A_1 and A_1 , A_2 and A_2 , then A_1 and A_2 , respectively.

$$\begin{bmatrix} C_{11} & C_{12} \\ C_{21} & C_{22} \end{bmatrix} = \begin{bmatrix} C_{11} \begin{bmatrix} \text{cov}(\alpha_{11}^1) & \cdots & \text{cov}(\alpha_{1q}^1) \\ \vdots & \ddots & \vdots \\ \text{cov}(\alpha_{p1}^1) & \cdots & \text{cov}(\alpha_{pq}^1) \end{bmatrix} & C_{12} \begin{bmatrix} \text{cov}(\alpha_{11}^{12}) & \cdots & \text{cov}(\alpha_{1q}^{12}) \\ \vdots & \ddots & \vdots \\ \text{cov}(\alpha_{p1}^{12}) & \cdots & \text{cov}(\alpha_{pq}^{12}) \end{bmatrix} \\ C_{21} \begin{bmatrix} \text{cov}(\alpha_{11}^{21}) & \cdots & \text{cov}(\alpha_{1q}^{21}) \\ \vdots & \ddots & \vdots \\ \text{cov}(\alpha_{p1}^{21}) & \cdots & \text{cov}(\alpha_{pq}^{21}) \end{bmatrix} & C_{22} \begin{bmatrix} \text{cov}(\alpha_{11}^2) & \cdots & \text{cov}(\alpha_{1q}^2) \\ \vdots & \ddots & \vdots \\ \text{cov}(\alpha_{p1}^2) & \cdots & \text{cov}(\alpha_{pq}^2) \end{bmatrix} \end{bmatrix}$$

By using Lagrangian multiplier techniques one can transform the constrained optimization problem to a generalized multivariate eigenvalue problem of the form:

$$[C_{22}^{-1} C_{21} C_{11}^{-1} C_{12} - \lambda I] = 0 \quad (5)$$

$$\begin{bmatrix} C_{11}^{-1} - \lambda & C_{12} \\ C_{21} & C_{22}^{-1} - \lambda \end{bmatrix} = 0$$

$$(C_{11}^{-1} - \lambda)(C_{22}^{-1} - \lambda) - (C_{21})(C_{12}) = 0$$

Where

$$\lambda = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

After this process, the eigenvalue λ_i was presented. Canonical vectors are unknown and must be computed.

$$[C_{22}^{-1}C_{21}C_{11}^{-1}C_{12} - \lambda_i I]w_j = 0$$

where $i \in 1, 2, \dots, n$ is the number of datasets, for instance, if the first matrix $A_1 \in R^{2 \times 2}$ and the second matrix $A_2 \in R^{2 \times 2}$, the covariant matrix are 2×2 , the eigenvalue compose of λ_1 and λ_2 , the eigenvector compose of $W_1 \in R^{2 \times 2}$ and $W_2 \in R^{2 \times 2}$, while if we have n matrix, the covariant metric are $C_i \in R^{n \times n}$, the eigenvalue compose of $\lambda_1, \lambda_2, \dots, \lambda_n$, the weight matrix compose of $W_i \in R^{n \times n}$.

CCA is a method for finding linear relationships between two datasets. Given two datasets $X = (x_1, x_2, \dots, x_n) \in R^{d \times n}$ and $Y = (y_1, y_2, \dots, y_m) \in R^{d \times m}$ (where x_i, y_i are d -dimensional vectors), CCA finds a canonical coordinate space that maximizes correlations between the projections of the datasets onto that space. For each dimension of this coordinate space, there is a pair of projection weight vectors. Therefore, it is convenient to formulate CCA as a generalized eigenvalue problem that can be solved in one shot. The objective function (equation 4), which solves for the maximum of the canonical correlation vector, is rewritten in terms of the sample covariance C_{xy} of datasets X and Y and the autocovariances C_{xx} and C_{yy} :

Without constraints on the canonical weights w_1 and w_2 , the objective function has infinite solutions. However, the size of the canonical weights can be constrained, such that $w_1^T C_{xx} w_1 = 1$, and $w_2^T C_{yy} w_2 = 1$. This constraint results in the following Lagrangian:

$$L(\lambda, w_1, w_2) = w_1^T C_{xy} w_2 - \frac{\lambda_x}{2} (w_1^T C_{xx} w_1 - 1) - \frac{\lambda_y}{2} (w_2^T C_{yy} w_2 - 1)$$

The objective function can then be formulated as the following generalized eigenvalue problem:

$$\begin{bmatrix} 0 & C_{xy} \\ C_{yx} & 0 \end{bmatrix} \cdot \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} = \rho^2 \begin{bmatrix} C_{xx} & 0 \\ 0 & C_{yy} \end{bmatrix}$$

The generalized eigenvalue problem is also modified to incorporate regularization:

$$\begin{bmatrix} 0 & C_{xy} \\ C_{yx} & 0 \end{bmatrix} \cdot \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} = \rho^2 \begin{bmatrix} C_{xx} + \lambda I & 0 \\ 0 & C_{yy} + \lambda I \end{bmatrix}$$

Regularized CCA is mathematically like partial least squares regression (PLS). Compare to the objective function of CCA (Equation 4) the objective function that is optimized in PLS:

$$\rho = \underset{w_1 \in R^p, w_2 \in R^q}{\text{maximize}} \frac{w_1^T C_{xy} w_2}{\sqrt{(w_1^T w_1 w_2^T w_2)}}$$

Analogously to CCA, PLS can be solved as a generalized eigenvalue problem:

$$\begin{bmatrix} 0 & C_{xy} \\ C_{yx} & 0 \end{bmatrix} \cdot \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} = \rho^2 \begin{bmatrix} I & 0 \\ 0 & I \end{bmatrix}$$

Once W_x and W_y are obtained, the projected new features, called canonical variables, are computed by $U = w_1^T A_1$ and $V = w_2^T A_2$

Two modalities can be used to represent in the fusion space. Given n embedding components $U_i^1, i \in \{1, 2, \dots, n\}$, are expressed via $U = w_{11}^T A_1$ for the first dataset and $V_i^1, i \in \{1, 2, \dots, n\}$, are expressed via $V = w_{21}^T A_2$ for the second dataset. The embedding components U_1, V_1 will be included to the fusion space based on the *largest* λ that is the optimal weight vectors are obtained by maximizing the correlation between the canonical variate pairs, also known as the canonical correlation. CCA develops a canonical function that maximizes the canonical correlation coefficient between the two canonical variates. The canonical correlation coefficient measures the strength of the relationship between the two canonical variates.

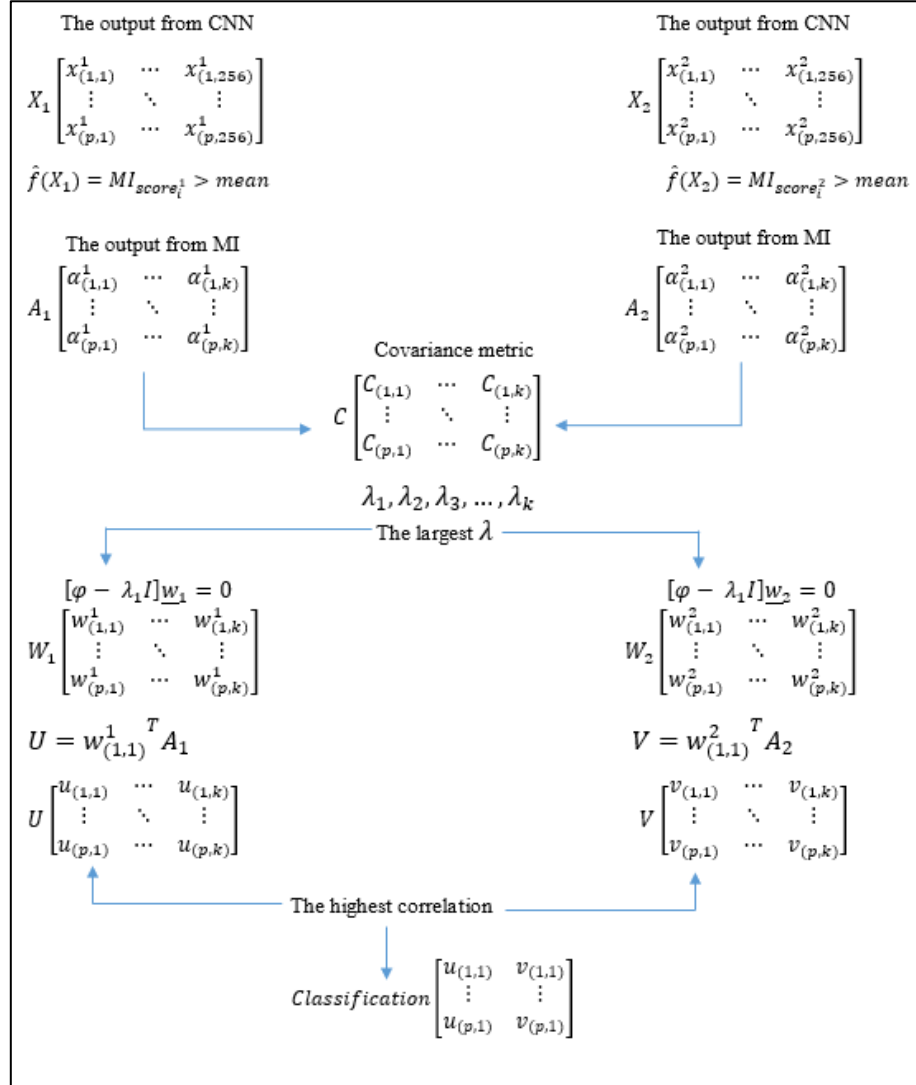


Figure 11 CCA matrix evaluation

In this experiments, two views of images were used, the output features from CNN are $X_1 \in R^{p \times 256}$ and $X_2 \in R^{p \times 256}$, then, the output features from mutual information $\hat{f}(X_i) = MI_{score_i^j} \geq mean$ are $A_1 \in R^{p \times k}$; $k < 256$ and $A_2 \in R^{p \times k}$; $k < 256$, the eigenvalue compose of $\lambda_1, \lambda_2, \dots, \lambda_k$, the eigenvector compose of $W_i \in R^{p \times k}$. The eigenvector corresponding with maximum eigenvalue in each view was used to calculate $U = w_{11}^T A_1$ and $V = w_{21}^T A_2$. So far, the canonical projection vector in each

view was used for classification. Figure 3.3 shows the proposed matrix evaluation. The CCA Canonical Correlation Analysis available on sklearn library.

Example:

```
from sklearn.cross_decomposition import CCA
cca = CCA(n_components=k)
cca.fit(A1, A2)
u, v = cca.transform(A1, A2)
```

3.5 Classification task

After the fusion step, the classification task was performed to classify the target class. Support Vector Machines offers very high accuracy compared to other classifiers such as logistic regression, and decision trees. The SVM classifier separates data points using an optimal hyperplane with the largest amount of margin. It can easily handle multiple continuous and categorical variables. Hyperplane in multidimensional space is constructed to separate different classes.

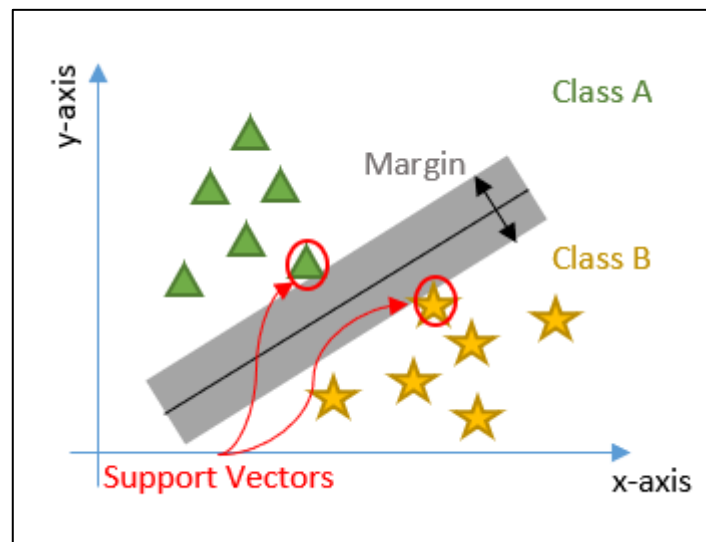


Figure 12 the SVM model finds the correct decision boundary.

We use the SVM model to predict breast cancer based on u and v features. The SVM is available on sklearn library.

Examples:

```
from sklearn import svm
X = [[0, 0], [1, 1]]
y = [0, 1]
clf = svm.SVC()
clf.fit(X, y)
```

where $X = \text{concatenate}(u, v)$, y is target classes, score is the prediction accuracy. In this section, we present experiments on four real datasets to evaluate the effectiveness of the proposed algorithms.

3.6 Comparison strategies

3.6.1 Evaluation of the performance

Confusion matrices were used to evaluate the. These matrices computed sensitivity (true positive rate), specificity (true negative rate) and accuracy of models. The predictive formulas were defined as:

$$\text{Sensitivity} = \frac{TP}{TP + FN}$$

$$\text{Specificity} = \frac{TN}{TN + FP}$$

$$\text{Accuracy} = \frac{TP + TN}{TP + FP + TN + FN}$$

3.6.2 Exploration of correlation analysis via Pearson correlation

Because the objective of the data fusion method is the strongest correlation between two datasets, the Pearson correlation was used to measure the distance of linear relationships between variables to confirm our contribution and compare between other strategies. When the correlation coefficient is close to 1 or -1, their correlation is the strongest. The correlation coefficient is close to 0, their correlation is weak. The calculation formula is as follows:

$$\rho(X, Y) = \frac{\text{cov}(X, Y)}{\sigma_X \sigma_Y}$$

where cov is the covariance, σ_X is the standard deviation of X , and σ_Y is the standard deviation of Y .

3.6.2 Comparison MI-CCA fusion vs. other fusion methods

When dimension reduction methods such as CCA or PCA are able to fusion for 2 views, MI-CCA has compared with the PCA followed by the concatenation of reduction feature. The evaluation of performance and correlation analysis were compared and discussed the result.



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Chapter IV

Result

4.1 Feature extraction

The architecture of VGGNet was used to extract the features for breast ultrasound and mammography images followed by top-layer. There are three steps for extracting the image feature. First, the input of each modes is fed to VGGNet backbone without fully training. Second, the output features from VGGNet layer are trained using CNN top-layer. Proposed top-layer model architecture consists of four types of building blocks. For simplicity, let type 1 is Convolution2D, type 2 is BatchNormalization, type 3 is MaxPooling2D, and type 4 is Flatten. Finally, the backpropagation process is performed only with CNN top-layer. Proposed model architecture consists of two parts that show in Figure 13.

This architecture was applied with two views of mammography and two modes of ultrasound images. Several experiments have been conducted to evaluate the performance and efficiency of the proposed models. These models were trained on the training data and tested them on the test data. The diagnostic efficiency was compared in single dataset, concatenation method, concatenation and PCA method, and MI-CCA using the Confusion matrix. Before the classification task was performed, the feature selection using mutual information was done to select the useful feature sets.

Layer name	Input shape	Output shape
Convolution2D	4, 4, 512	2, 2, 256
BatchNormalization	2, 2, 256	2, 2, 256
MaxPooling2D	2, 2, 256	1, 1, 256
Flatten (Final Layer)	1, 1, 256	256

Table 1 The number of features from top layer.

VGGNet Pre-train

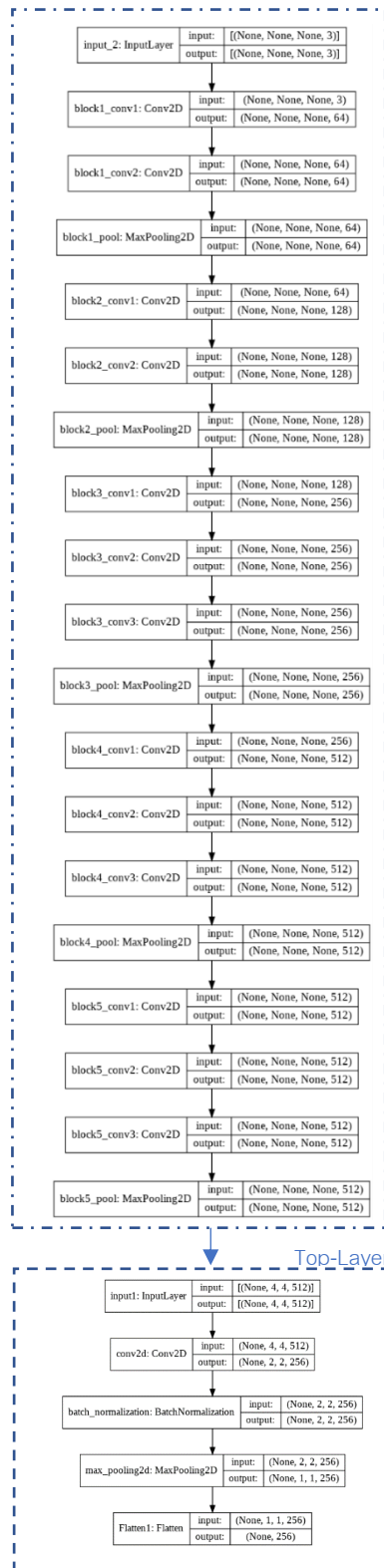


Figure 13 The structures and the number of features for each block.

4.2 Feature selection using mutual information

The MI algorithms described before were applied to the breast image dataset to select diagnostically “informative” features. For comparison purposes, the popular stepwise linear discriminant feature selection was compared before any decision modeling. Briefly, the stepwise linear discriminant analysis begins by selecting the feature with the largest difference in the mean values between the two classes. Subsequently, the next feature is added so that it improved the discrimination power of the model in combination with the existing finding. When a feature is entered into the statistical model, only its linear correlation with the pre-entered findings is considered until the model is improved. The result of the stepwise selection process is a subset of features ordered in terms of importance. This stepwise selection criterion is a search method to select candidate feature sets X . The complexity usually enforces the complexity of the search method for adding or removing each feature based on high scores or low scores. Therefore, the mutual information over feature and target class were established. To determine the number of features required for the estimation of the fusion step, we first tested whether the distribution of each feature is over mean.

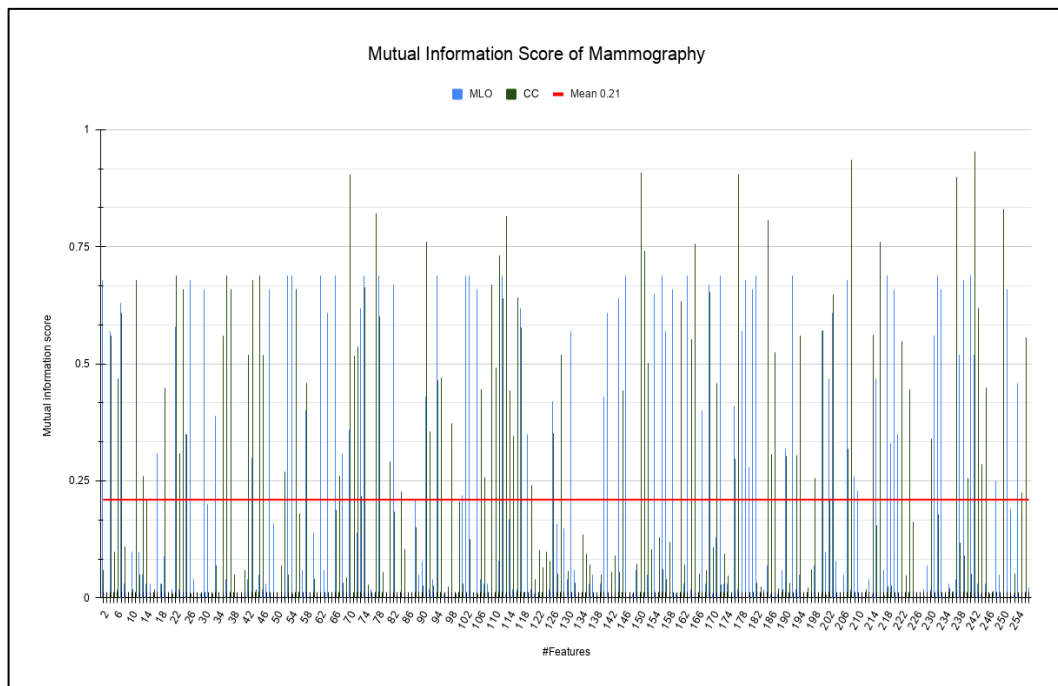


Figure 14 the mutual information score of mammography image

To explore the features contributing to the target class, we calculated the mutual information of each feature set, and selected the source image for each feature. The distribution of each feature is over mean were selected. The top view (CC) has 87 features, while the side view (MLO) has 75 features.

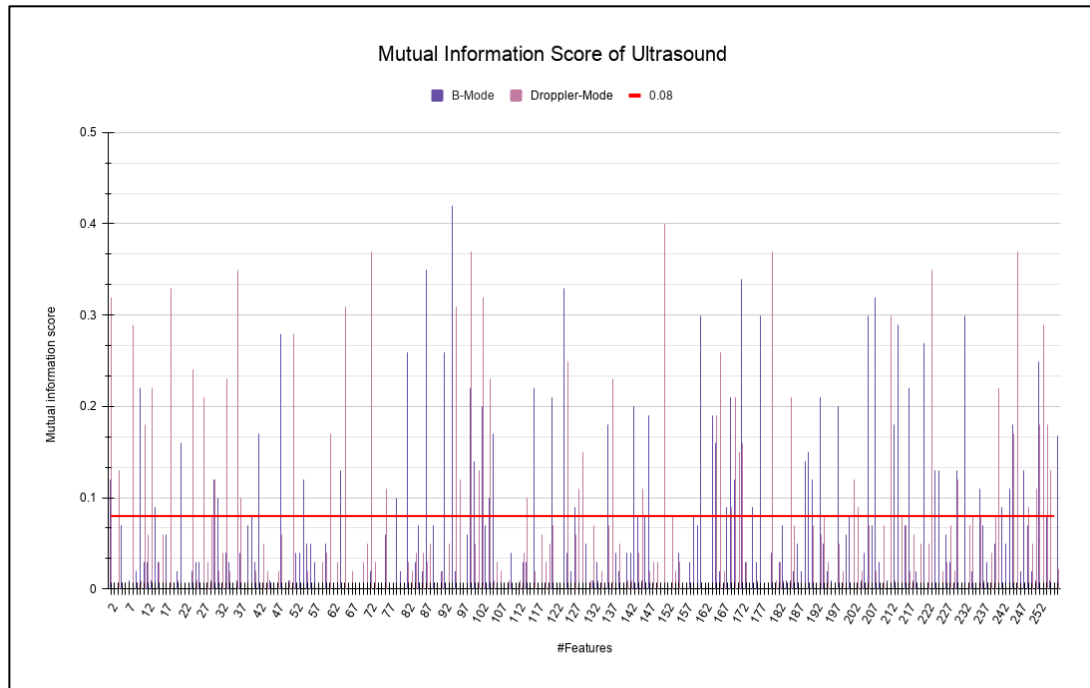


Figure 15 the mutual information score of ultrasound image

To explore the features contributing to the target class, we calculated the mutual information of each feature set, and selected the source image for each feature. The distribution of each feature is over mean were selected. The B-mode has 78 features, while the Doppler mode has 76 features.

Model	Mammogram		Ultrasound	
	CC	MLO	B-Mode	Doppler
Single	256	256	256	256
Mutual Information	87	75	78	76
Reduction	66%	70.70%	68.53%	70.31%

Table 2 comparison of the number of features

The number of features is reduced using mutual information. The top view mammogram is reduced from 256 features to 87 features, while the side view mammogram is reduced from 256 features to 75 features. The B-Mode ultrasound is reduced from 256 features to 78 features, while Doppler mode ultrasound is reduced from 256 features to 76 features. The results show that the exploration of mutual information could reduce the high-dimensional dataset.

4.3 Feature fusion using MI-CCA

Two modalities can be used to represent in the fusion space. the output features from mutual information $\hat{f}(X_i) = MI_{score_i^j} \geq \text{mean}$ are $A_1 \in R^{p \times k}$; $k < 256$ and $A_2 \in R^{p \times k}$; $k < 256$, the eigenvalue compose of $\lambda_1, \lambda_2, \dots, \lambda_k$, the eigenvector compose of $W_i \in R^{p \times k}$. Given n embedding components $U_i^1, i \in \{1, 2, \dots, n\}$ are expressed via $U = w_{11}^T A_1$ and $V_i^1, i \in \{1, 2, \dots, n\}$ are expressed via $V = w_{21}^T A_2$. The embedding components U_i^1, V_i^1 will be included to the fusion space based on the k -largest λ (which is the variance ratio).

CCA is a method for finding linear relationships between two datasets. Given two datasets $X = (x_1, x_2, \dots, x_n) \in R^{d \times n}$ and $Y = (y_1, y_2, \dots, y_m) \in R^{d \times m}$ (where x_i, y_i are d -dimensional vectors), CCA finds a canonical coordinate space that maximizes correlations between the projections of the datasets onto that space. For each dimension of this coordinate space, there is a pair of projection weight vectors. Therefore, it is convenient to formulate CCA as a generalized eigenvalue problem that can be solved in one shot. The objective function, which solves for the

maximum of the canonical correlation vector, is rewritten in terms of the sample covariance C_{xy} of datasets X and Y and the autocovariances C_{xx} and C_{yy} :

$$\rho = \underset{w_1, w_2}{\text{maximize}} \frac{w_1^T C_{xy} w_2}{\sqrt{(w_1^T C_{xx} w_1)(w_2^T C_{yy} w_2)}} \quad (4)$$

Without constraints on the canonical weights w_1 and w_2 , the objective function has infinite solutions. However, the size of the canonical weights can be constrained, such that $w_1^T C_{xx} w_1 = 1$, and $w_2^T C_{yy} w_2 = 1$. This constraint results in the following Lagrangian:

$$L(\lambda, w_1, w_2) = w_1^T C_{xy} w_2 - \frac{\lambda_x}{2} (w_1^T C_{xx} w_1 - 1) - \frac{\lambda_y}{2} (w_2^T C_{yy} w_2 - 1)$$

The objective function can then be formulated as the following generalized eigenvalue problem:

$$\begin{bmatrix} 0 & C_{xy} \\ C_{yx} & 0 \end{bmatrix} \cdot \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} = \rho^2 \begin{bmatrix} C_{xx} & 0 \\ 0 & C_{yy} \end{bmatrix}$$

The generalized eigenvalue problem is also modified to incorporate regularization:

$$\begin{bmatrix} 0 & C_{xy} \\ C_{yx} & 0 \end{bmatrix} \cdot \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} = \rho^2 \begin{bmatrix} C_{xx} + \lambda I & 0 \\ 0 & C_{yy} + \lambda I \end{bmatrix}$$

Regularized CCA is mathematically like partial least squares regression (PLS). Compare to the objective function of CCA (Equation 4) the objective function that is optimized in PLS:

$$\rho = \underset{w_1 \in R^p, w_2 \in R^q}{\text{maximize}} \frac{w_1^T C_{xy} w_2}{\sqrt{(w_1^T w_1)(w_2^T w_2)}}$$

Analogously to CCA, PLS can be solved as a generalized eigenvalue problem:

$$\begin{bmatrix} 0 & C_{xy} \\ C_{yx} & 0 \end{bmatrix} \cdot \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} = \rho^2 \begin{bmatrix} I & 0 \\ 0 & I \end{bmatrix}$$

Once W_x and W_y are obtained, the projected new features, called canonical variables, are computed by $U = w_1^T A_1$ and $V = w_2^T A_2$

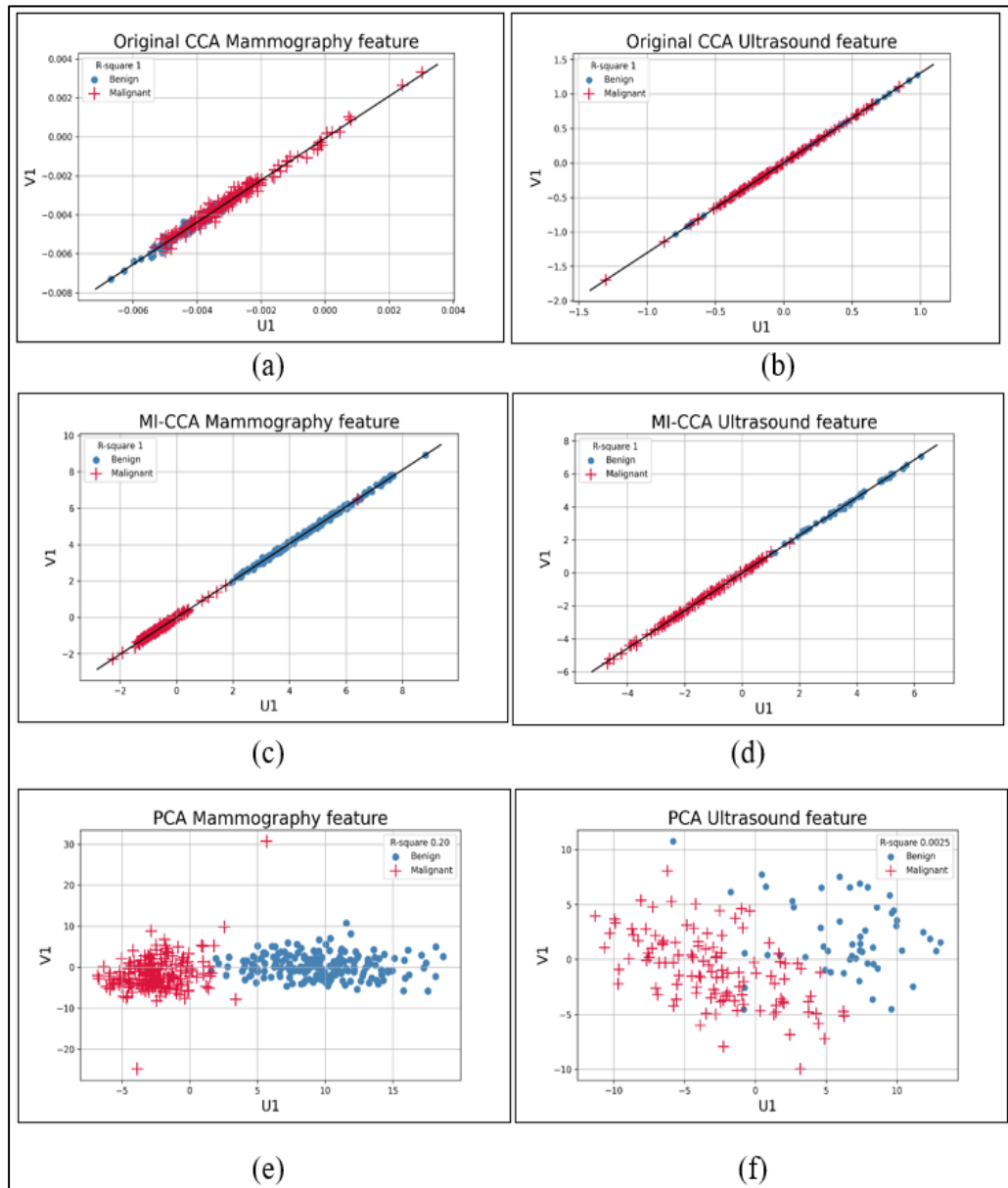


Figure 16 the correlation of original CCA, Concatenate-PCA and MI-CCA

Figure 16 shows the comparisons of Pearson correlation of original CCA, Concatenate-PCA and MI-CCA. The original CCA and MI-CCA show very high correlation (Figure 16a, b, c, d), while the PCA is a lower correlation than CCA strategies (Figure 16e, f). Although PCA seems to distinguish the class label better

than CCA, they are rarely optimal because they do not take into account the complementarity of groups of features together, something that most supervised algorithms can use very well.

4.4 Classification task

Several experiments have been conducted to evaluate the performance and efficiency of the proposed models. These models were trained on the training data and tested them on the test data. The diagnostic efficiency was analyzed using the Confusion matrix.

4.4.1 Single mammography

Table 3 shows the models' diagnostic efficiency of the mammography image. Using the SVM classification, the results achieve an accuracy of 90.00% on the top view (CC) and 96.60% on the side view (MLO).

Dataset	Accuracy	Sensitivity	Specificity	F1-Score	Precision
CC-View	0.90	1	0.82	0.88	0.79
MLO-View	0.91	0.85	0.99	0.92	0.99

Table 3 diagnostic efficiency of the mammography image.

Figure 17 show the Confusion matrix of two views were compared. The sensitivity on the top view (CC) is 0.80, the specificity on the top view (CC) is 1. The sensitivity on the side view (MLO) is 0.99, the specificity on the side view (MLO) is 0.82.

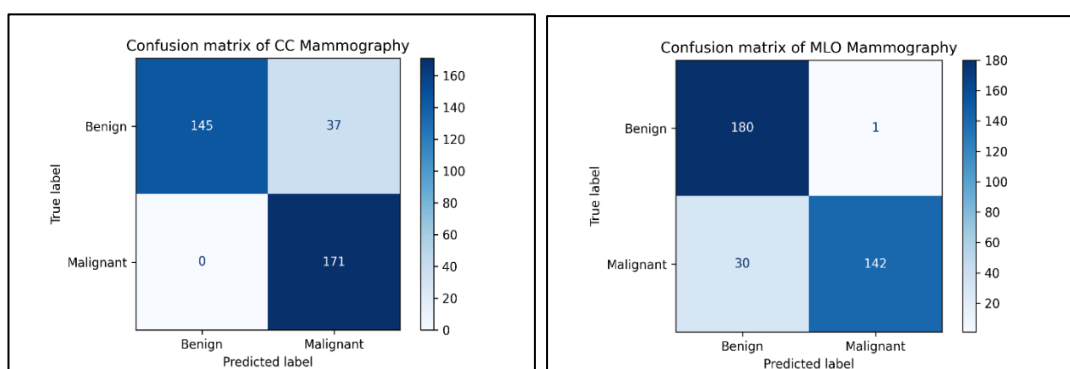


Figure 17 the mammography confusion matrix CC (left) and MLO (right).

These results show that the side view is more accurate than the top view. However, the top view seems to distinguish the malignant lesions better than the side view. In addition, we found that the side view seems to distinguish the benign lesions better than the top view.

4.4.2 Single ultrasound

Table 4.2 shows the models' diagnostic efficiency of the breast ultrasound image. Using the SVM classification, the results achieve an accuracy of 93.23% on the B-Mode and 91.73% on the Doppler mode.

Dataset	Accuracy	Sensitivity	Specificity	F1-Score	Precision
B-Mode	0.93	0.91	1	0.87	0.78
Doppler mode	0.91	1	0.89	0.85	0.74

Table 4 diagnostic efficiency of the breast ultrasound image.

Confusion matrix of two modes were compared. The sensitivity on the B-Mode is 0.78, the specificity on the B-Mode is 1. The sensitivity on the Doppler mode is 0.75, the specificity on the Doppler mode is 1.

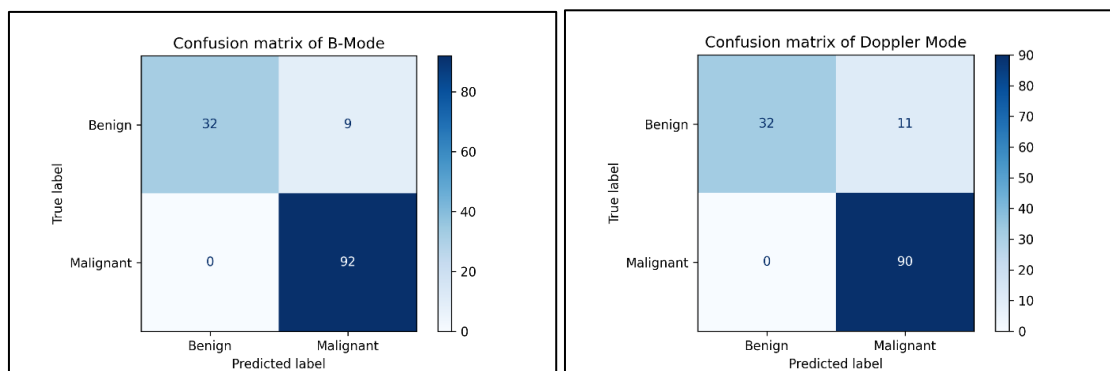


Figure 18 the confusion matrix of B-Mode (left) and Doppler mode (right).

These results demonstrated that B-Mode is more accurate than the Doppler mode (see Figure 18). From the experiment results, it is consistent with our assumption that the multi-evidence could complement the diagnosis information.

4.2 Fusion strategies

4.2.1 The fusion using PCA

The output from feature extraction was represented by 256 features for each view. Then, two datasets were concatenated into one matrix obtained 512 features. This data matrix is the input data set for PCA.

Mammogram: figure 19 illustrates the maximum percentage of total variance only 5 principal components while remaining components account for less than 0 of the total components. Hence, the 75 components were selected (To equal with MI-CCA). Thus, the new data set is of the dimension 600×75 . This is the new input set for the SVM classification model.

Ultrasound: figure 20 illustrates the maximum percentage of total variance only 10 principal components while remaining components account for less than 0 of the total components. Hence, the 76 components were selected (To equal with MI-CCA). Thus, the new data set is of the dimension 255×76 . This is the new input set for the SVM classification model.

Table 5 and table 6 show the model performance and comparisons.

4.2.2 The fusion of mammography using CCA

Table 5 shows the models' diagnostic efficiency of fusion mammography. When compare with the single dataset, MI-CCA improves high diagnostic accuracy. Using the PCA, the result achieves an accuracy of 0.96, while MI-CCA is achieved high diagnostic accuracy of 0.98.

Dataset	Accuracy	Sensitivity	Specificity	F1-Score	Precision
CC-View	0.90	1	0.82	0.88	0.79
MLO-View	0.91	0.85	0.99	0.92	0.99
PCA	0.96	1	0.93	0.96	0.93
MI-CCA	0.98	0.97	1	0.98	1

Table 5 comparison of diagnostic efficiency of mammography.

Confusion matrix of two fusion strategies were compared (Figure 19). The sensitivity on the PCA is 0.93, the specificity on the PCA is 1. The sensitivity on the MI-CCA is 1, the specificity on the MI-CCA is 1. These results show that proposed MI-CCA is more accurate than the PCA approach.

4.2.3 The fusion of ultrasound

Table 4.4 shows the models' diagnostic efficiency of fusion mammography. When compare with the single dataset, MI-CCA improves high diagnostic accuracy. Using the PCA, the result achieves an accuracy of 0.91, while MI-CCA is achieved high diagnostic accuracy of 0.95.

Dataset	Accuracy	Sensitivity	Specificity	F1-Score	Precision
B-Mode	0.93	0.91	1	0.87	0.78
Doppler mode	0.91	1	0.89	0.85	0.74
PCA	0.91	0.89	0.91	0.84	0.80
MI-CCA	0.95	1	0.94	0.92	0.86

Table 6 comparison of diagnostic efficiency of ultrasound.

Confusion matrix of two fusion strategies were compared. The sensitivity on the PCA is 0.80, the specificity on the PCA is 0.95. The sensitivity on the MI-CCA is 0.81, the specificity on the MI-CCA is 1. These results show that proposed MI-CCA is more accurate than the PCA approach. Because of MI-CCA is performed using high

mutual information between variables and class labels. Therefore, the variables tend to be more compatible with the class labels than other fusion strategies.

Based on our experiments, the fusion strategies could improve diagnosis performance rather than using a single dataset because multi-evidence in medical diagnosis can provide more relevant information.

4.3 Explain variance ratio

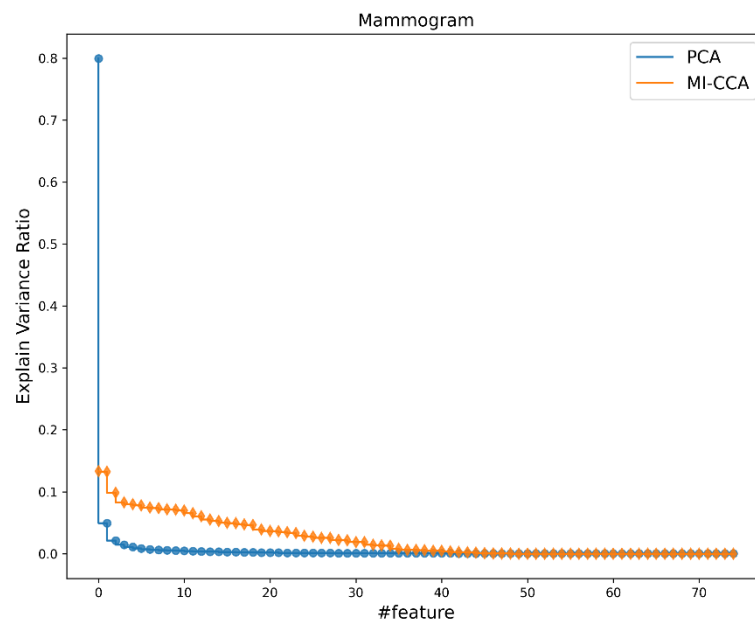


Figure 19 Mammogram explain variance ratio

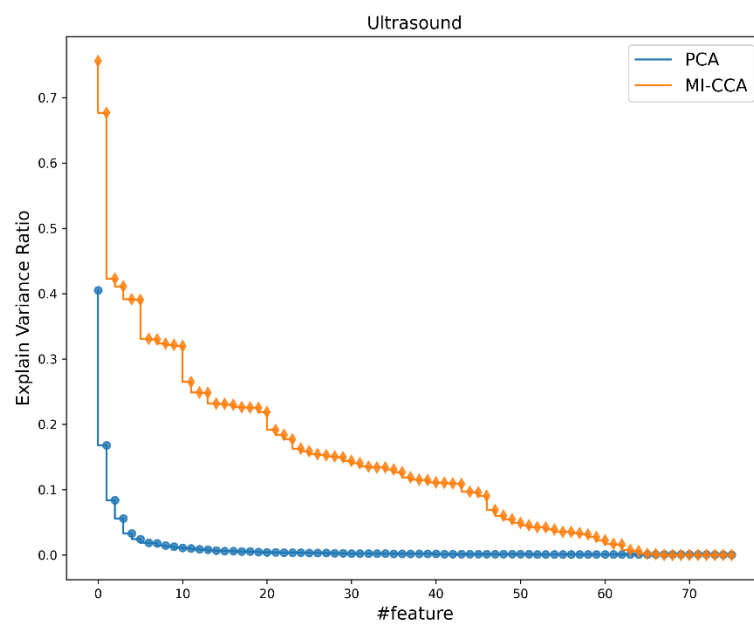


Figure 20 Ultrasound explain variance ratio

The Explained Variance Ratio was used to evaluate the usefulness of features and to choose how many features to use in the model. The explained variance ratio is the percentage of the variance of the selected features. In our experiments, selected features from MI-CCA tend to present the highest number of features that can explain the variance compared with concatenate-PCA method.



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Chapter V

Discussion

In this work, the multi-evidence learning based on feature fusion strategy of multiple views was performed to build breast cancer classification models. The performance of state-of-the-art CNN architectures on the feature extraction was investigated. Furthermore, the supervised feature selection which explores the mutual information was examined for distinguishing the related feature with the class label to reduce the dimension. Finally, information fusion using canonical correlation analysis was performed to combine multi-evidence features. According to our findings, three challenge problems of multiple dataset learning were solved and discussed.

5.1 Consensus principle and complementary principle

The consensus principle and complementary principle could be improved the diagnosis accuracy. The consensus principle aims to maximize the agreement on multiple distinct evidence, while the complementary principle can be employed to comprehensively and accurately describe the data by using the data that may contain some knowledge that other evidences do not have. According to our experiments and results, multi-evidence learning using MI-CCA tends to good consensus and complementary as show in predictions and explanations.

5.1.1 Mammogram dataset

Breast mammography is examined by two views including a side view (MLO) and top view (CC) of the breast. It is possible that some pitfalls presented in the top view (CC), whereas some missed presented in the side view (MLO).



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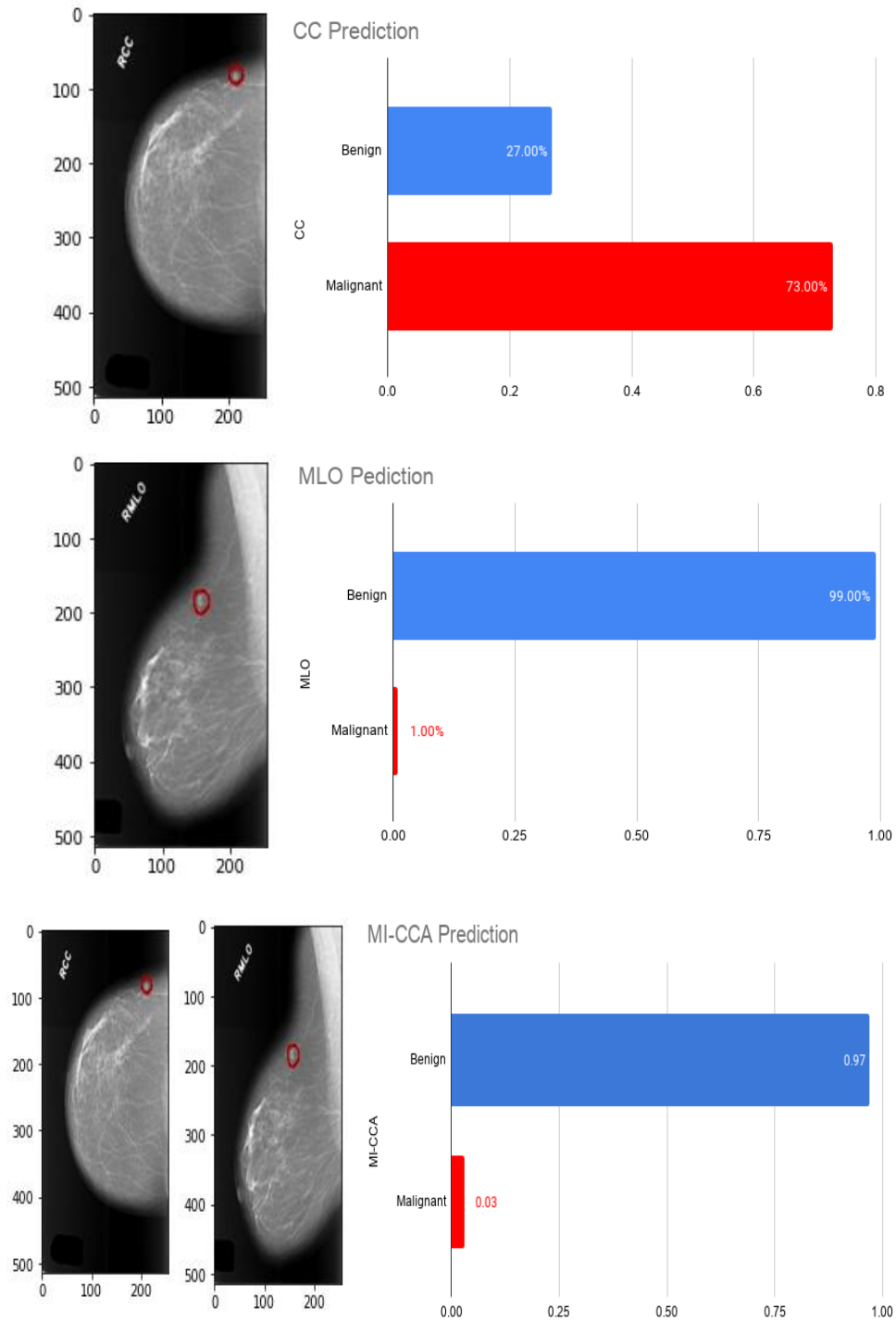


Figure 21 the consensus principle of benign lesion (red circle). The top is the original CC view image and its prediction. The bottom is the original MLO view image and its prediction.



Figure 21 shows the consensus principle. The single model in the top view decide this image in 73% malignant, while the side view decide this image in 99% benign. The explanation, the likelihood of false positives is expected in the top view because the top view can distinguish the positive class better than the side view as shown in the result (see Figure 17). In addition, it is possible that multiple views can be employed to describe the data comprehensively and accurately.

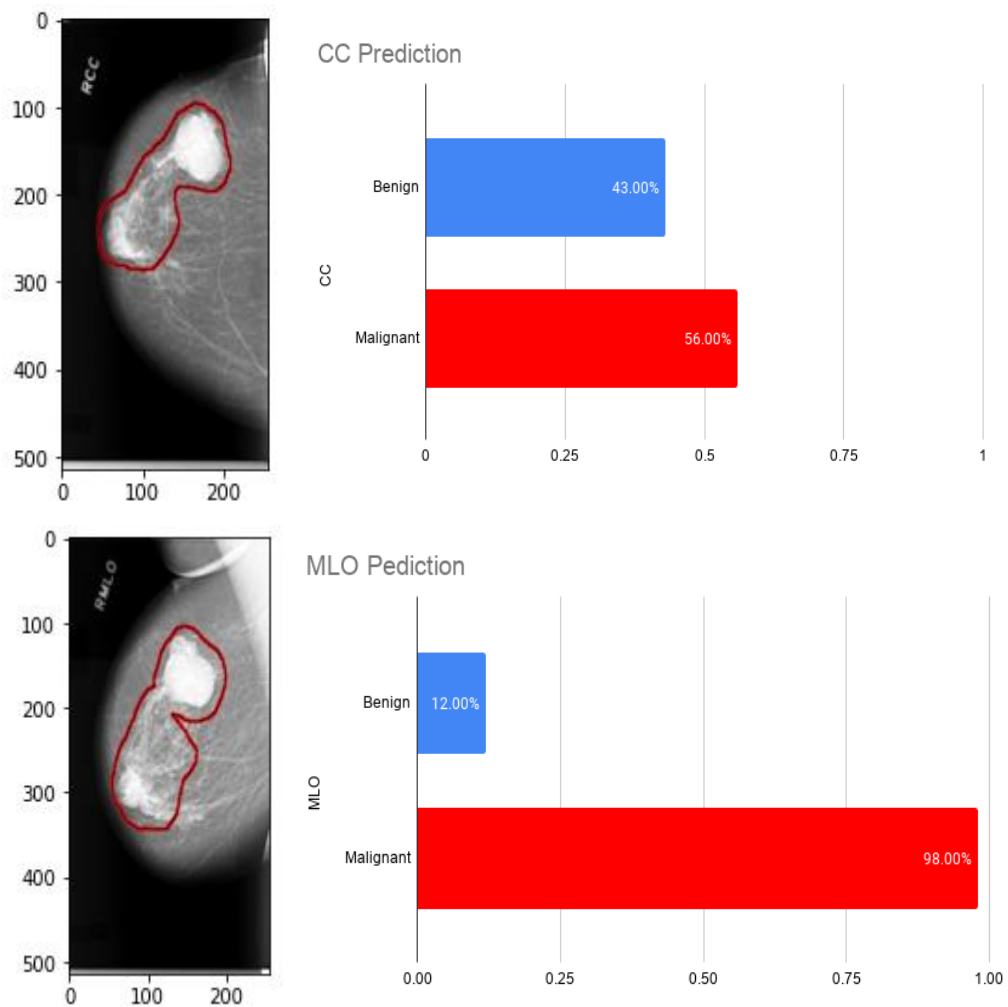


Figure 22 the complement principle of malignant lesion (red boundary). The top is the original CC view image and its prediction. The bottom is the original MLO view image and its prediction.

Figure 22 shows the complement principle. Although both models are correct predictions, the top view prediction is indecisive (43%:57%), while the side view is precisely prediction (2%:98%). It is possible that each view of the data may contain some knowledge that other views do not have.

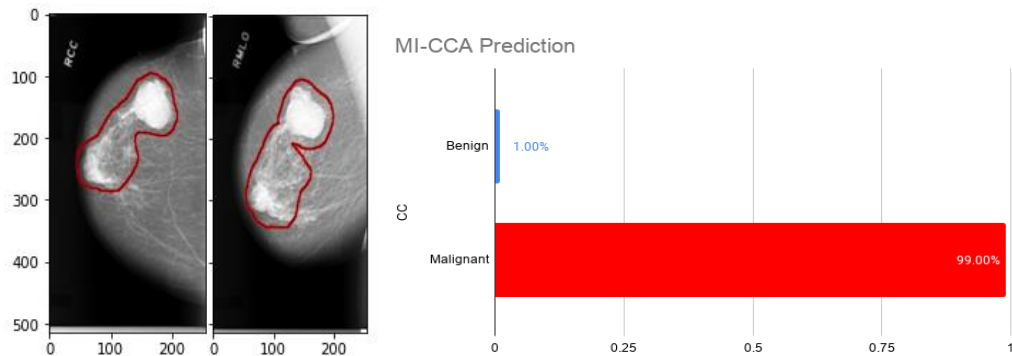


Figure 23 the prediction of MI-CCA of Mammography

Figure 23 the prediction of MI-CCA shows the highest prediction. The explanation, the complementary information underlying multiple views can be exploited to improve the learning performance by utilizing the complementary principle.

5.1.2 Ultrasound dataset

Breast ultrasound is examined by two modes including B-mode (grayscale) and color Doppler mode (color). B-mode displays the acoustic impedance of a two-dimensional cross-section of tissue, while color Doppler mode displays blood flow, the motion of tissue over time, the location of blood, the presence of specific molecules, the stiffness of tissue, or the anatomy of a three-dimensional region.

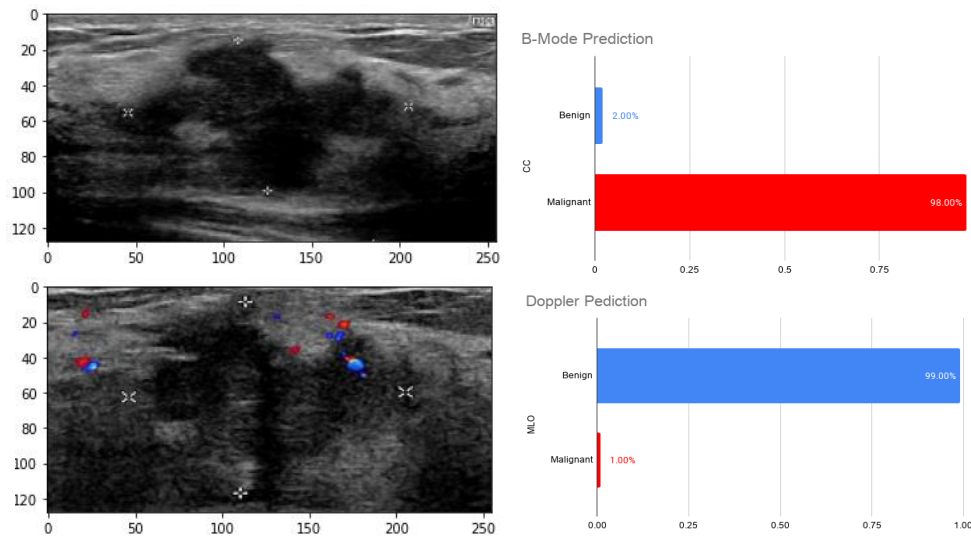


Figure 24 the consensus principle of malignant lesion. The top is the original B-Mode and its prediction. The bottom is the original Doppler and its prediction.

The single model in B-Mode decide this image in 99% malignant, while the Doppler decide this image in 99% benign.

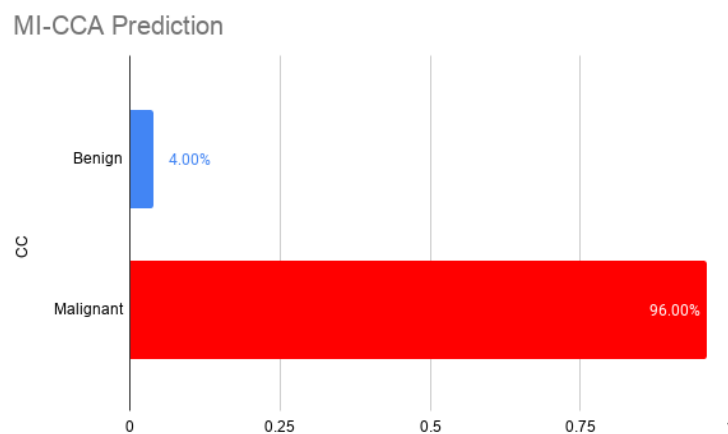


Figure 25 the prediction of MI-CCA of Ultrasound

Based on the above analysis, 'MI-CCA' disseminates the following suggestions: firstly, even if a single evidence approach does not perform well, an ensemble of evidence still can outperform individual evidence. Secondly, since accurate diagnosis is important, models trained on imbalanced training data can

provide wrong predictions, due to possible overfitting during the training. In this case, even a high accuracy score can be achieved based on mutual information without predicting minor classes. Thirdly, accurate predictions do not only depend on single imaging modalities but could also build upon additional modalities.

In addition, early detection and diagnosis of breast cancer is critical for survival [62-64]. Early diagnosis requires accurate and reliable tool to distinguish benign and malignant tumors. The major cancer screening problems are false negative to effect with the patients who lose the chance to early treatment. The false positive developed unnecessary surgery such as biopsy. Our experiments reduce the false positive and false negative, furthermore, overall accuracy is better than the single model.

5.2 The correlation among datasets

One traditional solution for the multi-view problem is to concatenate vectors from different views into a new vector and then apply single-view learning algorithms straightforwardly on the concatenated vector. However, different data sources may have correlated and uncorrelated features. Correlation-based techniques have been used to find a set of new attributes that correlate and ensure their compatible between multiple views. Therefore, not only high accuracy but also the maximal correlation has been important. Data fusion as described in Zhang et al [65]. noted that dataset X and Y will be similar information when there is a maximal correlation. When two modalities are maximally correlated, each modality tends to represent similar information. Thus, two objects, which are a high correlation, will be added to the subspace. In practical, the advantage of data fusion should meet two requirements [66]. First, the final layer should be accurate. Second, the fusion layers should be high relationship among views. Our results differ from paper [67] that reported maximized the correlation of dataset.

Three implementations of Original-CCA, PCA, and MI-CCA are compared by Pearson correlation. The proposed MI-CCA not only had the highest correlation but also the mutual information was helpful to maximize the accuracy performance.

Moreover, when the prediction relies on investigating the outlier, an MI-CCA may provide the best fit and robust to outliers.

5.3 Dimension reduction of a huge dataset

Canonical correlation analysis (CCA) is a multivariate statistical method which describes the associations between two sets of variables. The objective is to find linear combinations of the variables in each data set having maximal correlation. However, the multiple datasets are typically high-dimensional, containing a lot of variables. In high dimensional setting, the classical canonical correlation analysis is complicated.

We propose a sparse canonical correlation analysis by adding mutual information on the canonical vectors. A two-stage approach to the sparse CCA problems was introduced, where in the first stage we computed the mutual information between the feature and the class labels. Then the distribution of each feature is over mean were selected. These sparsity features shrink smaller matrices and use to the CCA step. Our experiment demonstrated that the mammogram dataset reduced by more than 60%, while the ultrasound dataset reduced by more than 70%. These results show that the search space tends to reduce the boundaries set. Contrary to other popular sparse CCA procedures[68, 69] (i.e. Witten et al., 2009; Parkhomenko et al., 2009) smaller matrices are determined in covariance metrics instead of the high dimension in original CCA. In the other work, Lykou and Whittaker (2010) [70] also treat CCA as a least squares problem. They focus on orthogonality properties of CCA and only construct the first two pairs of sparse canonical vectors. Their approach could be extended to higher order canonical correlations, but this would increase the number of orthogonality constraints and the computing time substantially.

5.4 Summary

The applications of the multi evidences learning used in this present study provide useful insights into the information. The findings can be summarized as follows:

- The feature selection criterion can minimize the error rate by considering the mutual information of feature sets. This mutual information is maximized by having a high predictive probability for all the true labels of a training dataset. In general, we can adjust the quality of our training model, but we should not adjust upon the data that will be affected with overfitting problem. Assuming from mutual information allows us to select feature sets which maximizes the high predictive probability, and then to build classification models which maximize the probability based on that feature sets.

- Both complementary and consensus principles play important roles in multi-evidence learning. By considering the complementary information underlying distinct views, advantage can be taken of metric learning to construct a shared latent subspace to precisely measure the dissimilarity between different examples. In other words, the complementary information in distinct views that influences the performance of classification model.

- The strength of correlation between two quantitative variables means that two or more variables have a strong relationship with each other, while a weak correlation means that the variables are hardly related. This conclusion plays important role with data combination strategy. It is very important to understand relationship between variables to draw the right conclusion from a statistical analysis. The relationship between variables determines how the right conclusions are reached. Without high correlation of dataset, many pitfalls can appear that accompany statistical analysis and infer wrong results from fusion data.



Chapter VI

Conclusion and Future Work

6.1 Conclusion

In this study, we proposed a multi-evidence learning model that utilizes the extracted information of two views of mammograms and two modes of breast ultrasound for breast cancer classification. We concluded that multi-evidence feature fusion based on mutual information including canonical correlation analysis is more efficient than a single view system. We demonstrated on three challenging. First, MI-CCA plays an important role in consensus and complementary when a single evidence approach has an ambiguous interpretation. Second, correlation-based techniques have been used to find a set of new attributes that correlate and ensure their compatible between multiple views. The proposed MI-CCA not only had the highest correlation but also the mutual information was helpful to maximize the accuracy performance. Finally, dimension reduction of a huge dataset is considered. The mutual information shrinks smaller matrices and use to the CCA. Our experiment demonstrated that the mammogram dataset reduced by more than 60%, while the ultrasound dataset reduced by more than 70%. Additionally, we demonstrated that multi-evidence learning over the mutual information including canonical correlation analysis led to a more refined feature representation that also resulted in increased classification accuracy.

6.2 Limitations of MI-CCA and Future Perspective

This study can learn models from multi-evidence data by considering the fusion of different views. The experimental results show the extensive development of multi-evidence learning and its promising performance compared to single model learning. However, some limitations of our study should be considered.

In theoretical perspective, estimating mutual information from samples struggle to scale up to modern machine learning problems. There are two limitations of variational approaches to MI estimation. The theoretically demonstrate that the



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variance of certain estimators is high. These limitations challenge the effectiveness of these methods for estimating or optimizing MI.

In diagnosis perspective, First, the other information such as patient demographics and health history were not included. Second, other significant tumor characteristics such as dense breast or fat breast were considered. Finally, more sample datasets were included in future work. In addition, like the clinicians' decision, other medical evidence should be fused for diagnosis.



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VITA

NAME	นางสาวต๋องใจ แยมผกา
DATE OF BIRTH	24 มิถุนายน 2523
PLACE OF BIRTH	กรุงเทพมหานคร
INSTITUTIONS ATTENDED	วิทยาศาสตรมหาบัณฑิต (วิทยาศาสตรคอมพิวเตอร์)
HOME ADDRESS	388/95 ถนนร่มเกล้าซอย 22 แขวงมีนบุรี เขตมีนบุรี กทม. 10510
PUBLICATION	<p>1. An application of process mining for queueing system in health service, 13th International Joint Conference on Computer Science and Software Engineering (JCSSE), 2016</p> <p>Integrated Dataset Method for Breast Cancer Prediction, International Conference on Innovation in Cancer Research and Care, 18-20 December 2017, Bangkok, Thailand.</p> <p>2. Combination of B-mode and color Doppler mode using mutual information including canonical correlation analysis for breast cancer diagnosis</p> <p>Medical Ultrasonography, Vol 22, No 1, 2020, p49-57</p>



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