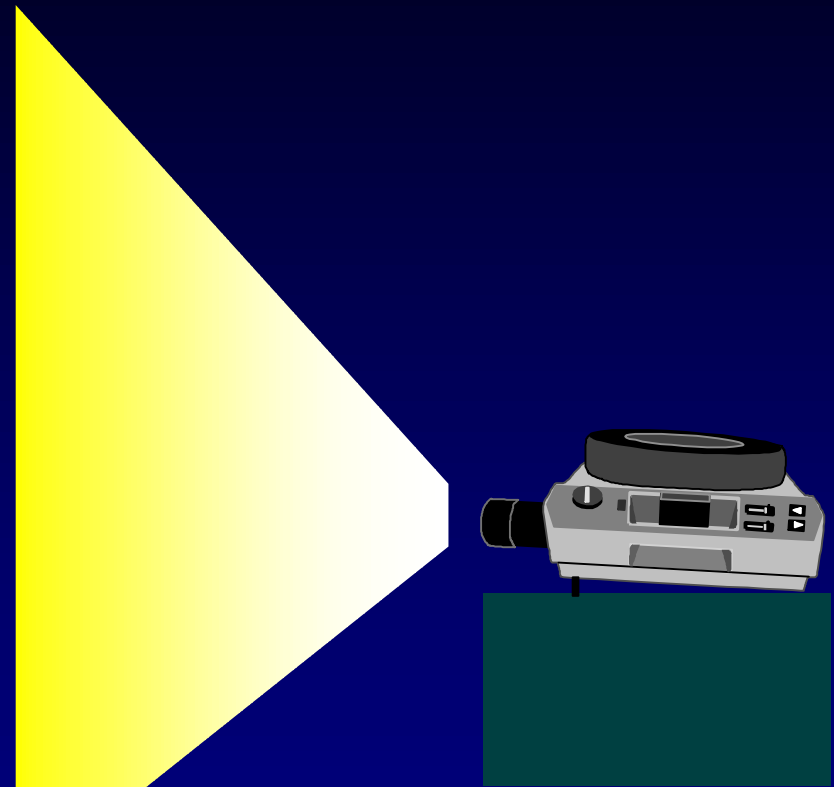


Direct Files : Outline

- Introduction
- Key-to-Address
- Hashing
- Collision
- Overflow Management
- Coalesced Chaining
- Extendible Hashing
- Linear Hashing



Direct Files

▼ Physical sequential files

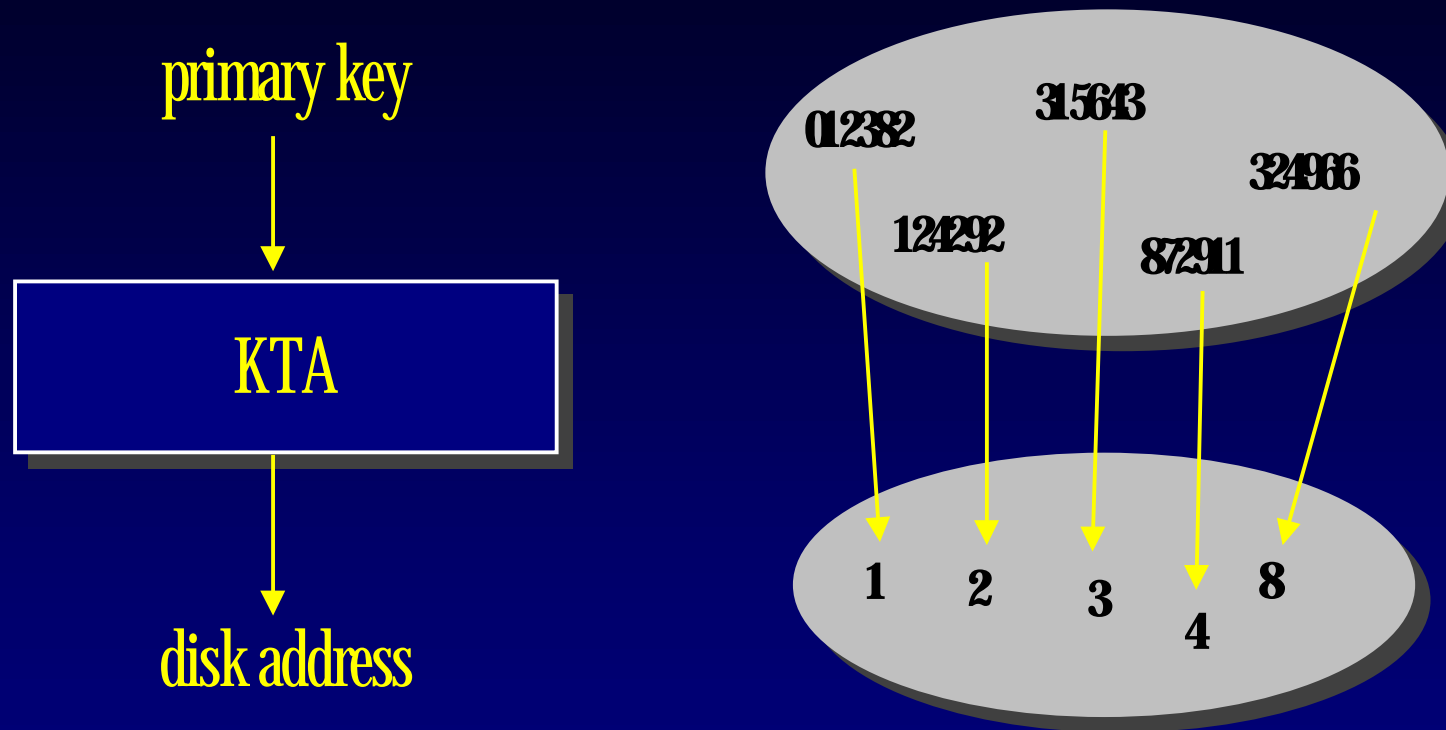
- $1 + \log NBLK$ *rba*
- $(NBLK+1) / 2$ *sba*

▼ Direct files

- 1 *rba*



Key-to-Address Transformation



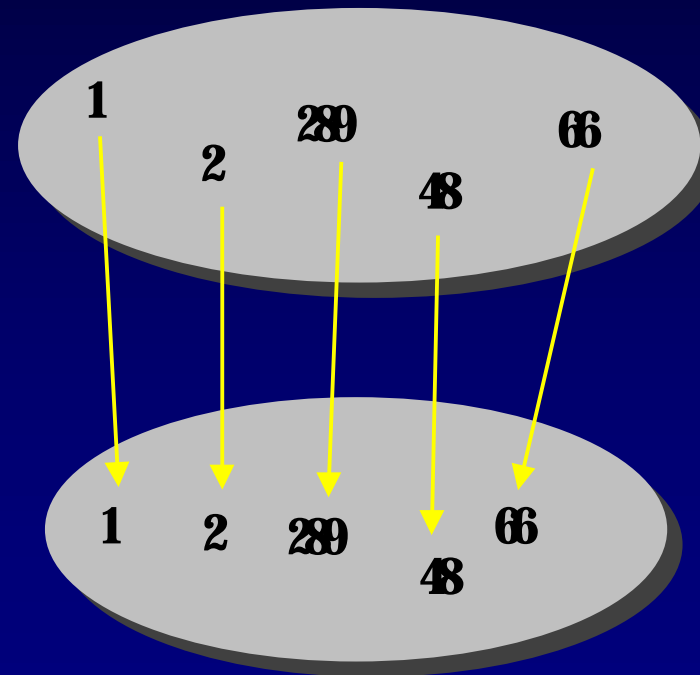
Notations

- ▼ NR : the number of records
- ▼ T : the number of allocated buckets
- ▼ B : bucket size
- ▼ LF : load factor

$$LF = \frac{NR}{T \cdot B}$$

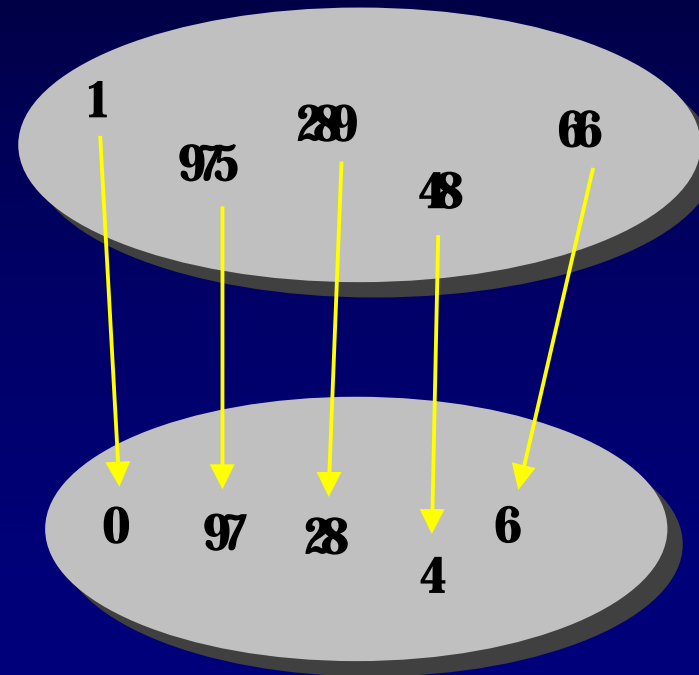
Key-to-Address

- ▼ A file of 1,000 records
- ▼ Primary keys are interger 0 to 999
- ▼ $f(key) = key$
- ▼ $T = 1,000, B = 1$
- ▼ $LF = 100\%$



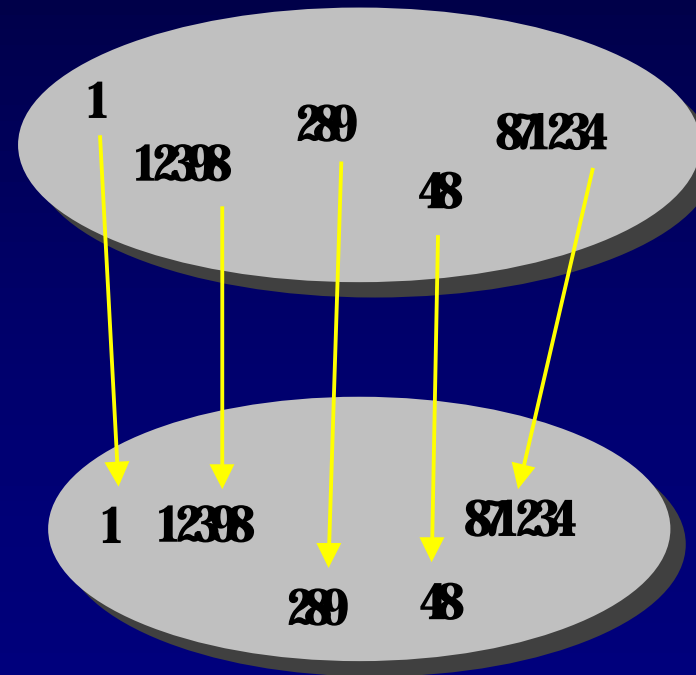
Key-to-Address

- ▼ A file of 1,000 records
- ▼ Primary keys are interger 0 to 999
- ▼ $f(key) = key \div 10$
- ▼ $T = 100, B = 10$
- ▼ $LF = 100\%$



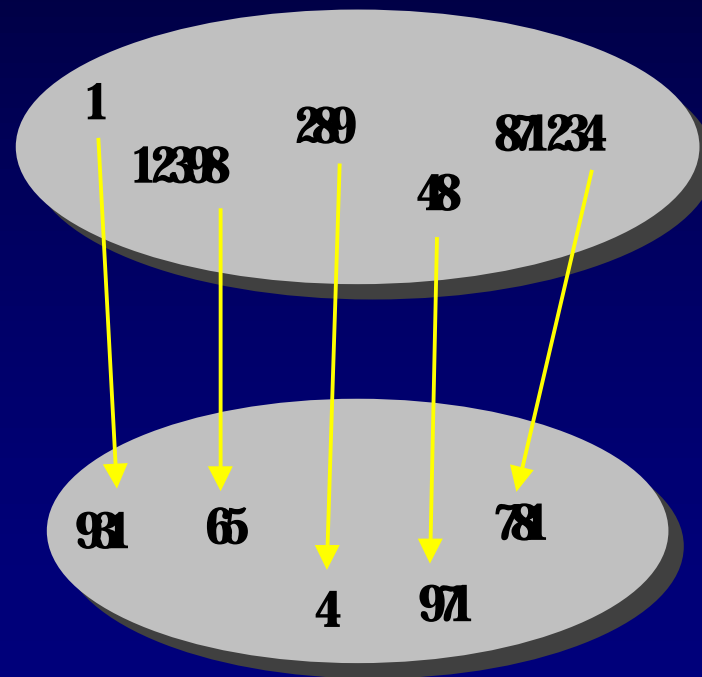
Key-to-Address

- ▼ A file of 1,000 records
- ▼ Primary keys are interger 0 to 999999
- ▼ $f(key) = key$
- ▼ $T = 1,000,000, B=1$
- ▼ $LF = 0.1\%$



Key-to-Address

- ▼ A file of 1,000 records
- ▼ Primary keys are interger 0 to 999999
- ▼ Let $T = 1,000$, $B=1$
- ▼ $f(key) = ???$
- ▼ $LF = 100\%$

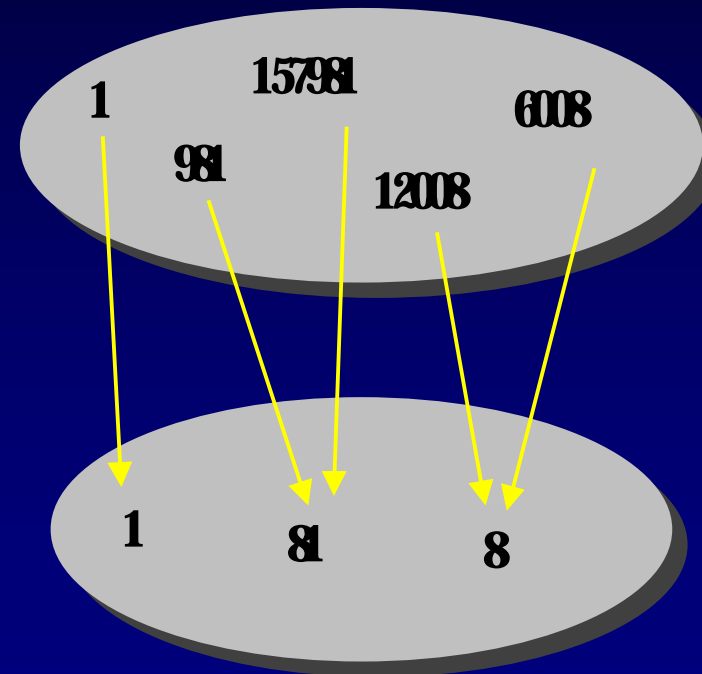


Hashing

- ▼ A file of 1,000 records
- ▼ Primary keys are interger 0 to 999999
- ▼ Let $T = 100$, $B = 10$
- ▼ $f(\text{key}) = \text{key} \bmod 100$

Collision

Record overflow



Hashing

- ▼ To avoid collision
 - perfect hashing function
- ▼ To reduce *NOR*
 - spread out the records
 - bigger *T*
 - bigger *B*

NOR = the number of overflow records

T, B, NOR, and LF

- ▼ Increase T and $B \Rightarrow$ decrease NOR, LF
- ▼ Decrease $LF \Rightarrow$ decrease space utilization
- ▼ Unacceptable, if $LF < LF_0$
- ▼ NOR depends on NR / T
- ▼ Reduce NOR , by adjusting T and B while maintaining LF

Number of Collisions

$$LF = \frac{NR}{T \cdot B}$$

Random distribution

$Dh(k)$ is the expected number of buckets that receive exactly k records under the transformation h .

Ex. $T=2000$, $NR=1500$, hashing function is randomly distributed

$$Dh(0) = 945$$

$$Dh(1) = 708$$

$$Dh(2) = 266$$

$$Dh(3) = 66$$

$$Dh(4) = 12$$

$$Dh(5) = 2$$

$$Dh(6) = 1$$

$$Dh(k) = 0, k > 6$$

Number of Overflow Records

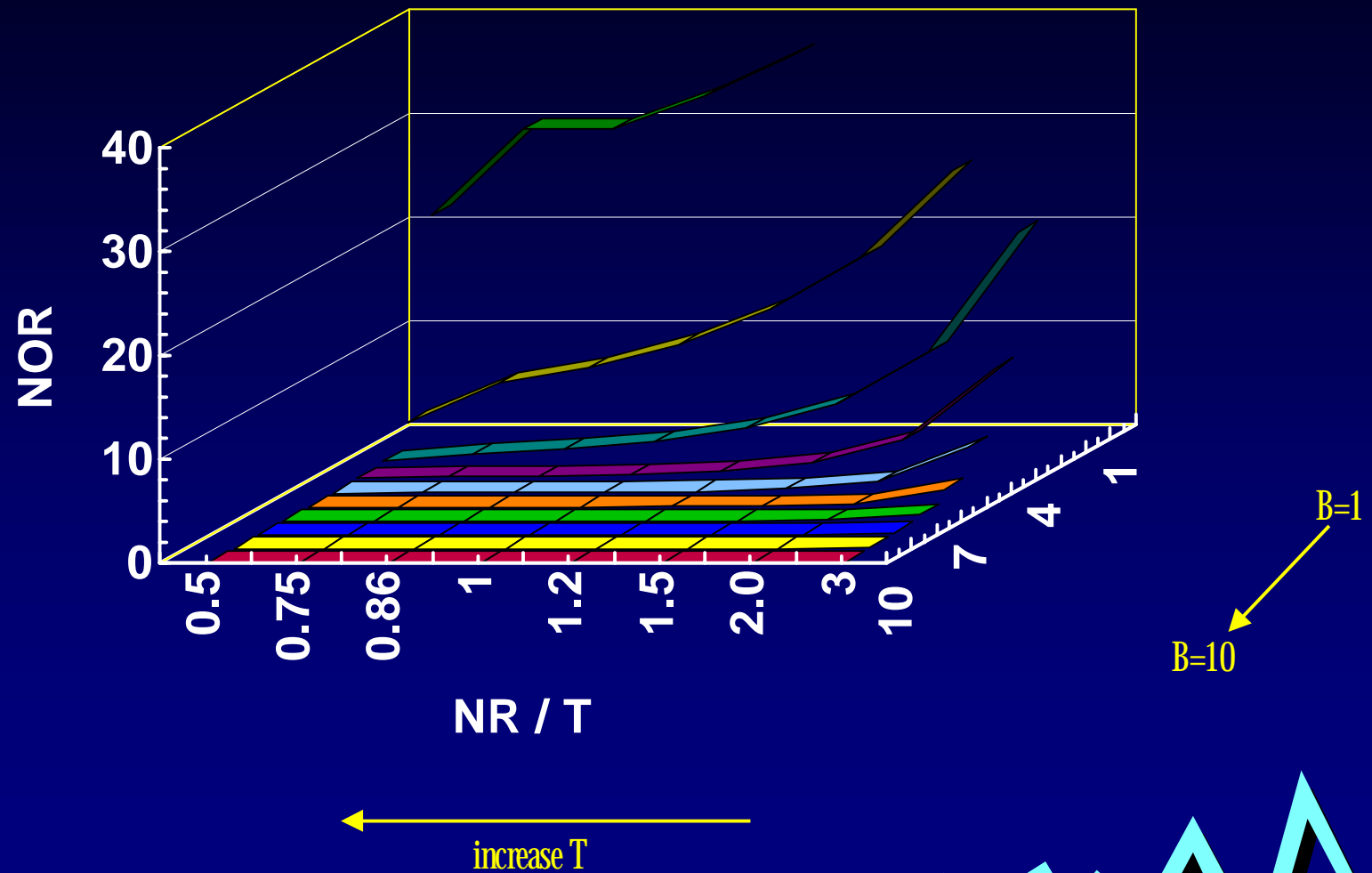
$$LF = \frac{NR}{T \cdot B}$$

Random distribution

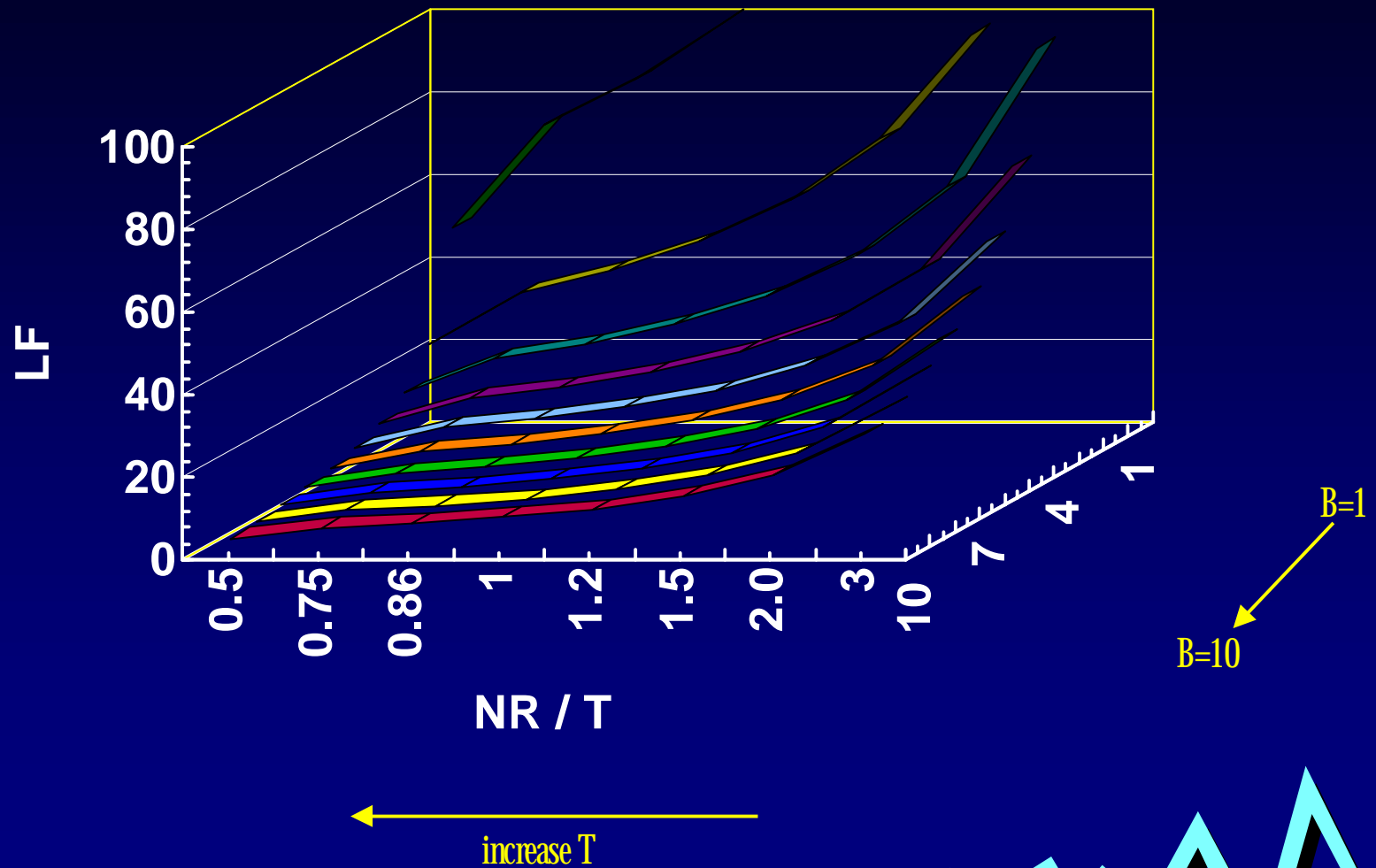
Ex. $T=2000$, $NR=1500$, hashing function is randomly distributed and $B=2$.

$$\begin{aligned} \text{NOR} &= 3xDh(3) + 4xDh(4) + 5xDh(5) + 6xDh(6) \\ &= 3x66 + 4x12 + 5x2 + 6x1 \\ &= 262 \text{ records} \end{aligned}$$

NOR vs. B and T

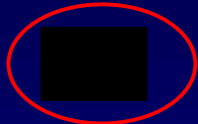


LF vs. B and T



T, B, LF, NOR

	Bucket size									Bucket size								
0	0.0	0.0	0.0	0.0	0.0	0.4	2.8	5.0	5.6	6.3	7.1	8.3	10.0	12.5	16.7	25.0	50.0	
0.75	0.0	0.0	0.0	0.0	0.2	1.1	6.5	7.5	8.3	9.4	10.7	12.5	15.0	18.8	25.0	37.5	75.0	
0.86	0.0	0.0	0.0	0.0	0.3	1.6	8.1	8.6	9.5	10.7	12.2	14.3	17.1	21.4	28.6	42.9	85.7	
1	0.0	0.0	0.0	0.0	0.1	0.4	2.3	10.3	10.0	11.1	12.5	14.3	16.7	20.0	25.0	33.3	50.0	100.0
1.2	0.0	0.0	0.0	0.0	0.1	0.8	3.6	13.7	12.0	13.3	15.0	17.1	20.0	24.0	30.0	40.0	60.0	
1.5	0.0	0.0	0.0	0.1	0.3	1.6	5.9	18.6	15.0	16.7	18.8	21.4	25.0	30.0	37.5	50.0	75.0	
2.0	0.0	0.0	0.0	0.3	1.1	3.7	10.8	27.0	20.0	22.2	25.0	28.6	33.3	40.0	50.0	66.7	100.0	
3	0.0	0.1	0.6	1.7	4.5	10.6	22.4	30.0	33.3	37.5	42.9	50.0	60.0	75.0	100.0			



OverflowRecords(%)

LoadFactor(%)

