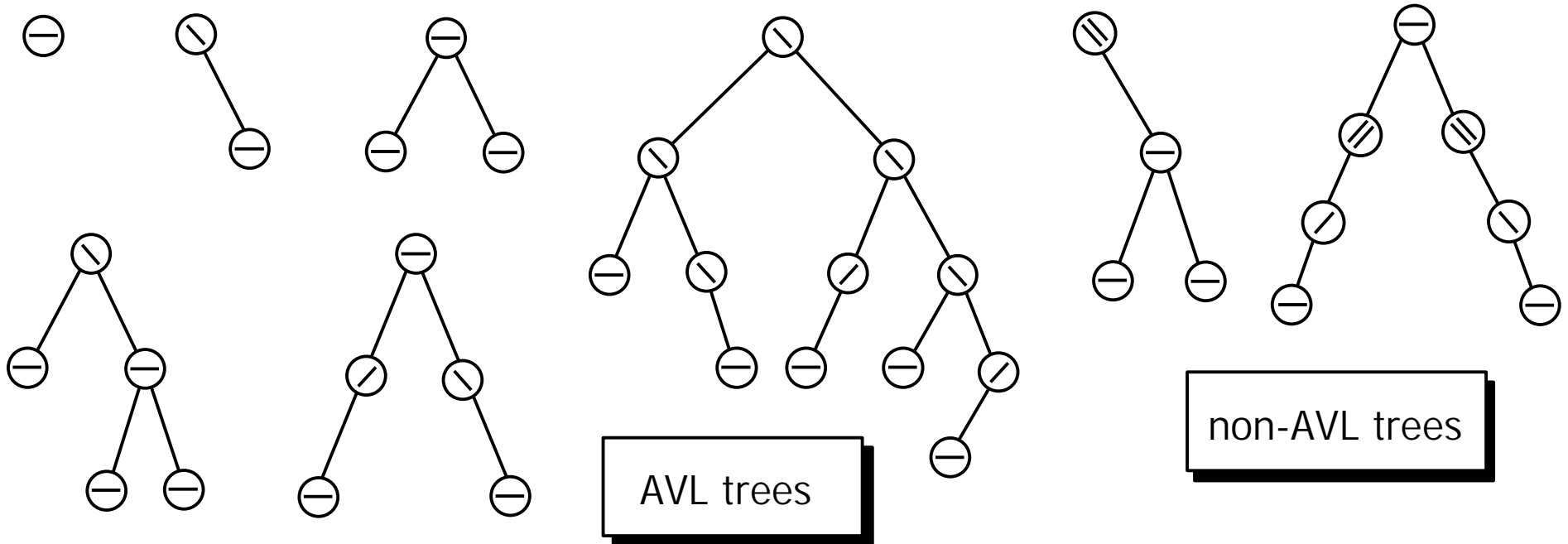
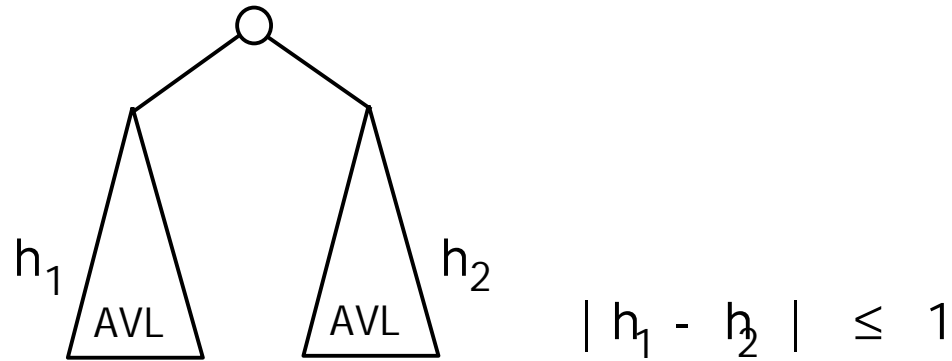
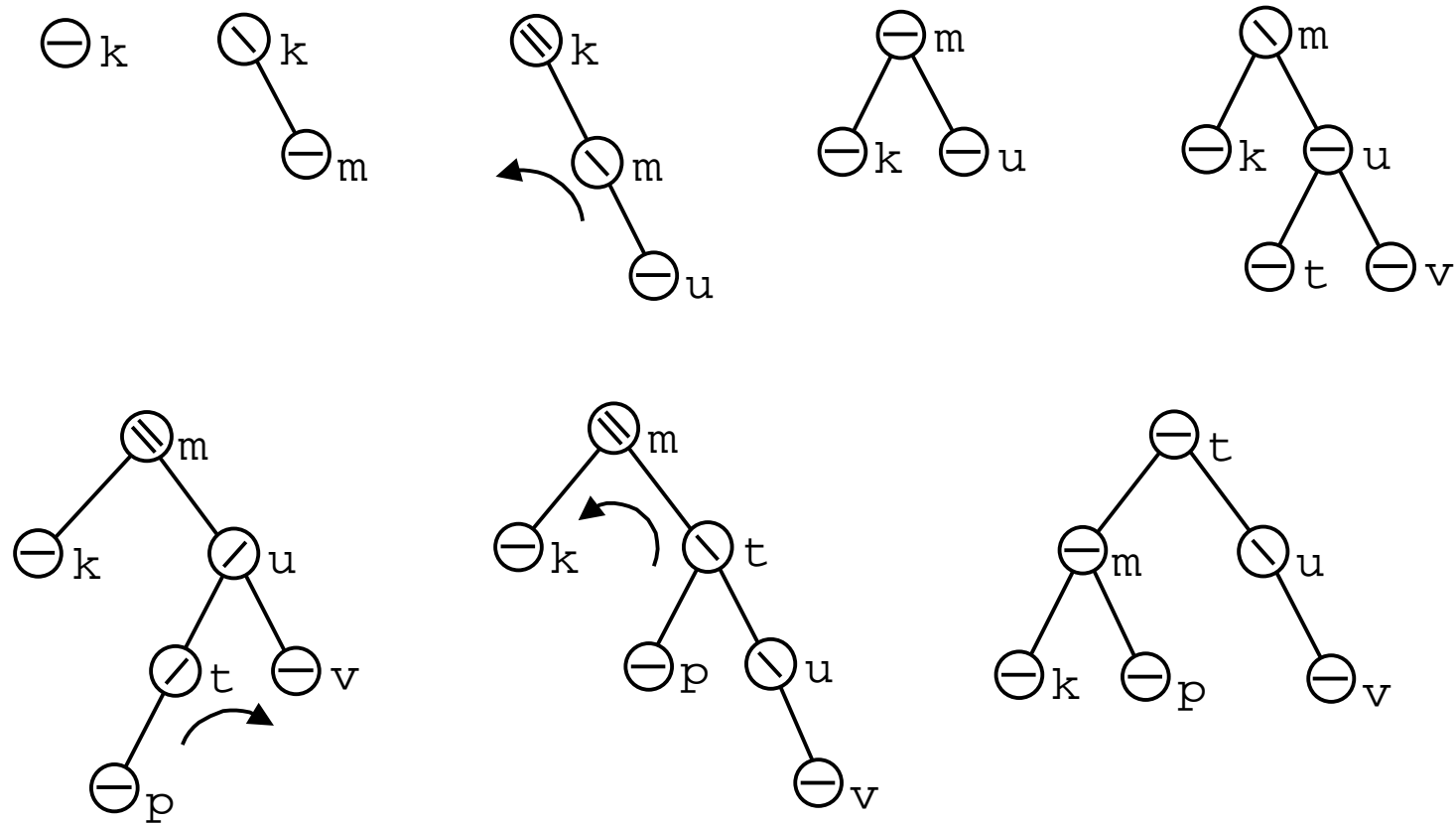

AVL TREES

Height Balance : AVL Trees

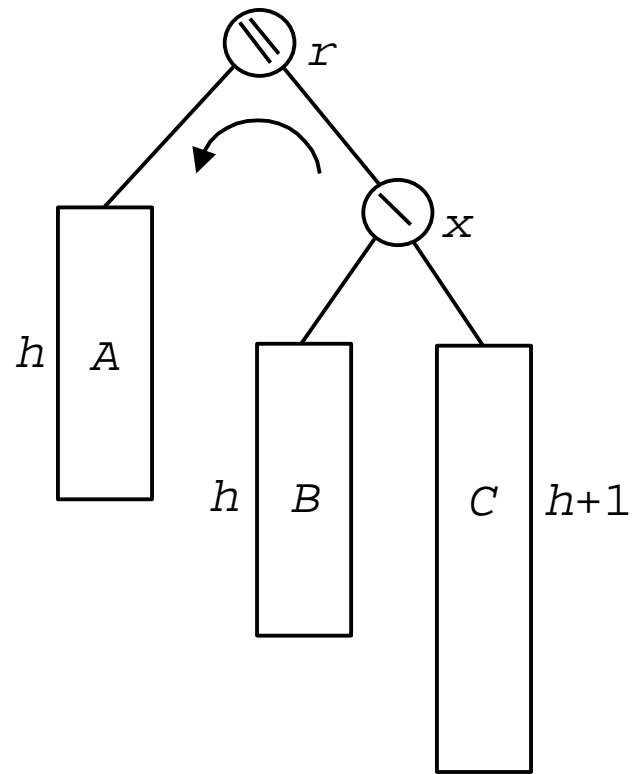


AVL Trees : Insertion

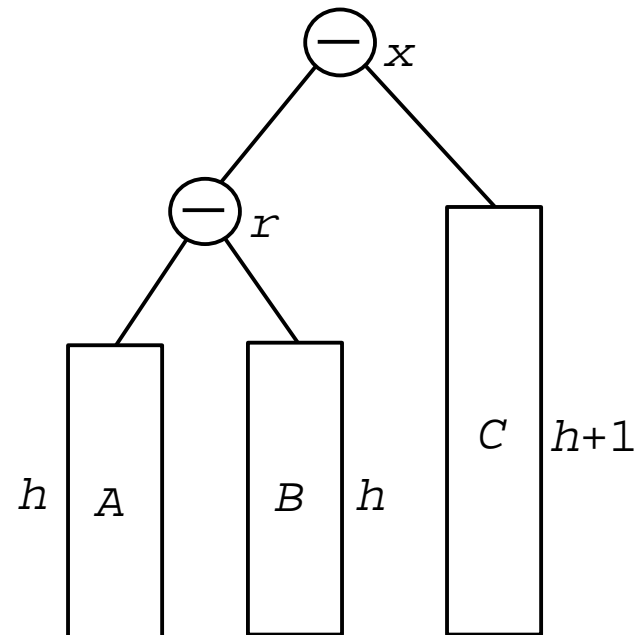


Rotations

Rotations : Right High (Left Rotation)

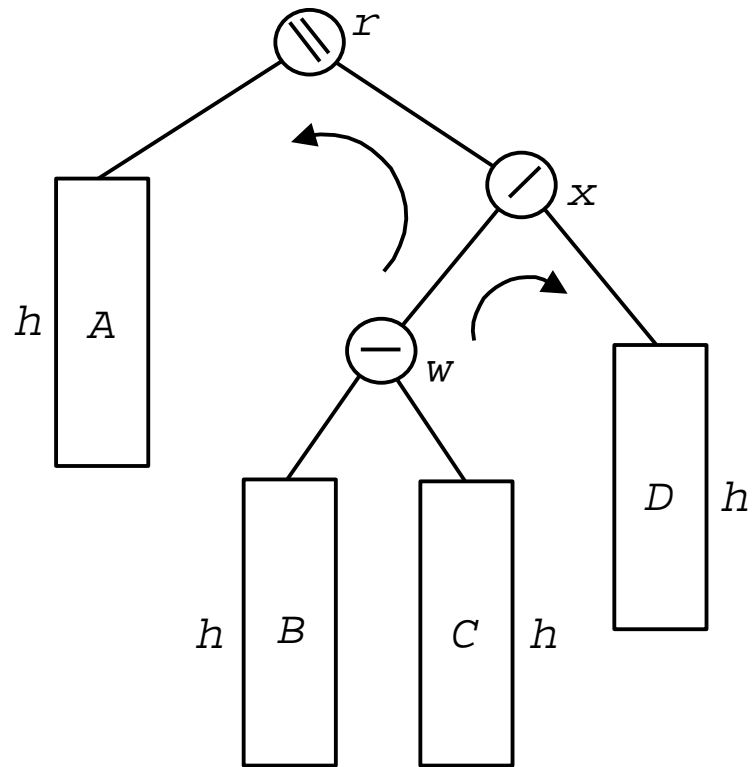


Total height = $h+3$

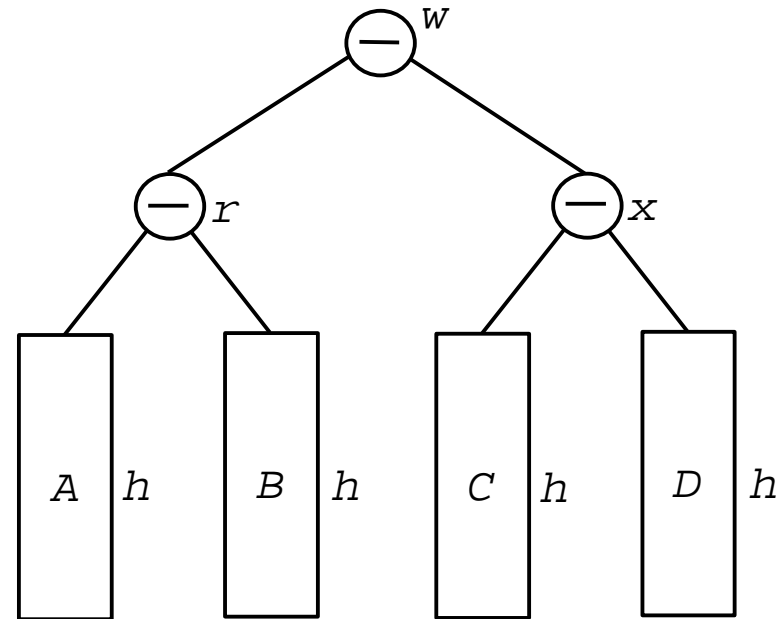


Total height = $h+2$

Rotations : Left High (Double Rotation)

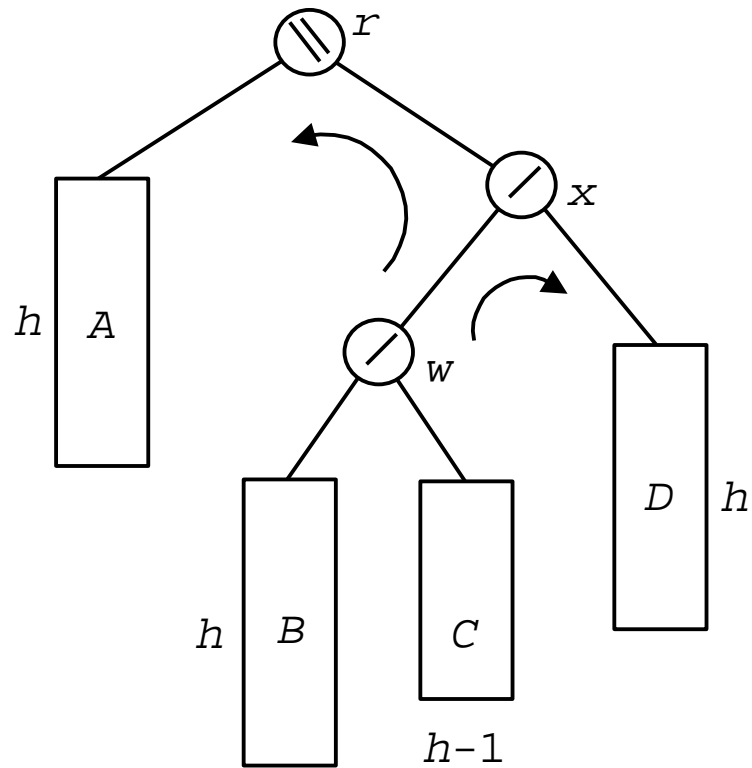


Total height = $h+3$

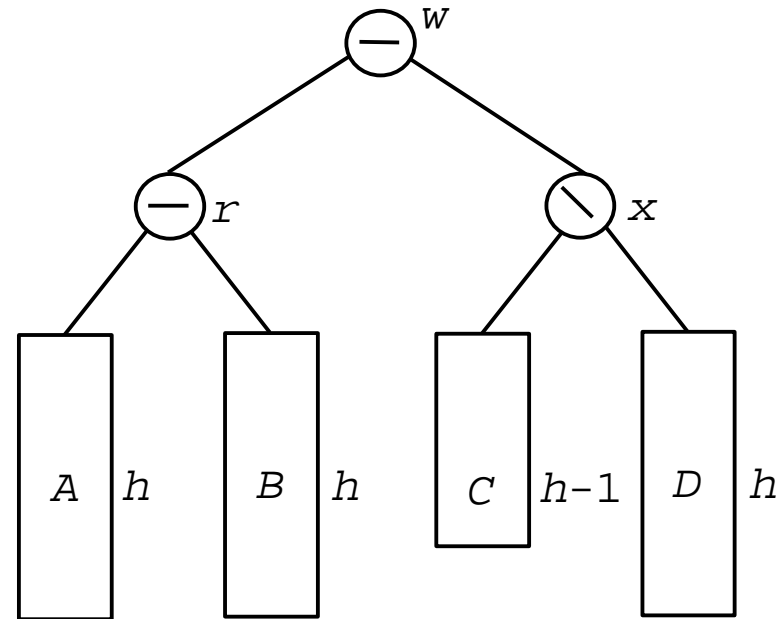


Total height = $h+2$

Rotations : Left High (Double Rotation)

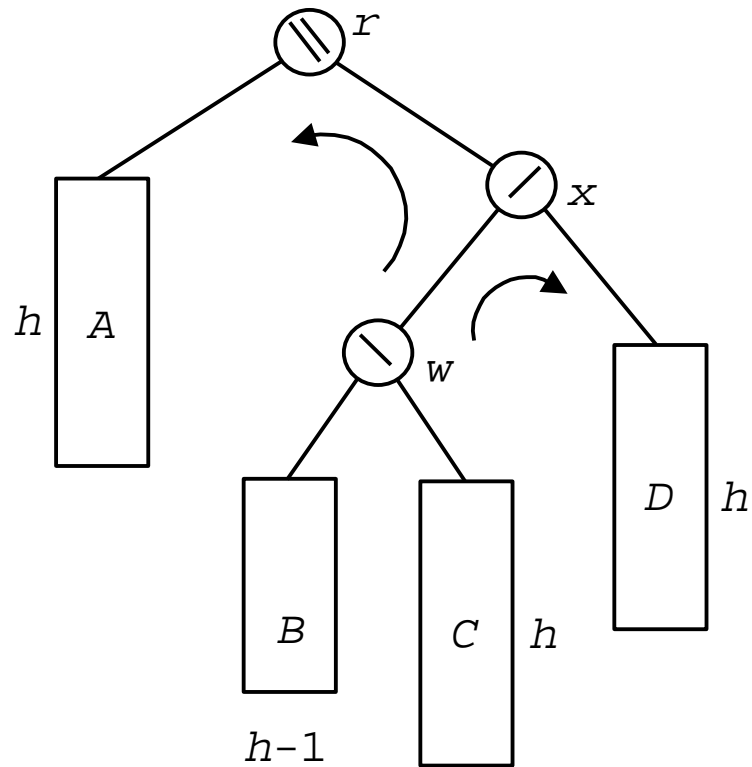


Total height = $h+3$

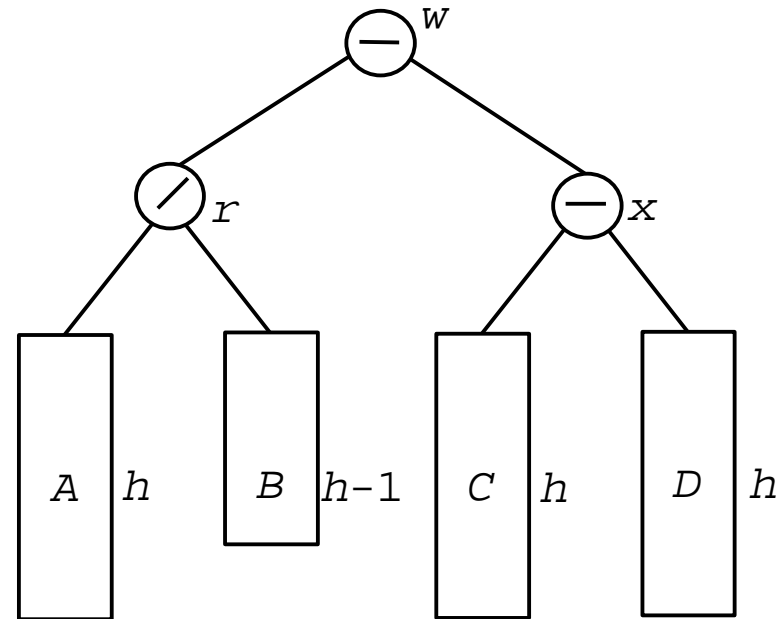


Total height = $h+2$

Rotations : Left High (Double Rotation)

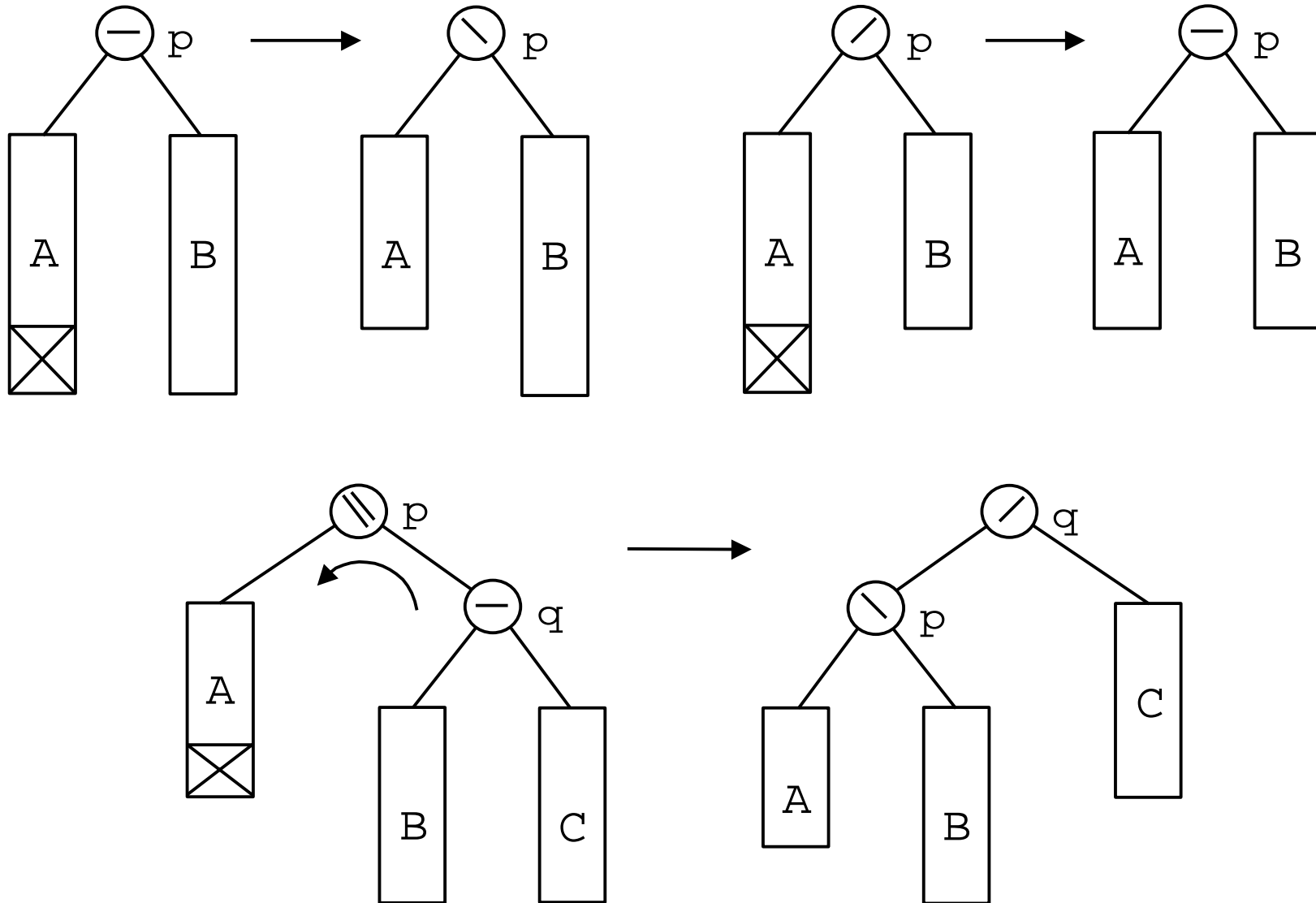


Total height = $h+3$

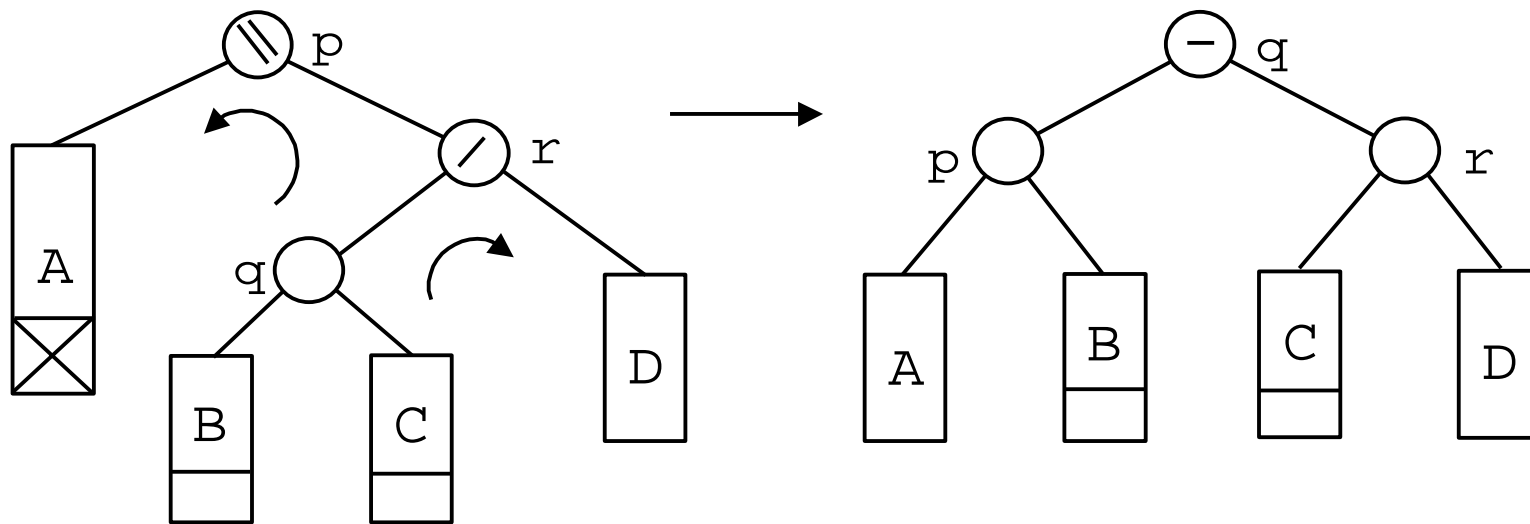
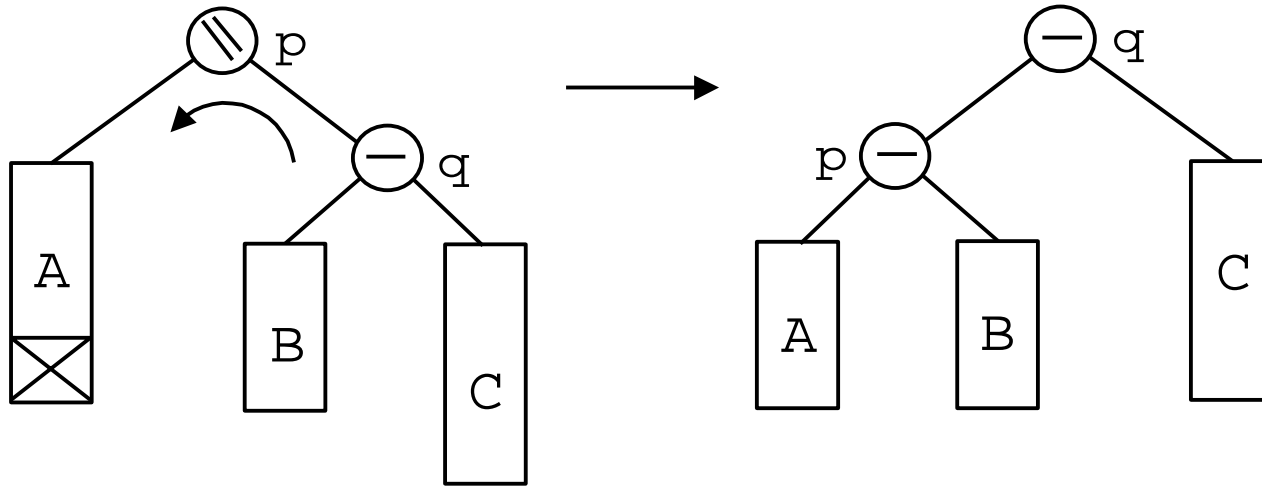


Total height = $h+2$

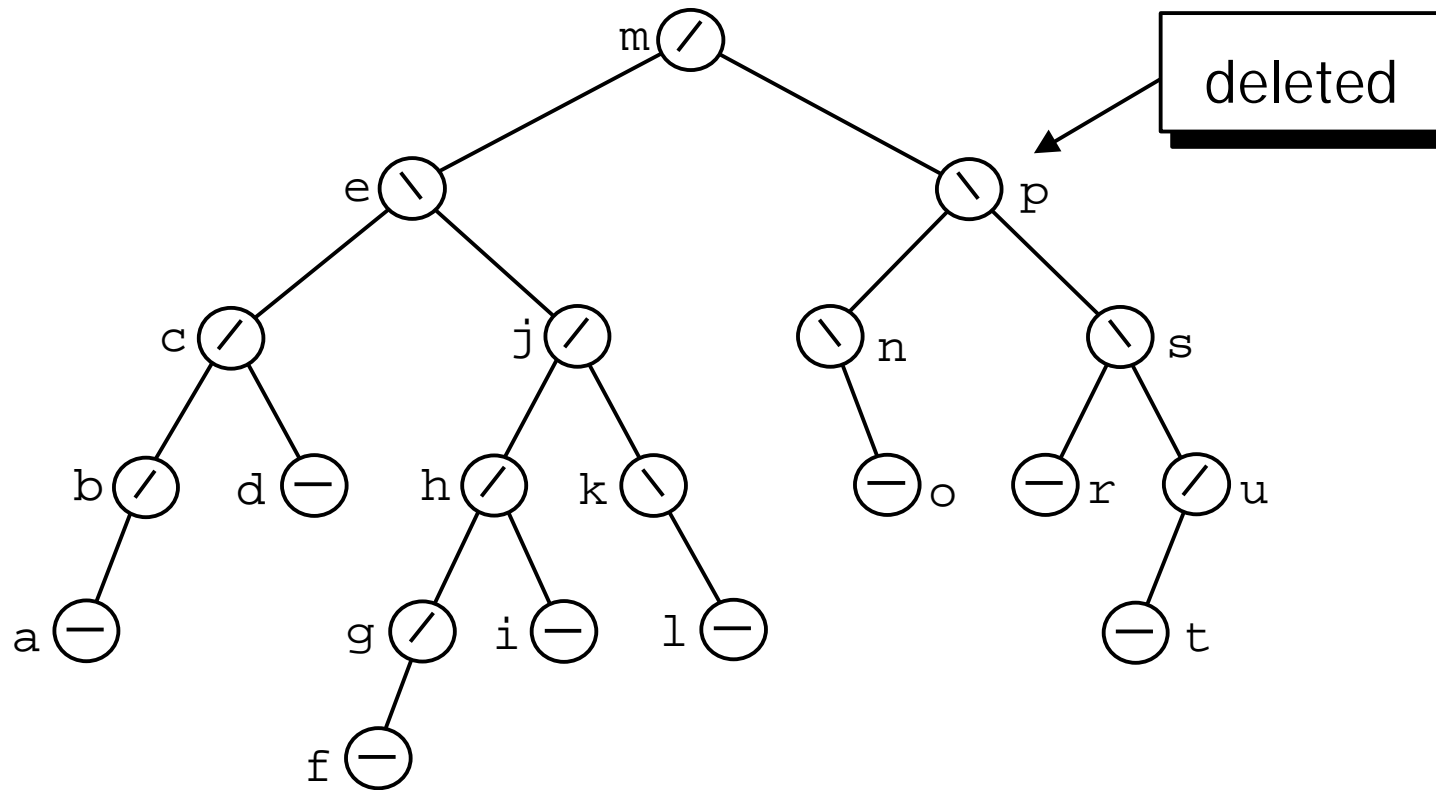
Deletion from an AVL Tree



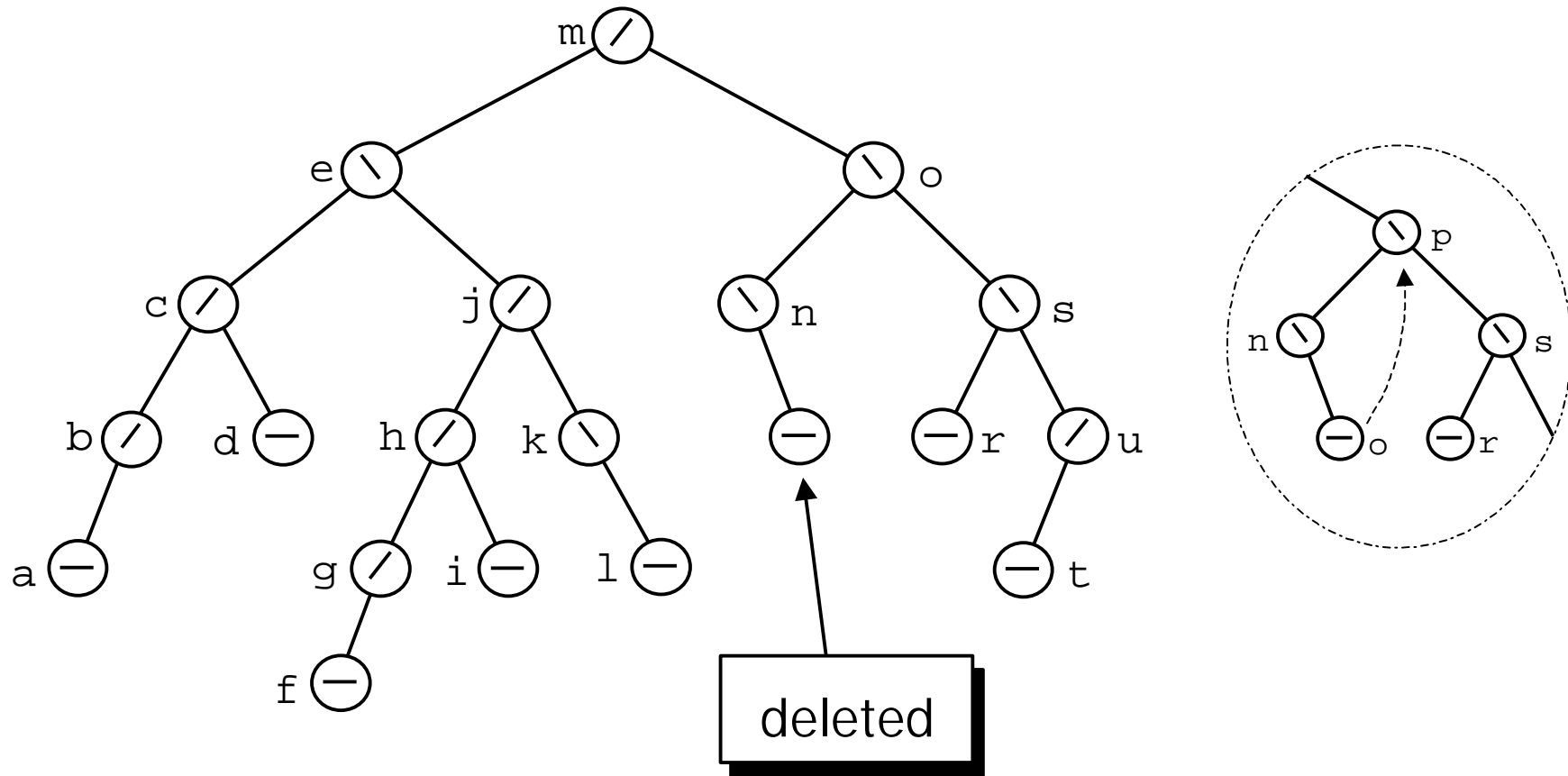
Deletion from an AVL Tree



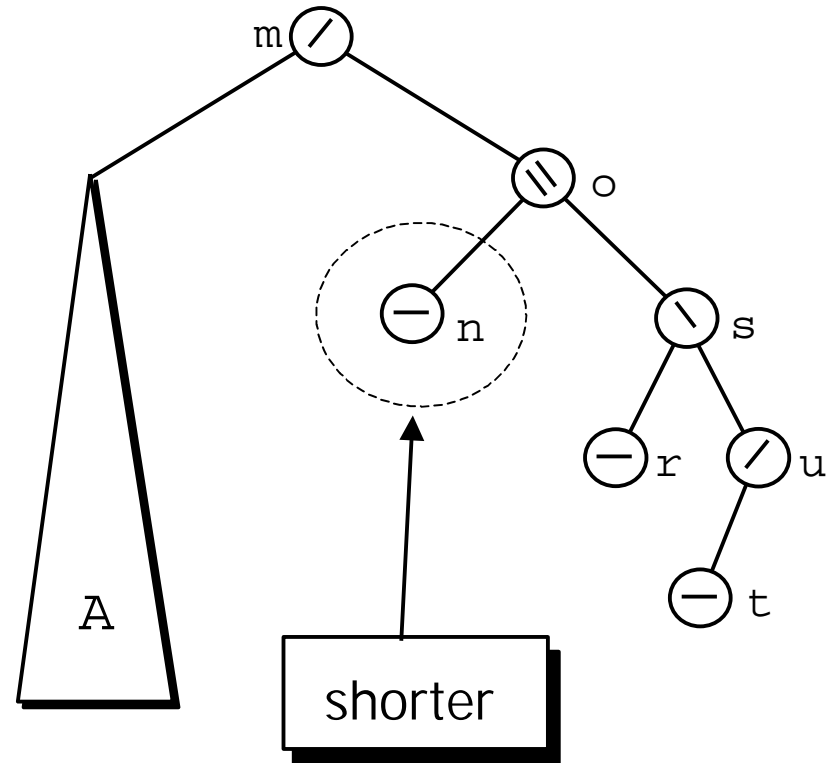
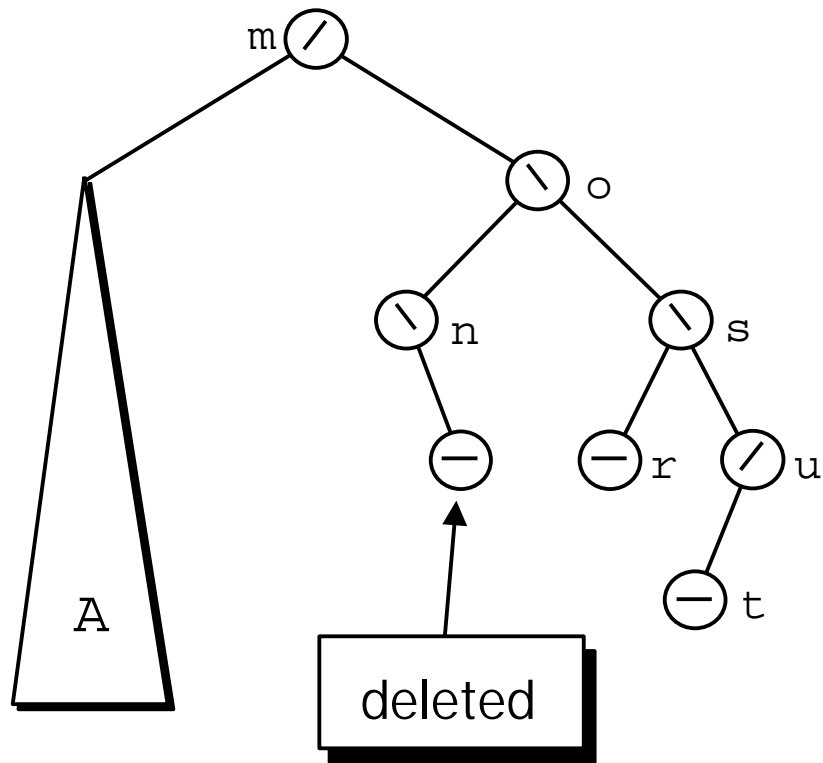
Deletion : Example



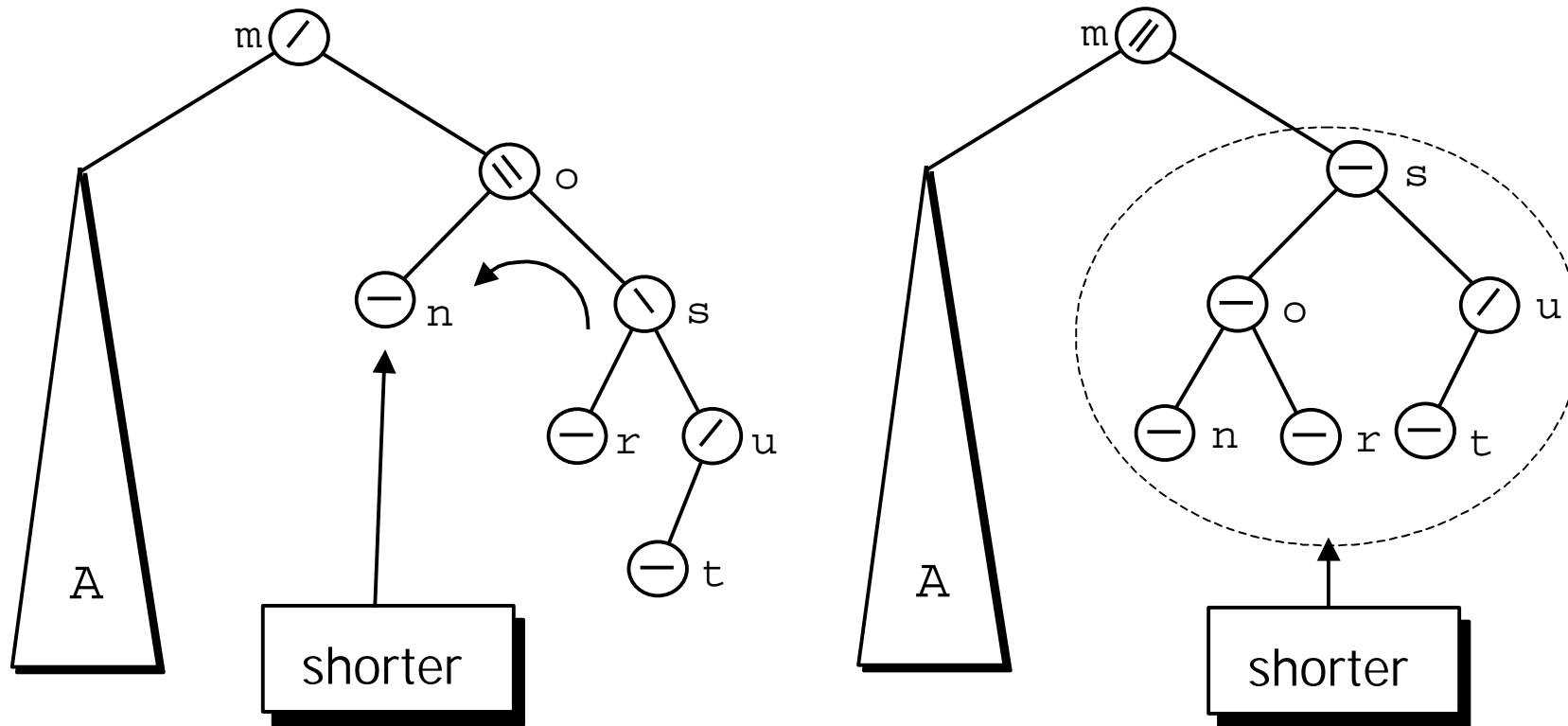
Deletion : Example



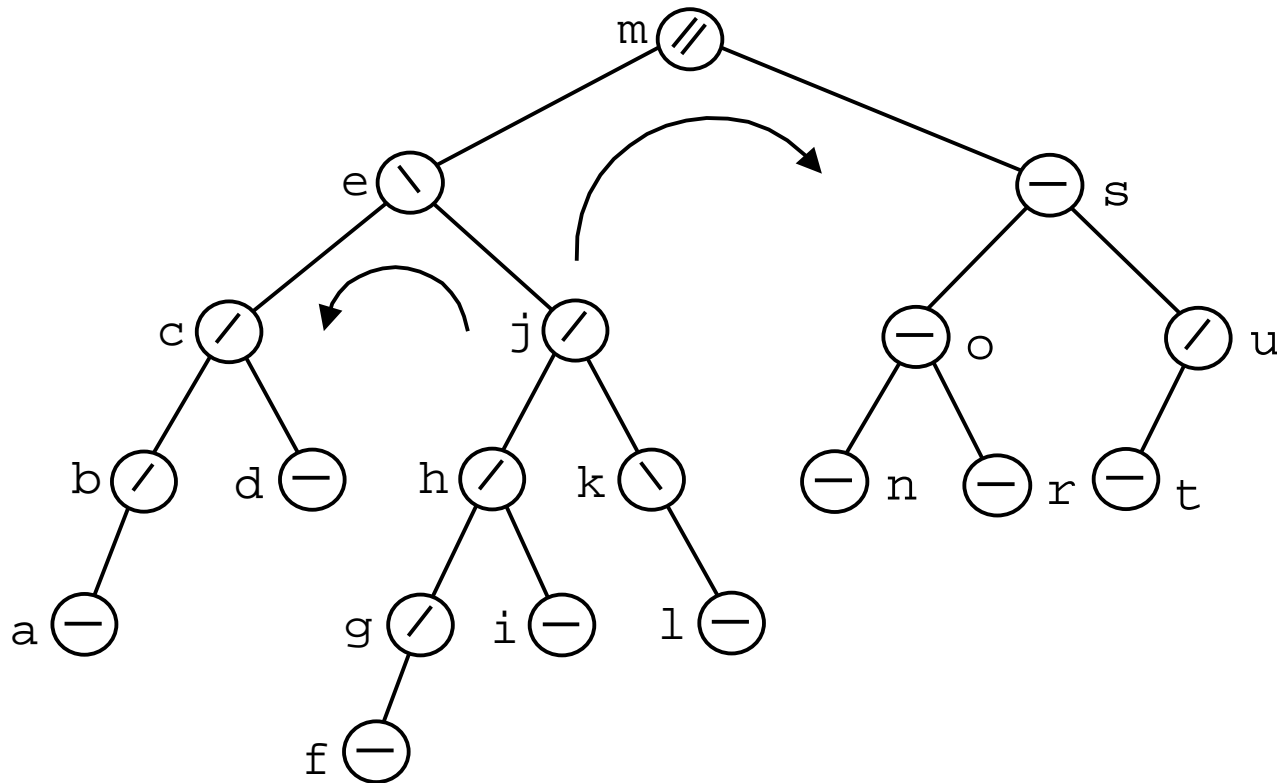
Deletion : Example



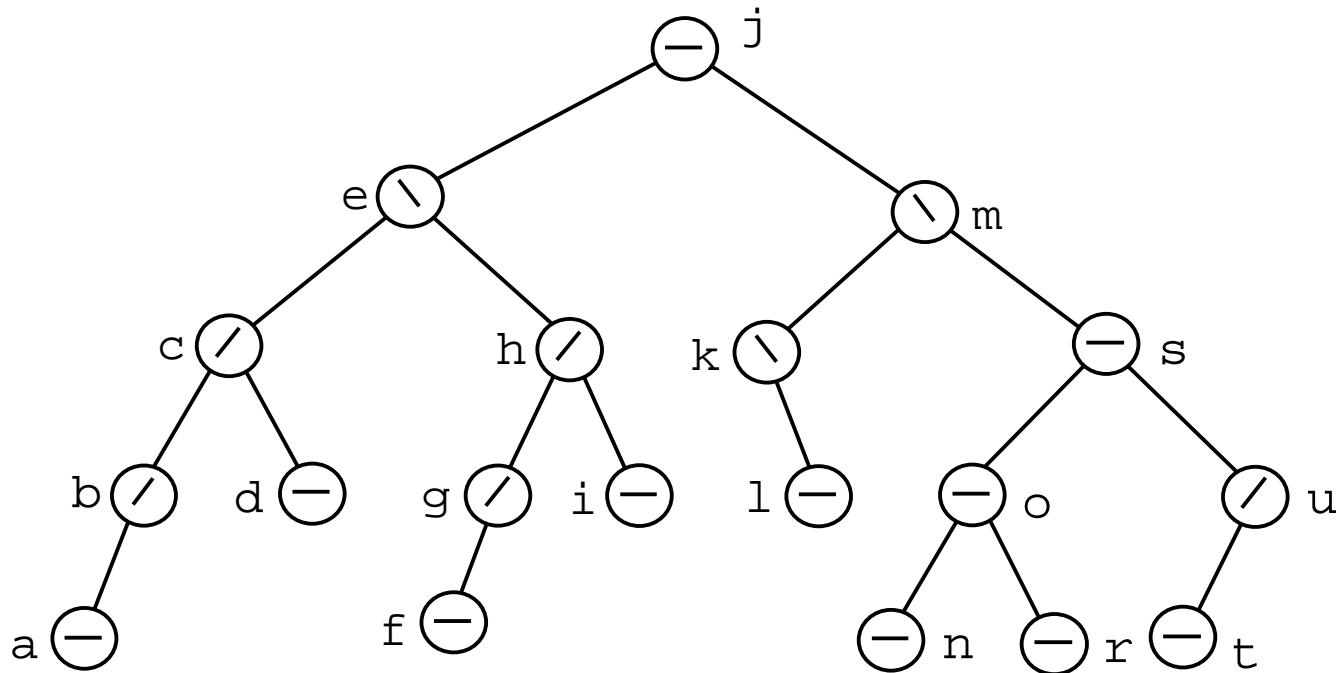
Deletion : Example



Deletion : Example

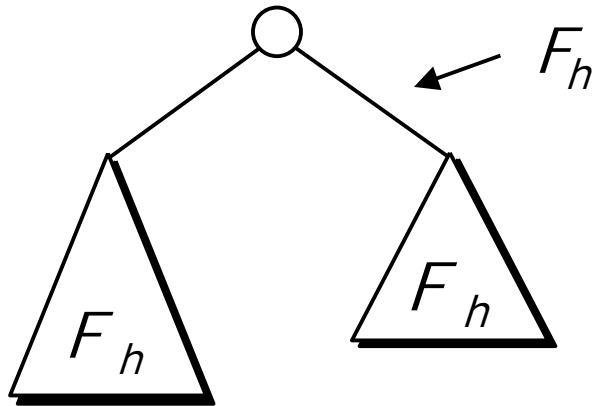


Deletion : Example



The Height of an AVL Tree

กำหนดให้ F_h คือ AVL tree ที่มีความสูง h ที่มีจำนวน nodes น้อยที่สุด
และให้ $|F_h|$ คือจำนวน nodes ของต้นไม้ F_h



Fibonacci Tree

F_h

worst-case bound